

IDPASC School, Santiago de Compostela, 21 Jan.-2 Feb., 2013

Theoretical cosmology

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Hubble Space Telescope image
of supernova 1994D in galaxy
NGC 4526 ($z=0.0015$)

Outline of the Course

1.- Cosmological observations and FLRW models

2.- Thermodynamics in an expanding universe: decoupling and dark matter

3.- Inflation

4.- Cosmological perturbations and CMB anisotropies

Observational basis of Cosmology

Cosmology studies the origin, evolution and structure of the universe on large scales (larger than the galaxy scale)

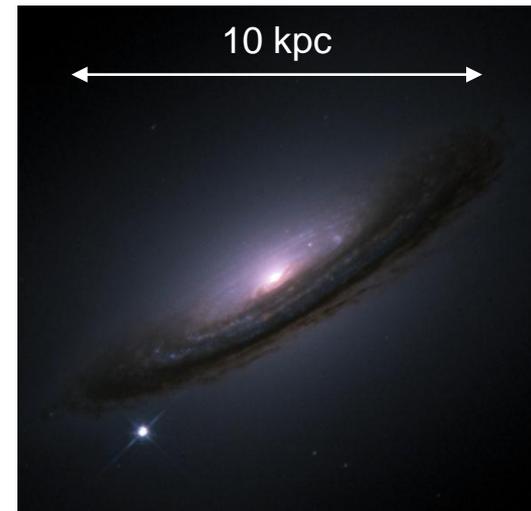
$$1 \text{ pc} = 3.26 \text{ light years} = 3.09 \times 10^{16} \text{ m}$$

Galaxy

10^{11} stars

$$M_{\text{gal}} = 10^{42} \text{ kg}$$

$$L_{\text{gal}} = 10 \text{ kpc}$$



*On these scales **gravitation** is the only relevant interaction*

Observational basis of Cosmology

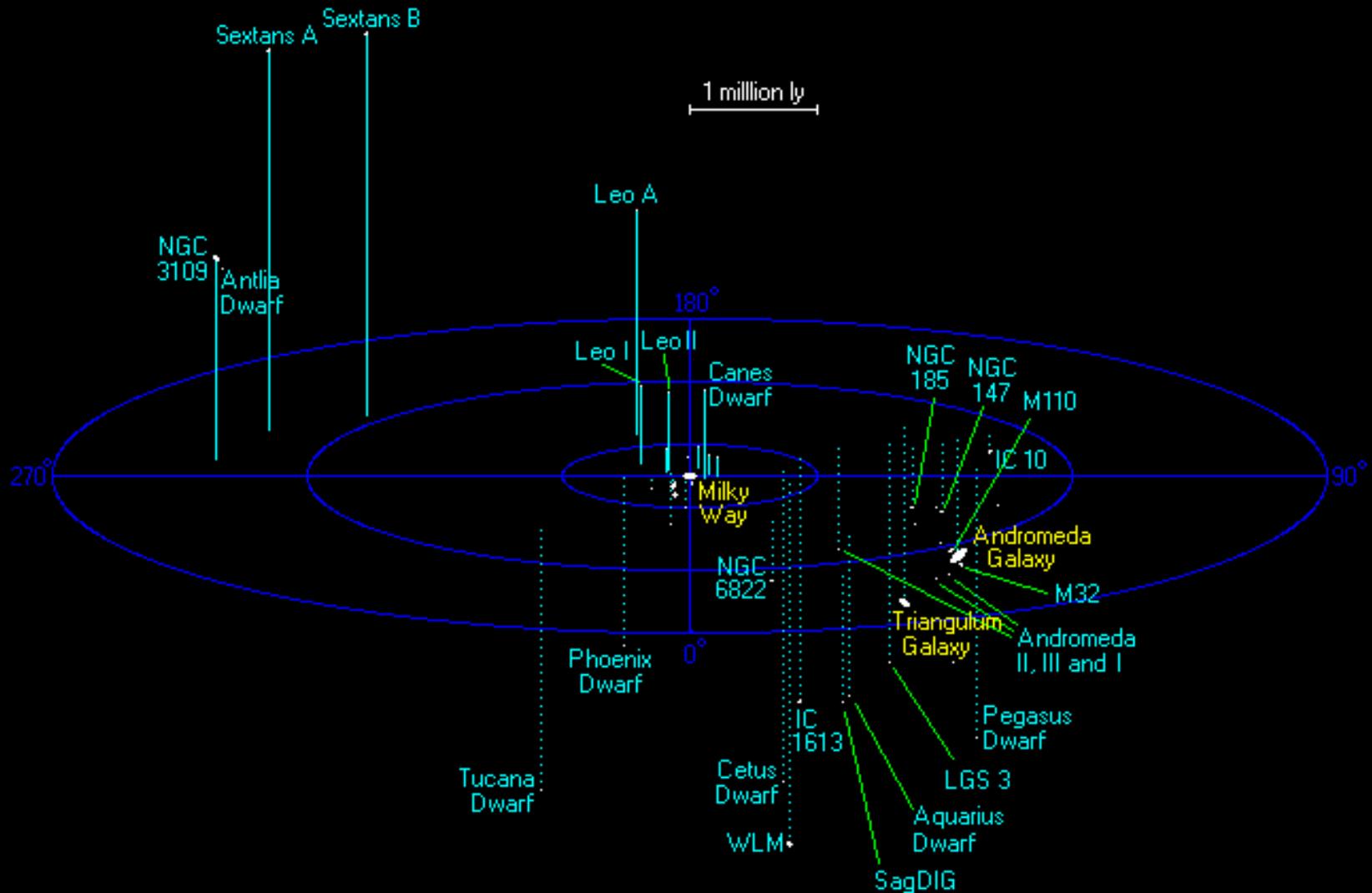
1.- Matter distribution and matter density in the universe: dark matter

