

Models with extended Higgs sectors at future e^+e^- colliders

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Compact Linear Collider (CLIC)

CLIC will start with an energy of 350/380 GeV. Upgradeable to 1.5 and 3 TeV.

- Deviations from the Standard Model (SM) will be evidence of new physics.
- Expected $\mathcal{O}(1\%)$ precision in fermion, and vector boson couplings with Higgs.
- Accurate measurement of trilinear and quartic Higgs couplings.

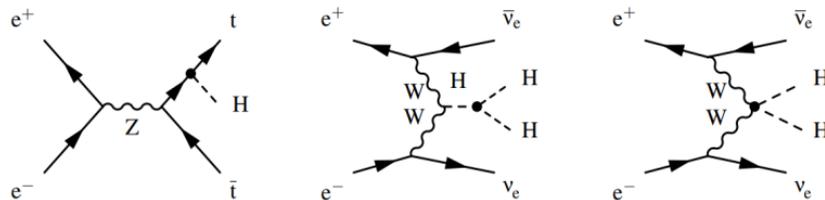


Figure: Main processes containing a top-quark Yukawa coupling $g_{t\bar{t}H}$, trilinear self-coupling g_{HHH} , and g_{WWHH} .

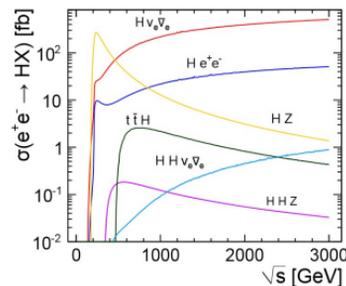