2.- Universe expansion and acceleration: dark energy

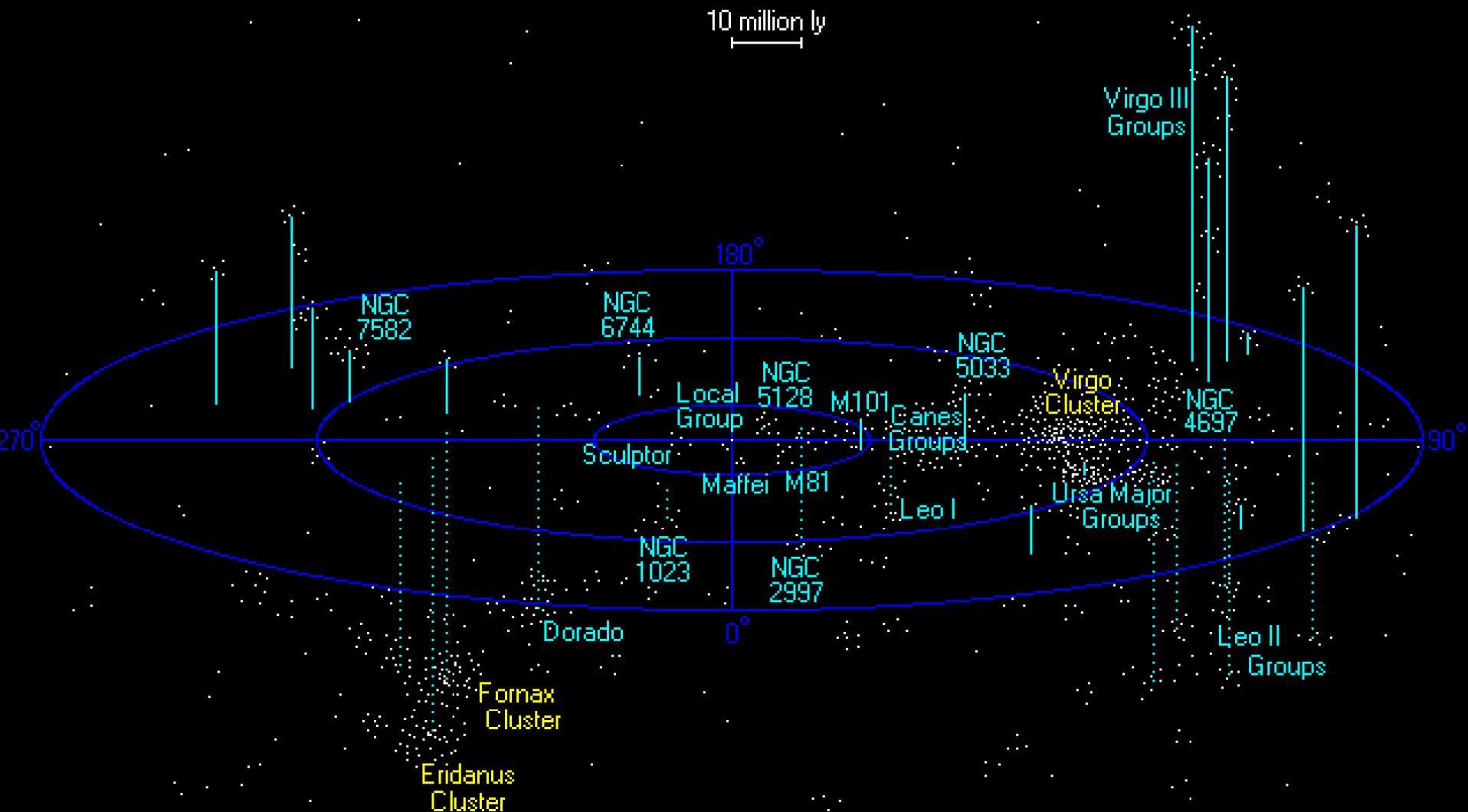
3.- Light elements abundances

4.- Cosmic microwave background and anisotropies

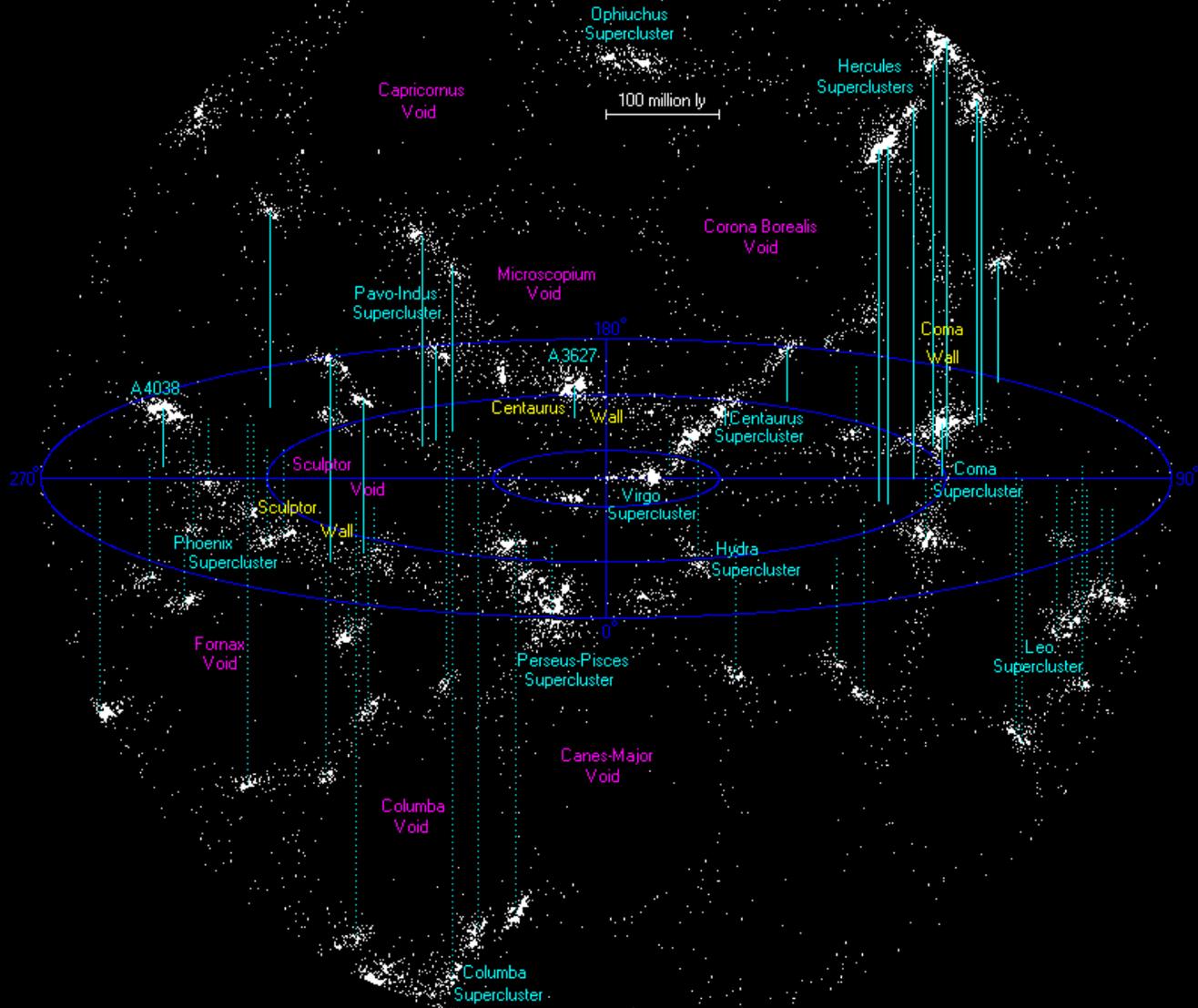
1.- Matter distribution on large scales: the universe within 1.5 Mpc: Local Group



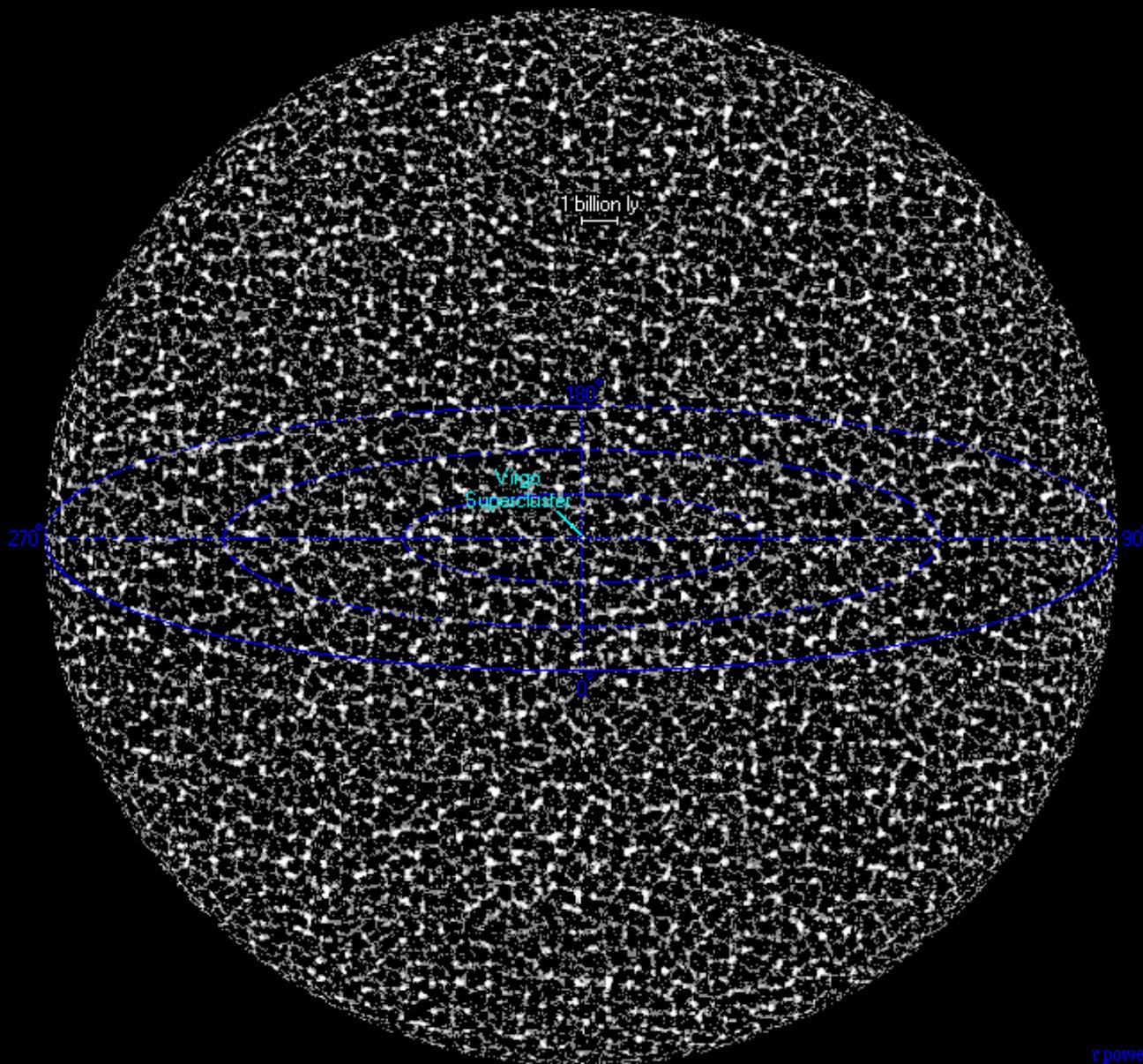
The universe within 30 Mpc: Virgo supercluster



Superclusters, filaments, walls and voids within 150 Mpc

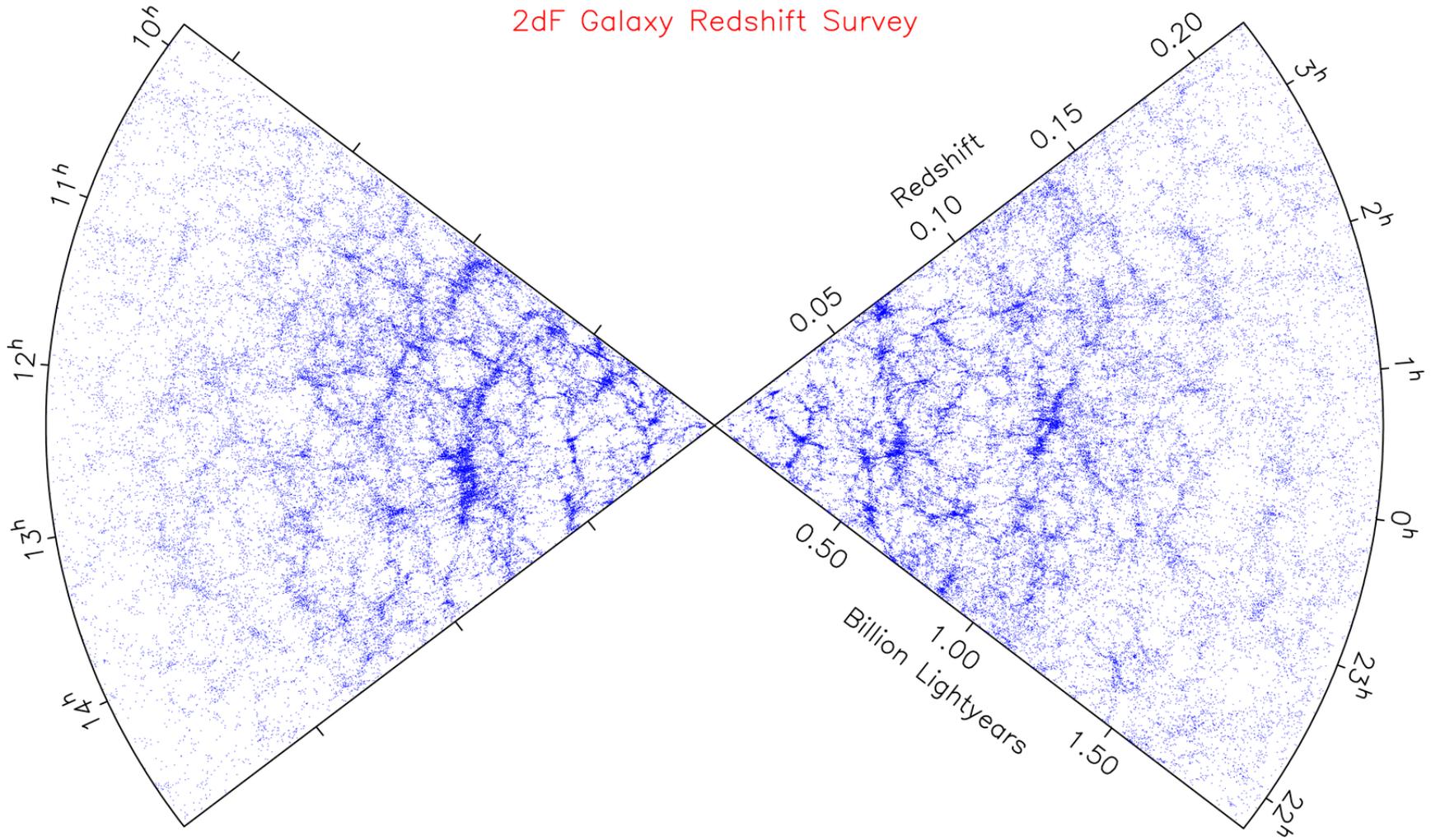


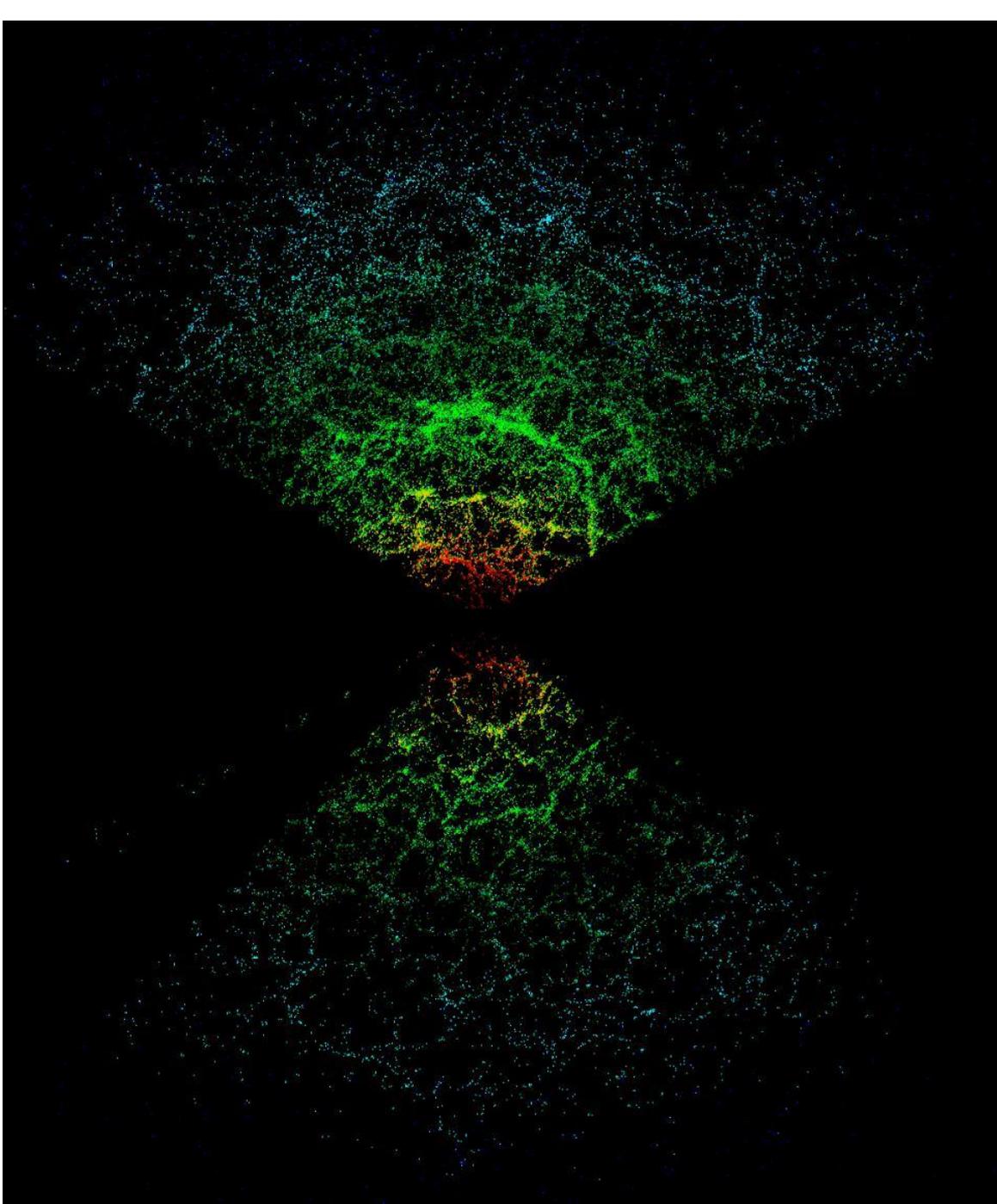
The universe within 4300 Mpc: large scale homogeneity



The Universe within 600 Mpc

2dF Galaxy Redshift Survey

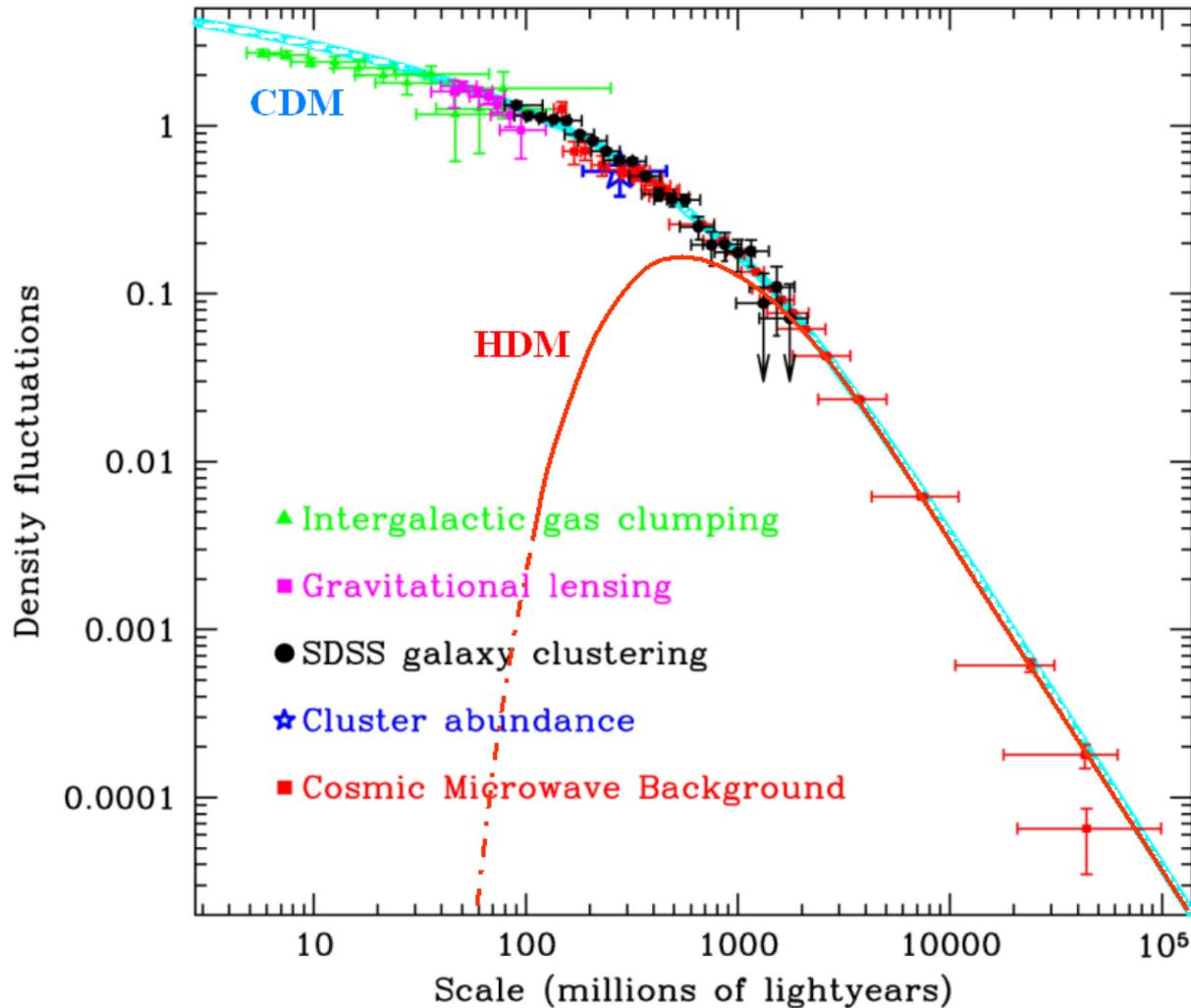




**The Universe within 600
Mpc
(Sloan Digital Sky Survey)**

Matter density fluctuations:

Statistical homogeneity $R \gg 100$ Mpc (Cosmological Principle)

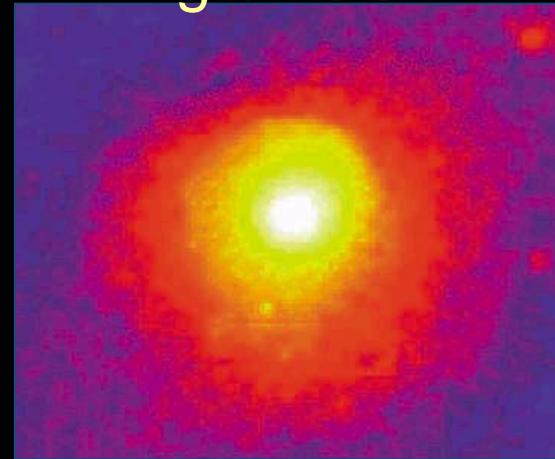


Matter density of the universe: luminous vs. dark matter



VISIBLE

Virgo/ROSAT



X RAY

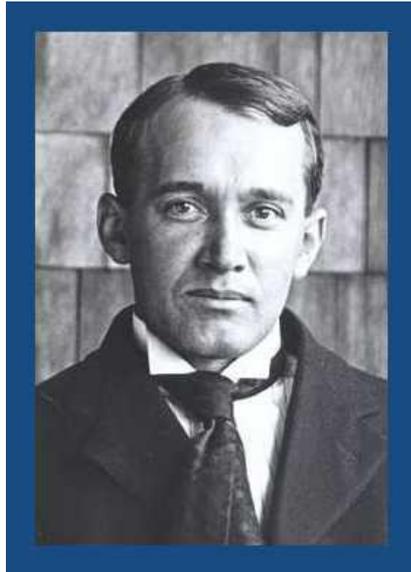
Virial mass: $M/L = 200$

$$\rho_M = \langle \mathcal{L} \rangle M/L, \quad \langle \mathcal{L} \rangle = (2.0 \pm 0.2) \times 10^8 h L_\odot \text{Mpc}^{-3}.$$

$$\Omega_M = \rho_M / \rho_c = 0.266 \pm 0.029$$

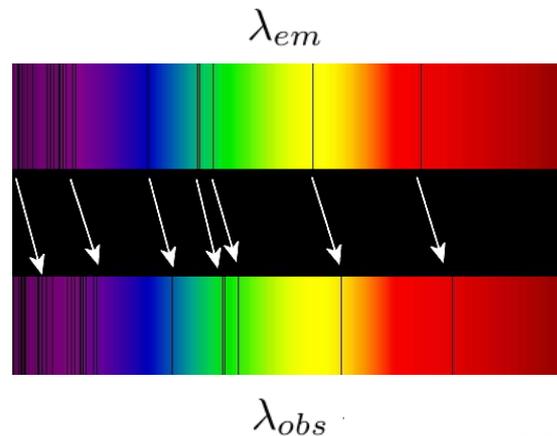
$$\Omega_{lum} = 0.005 \pm 0.002$$

2.- The expansion of the universe



Vesto M. Slipher
(1875-1969, USA),
Lowell Observatory

Discovers in 1915
the recession of galaxies



$$\frac{\lambda_{obs} - \lambda_{em}}{\lambda_{em}} = z$$

$$z \simeq \frac{v}{c}, \quad v \ll c$$

z = redshift

NEBULÆ.

By V. M. SLIPHER, PH.D.

(Read April 13, 1917.)

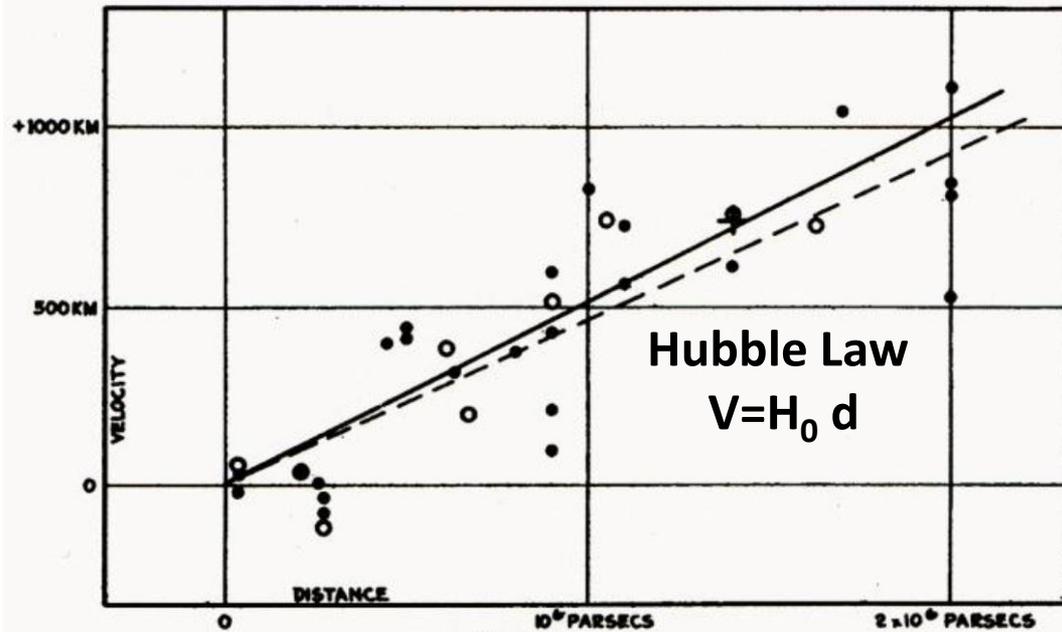
RADIAL VELOCITIES OF TWENTY-FIVE SPIRAL NEBULÆ.

Nebula.	Vel.	Nebula.	Vel.
N.G.C. 221	- 300 km.	N.G.C. 4526	+ 580 km.
224	- 300	4565	+ 1100
598	- 260	4594	+ 1100
1023	+ 300	4649	+ 1090
1068	+ 1100	4736	+ 290
2683	+ 400	4826	+ 150
3031	- 30	5005	+ 900
3115	+ 600	5055	+ 450
3379	+ 780	5194	+ 270
3521	+ 730	5236	+ 500
3623	+ 800	5866	+ 650
3627	+ 650	7331	+ 500
4258	+ 500		

Distance-redshift relation: Lemaître-Hubble (1927-29)

Cepheids as standard candles

(distances up to 3 Mpc ($z=0.001$), or 20 Mpc with HST ($z = 0.005$))



Hubble constant

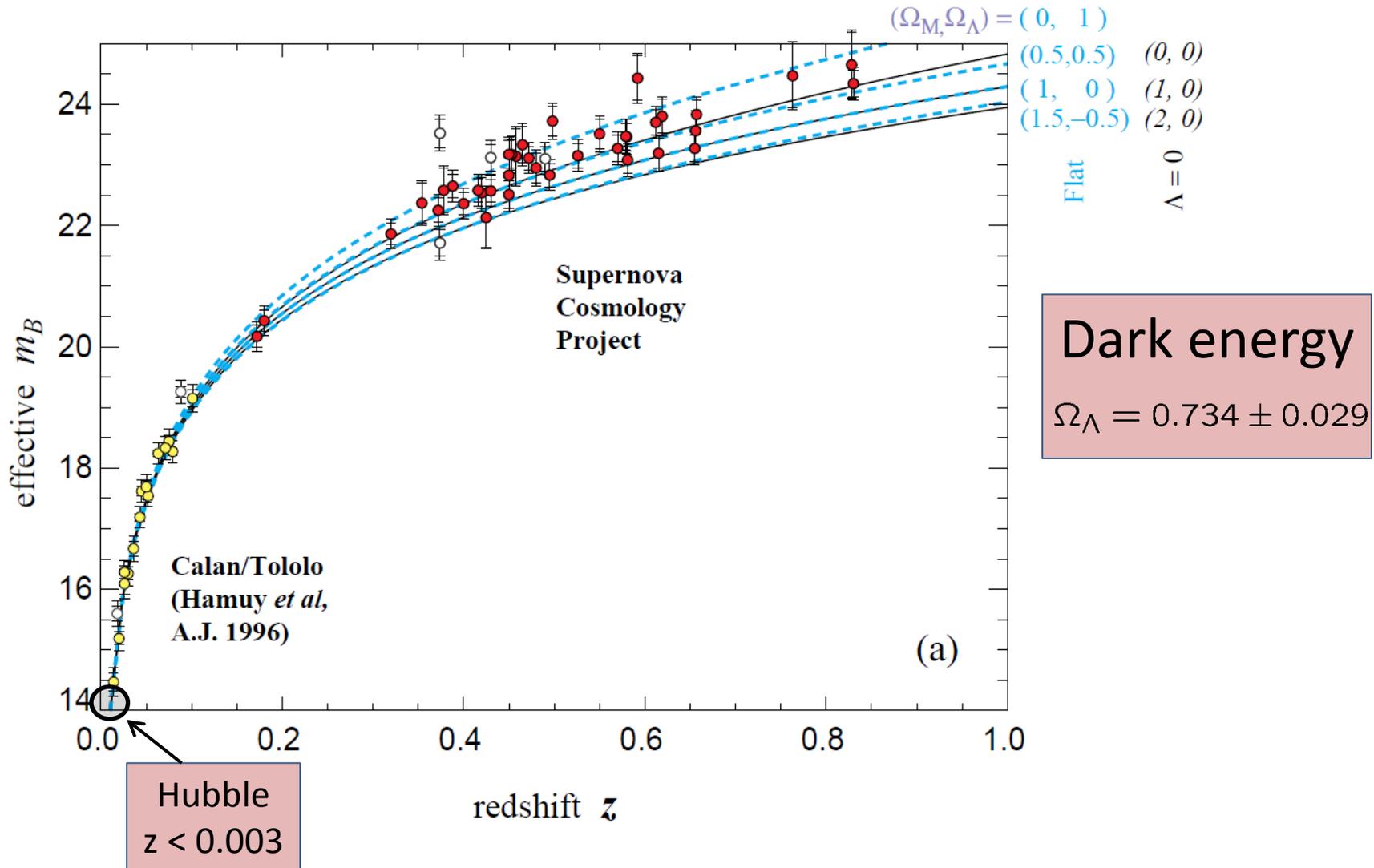
$$H_0 = 73.8 \pm 2.4 \text{ km/s/Mpc}$$

$$h = 0.738$$

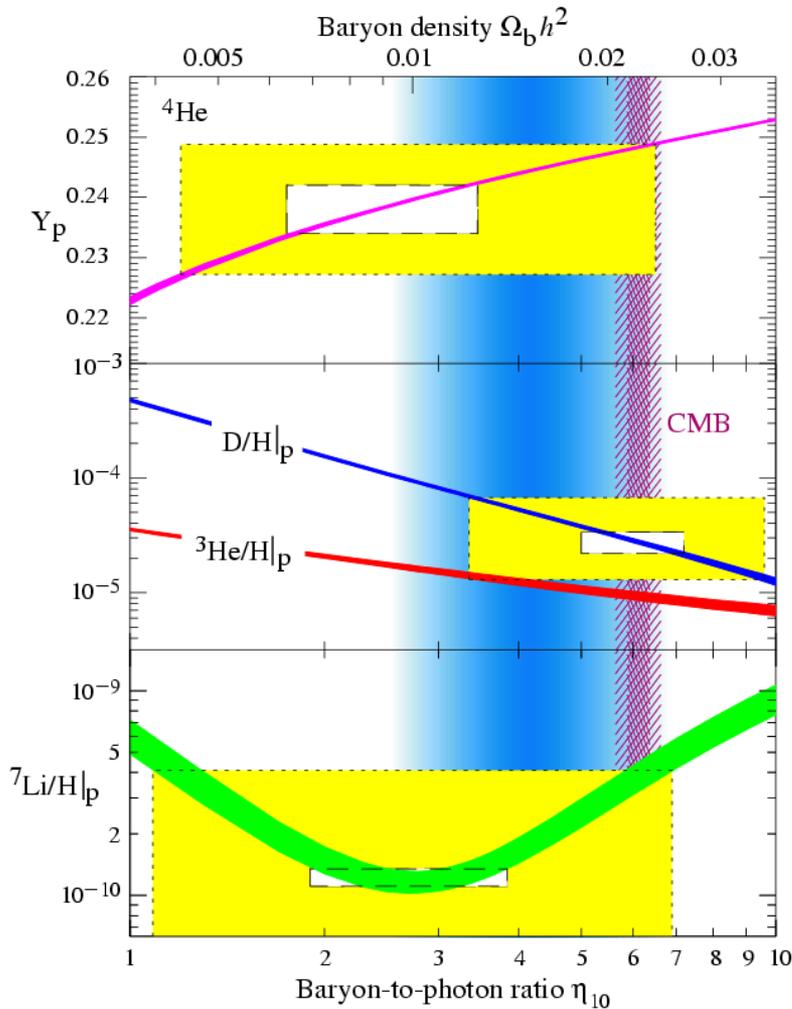
Age of the universe

$$t_0 \simeq H_0^{-1} \simeq 13700 \text{ Myears}$$

Accelerated expansion of the universe (1998)



3.- Light elements abundances



D, ³He, ⁴He, ⁷Li

$t_{\text{BBN}} = 1\text{s} - 3\text{ min}$, $T_{\text{BBN}} = 1 - 0.1\text{ MeV}$

Baryon asymmetry

$$\eta = \frac{n_B - n_{\bar{B}}}{n_\gamma} = (4.6 - 5.9) \times 10^{-10}$$

Baryon density

$$\Omega_B = \frac{\rho_B}{\rho_c} = 0.0449 \pm 0.0028$$

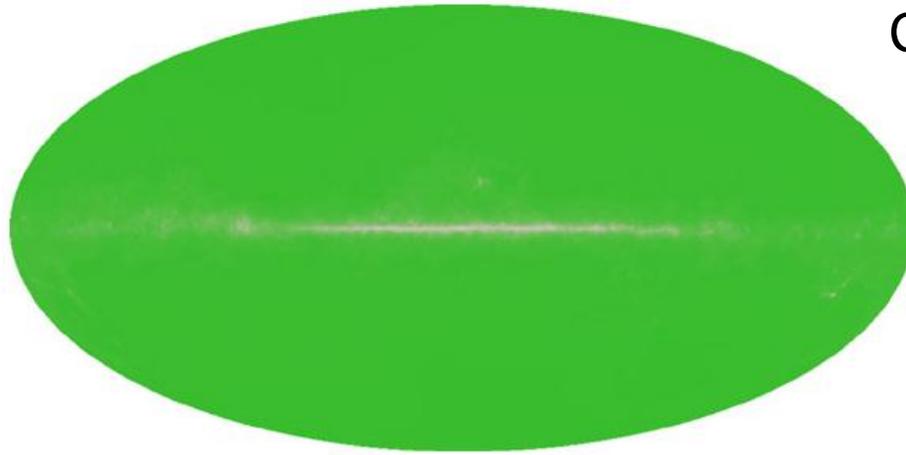
$$0.3 \quad 0.04 \quad 0.005$$

$$\Omega_M \gg \Omega_B \gg \Omega_{lum}$$

Non-baryonic dark matter problem

Baryonic dark matter problem

4.- Cosmic microwave background

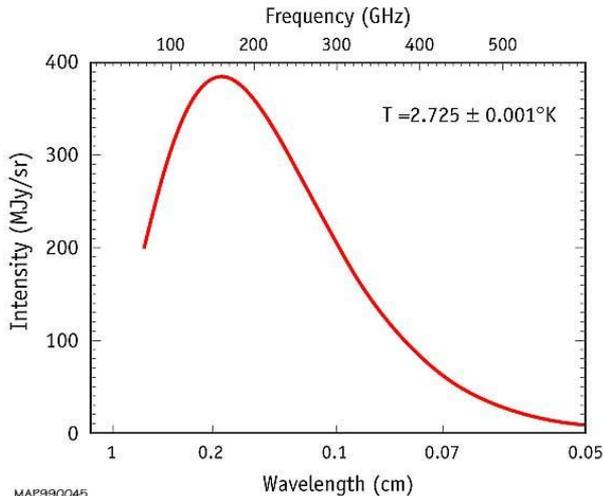


CMB monopole

1965

Penzias and Wilson

SPECTRUM OF THE COSMIC MICROWAVE BACKGROUND

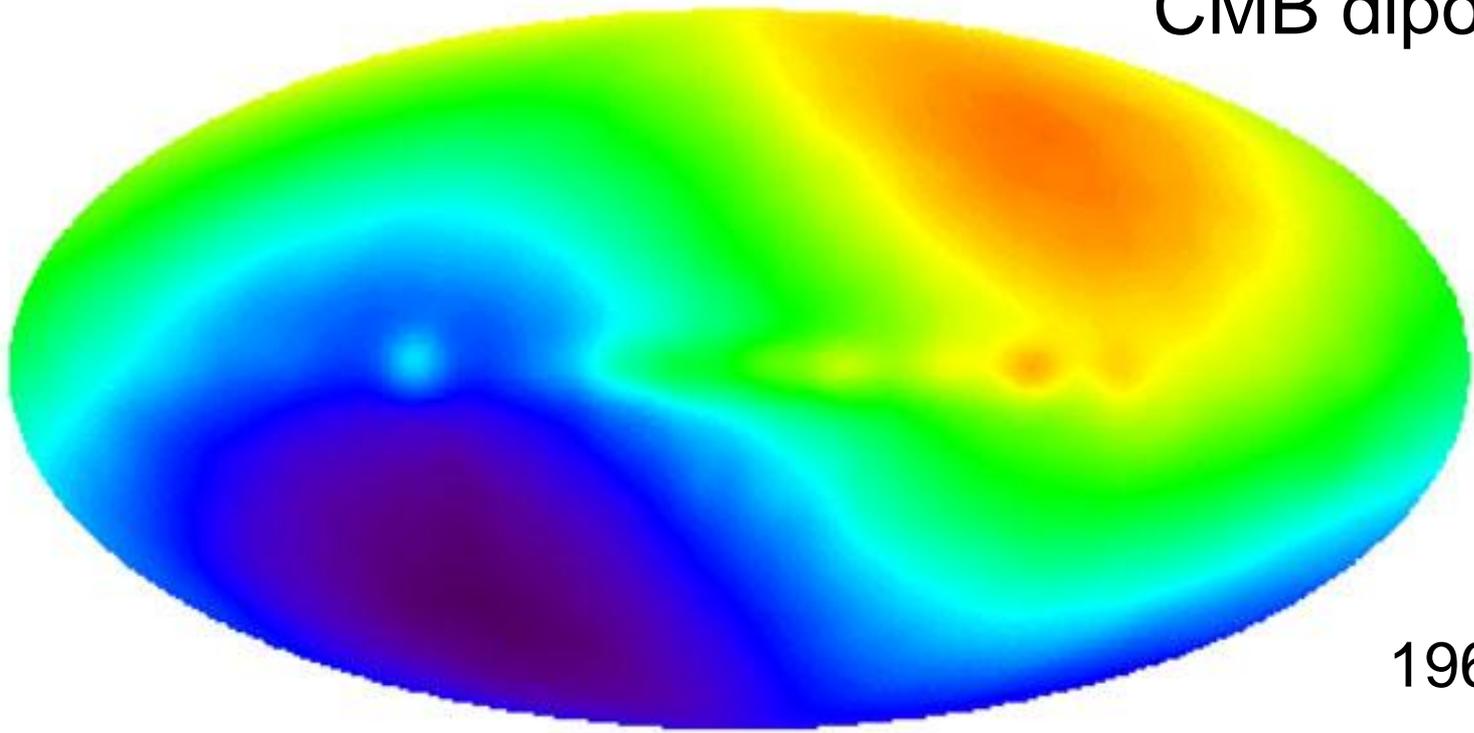


$$\text{COBE-FIRAS } T_0 = 2.725 \pm 0.001 \text{ K}$$

$$n_\gamma(T_0) = \frac{1}{\pi^2} \int_0^\infty \frac{\omega^2 d\omega}{e^{\omega/T_0} - 1} = 410 \text{ cm}^{-3}$$

$$\Omega_\gamma = \frac{\rho_\gamma}{\rho_c} = 2.47 \times 10^{-5} h^{-2}$$

CMB dipole

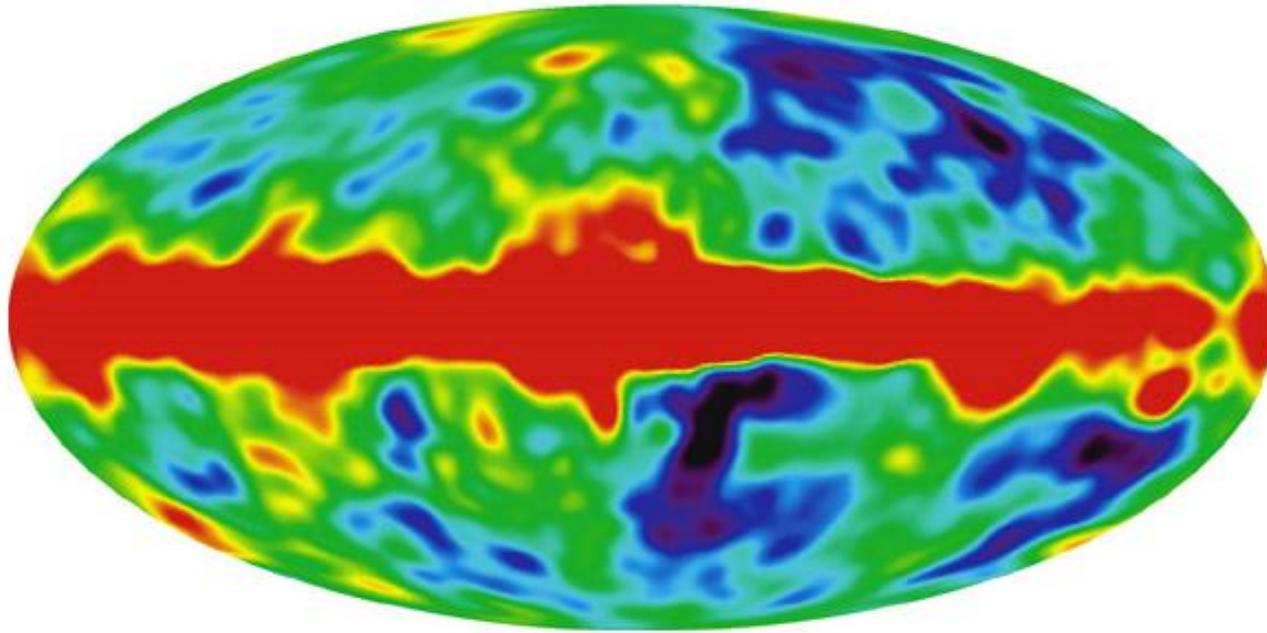


1969

E.K. Conklin
P.S. Henry

$$\frac{\delta T_1}{T_0} = 1.23 \times 10^{-3}$$

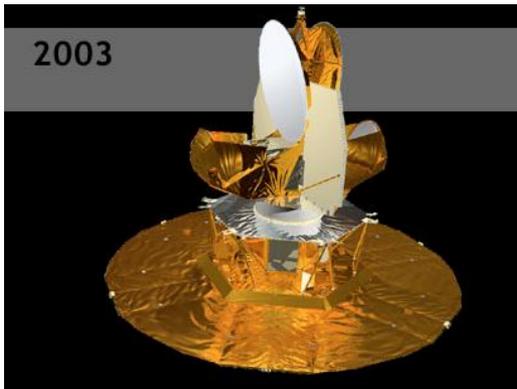
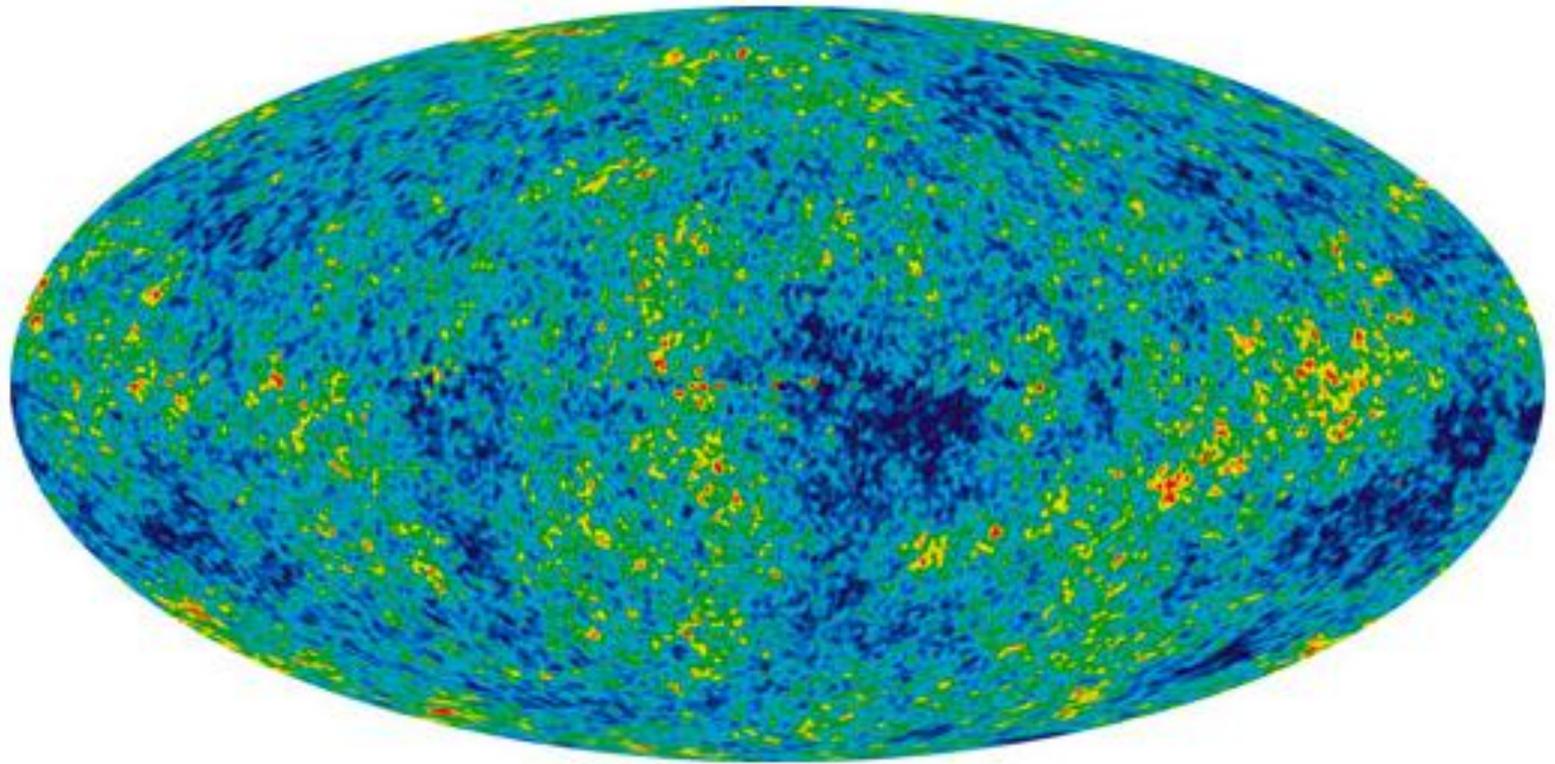
Fluctuations in the cosmic microwave background



COBE DMR

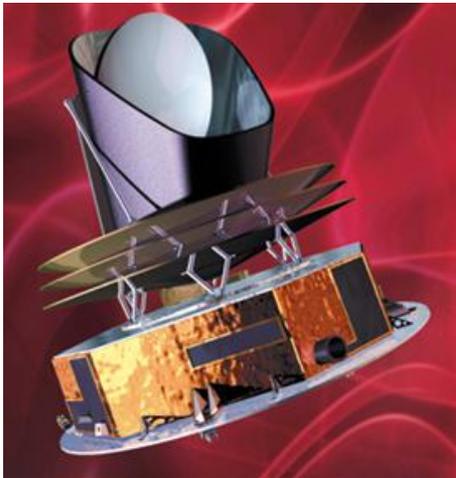
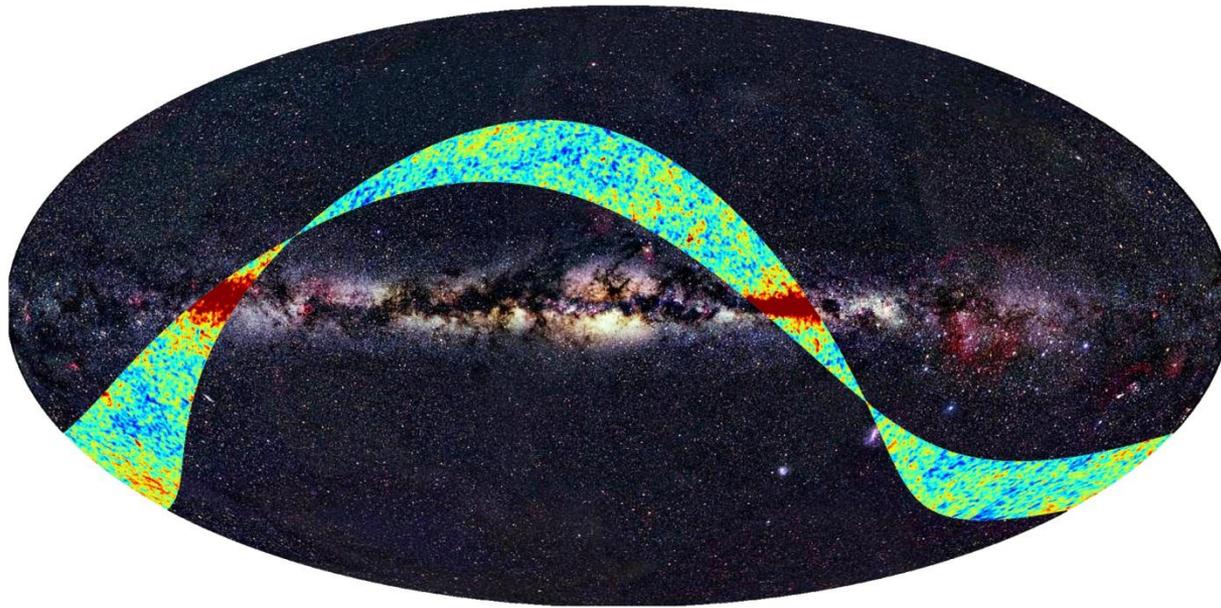
1992

$$\frac{\delta T_2}{T_0} = 1.1 \times 10^{-5}$$



WMAP

2003

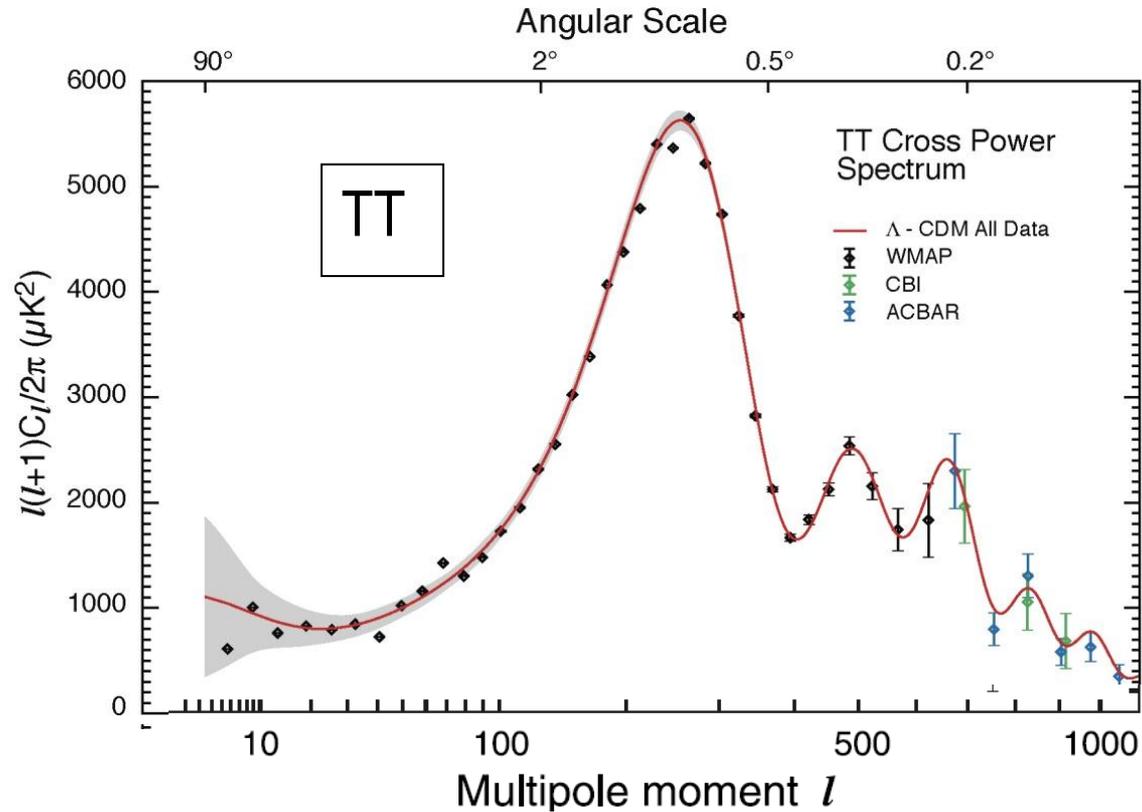


PLANCK

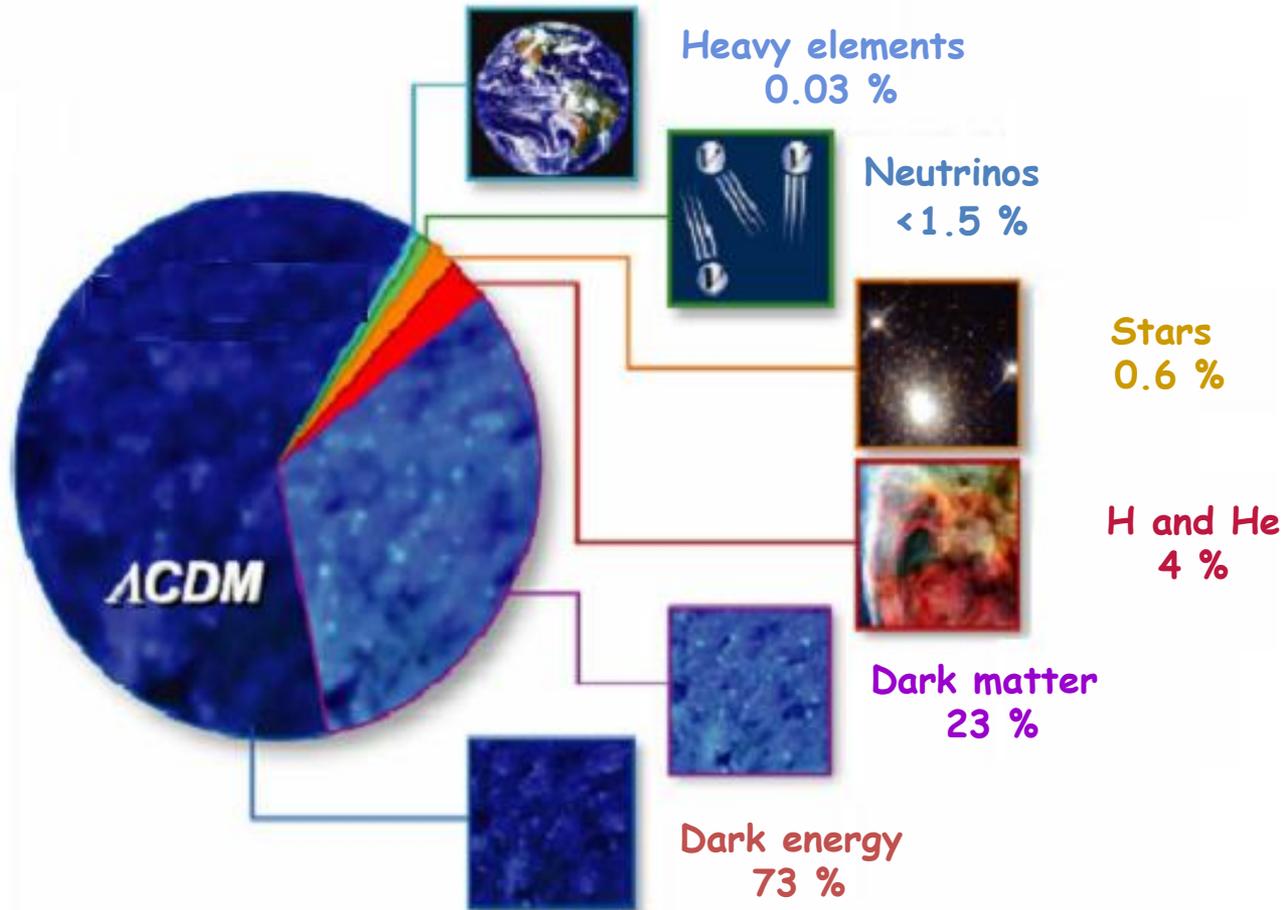
2009

(first data release in 1-2 months)

WMAP temperature power spectrum



Standard Cosmology Λ CDM



Expansion of the universe in Λ CDM

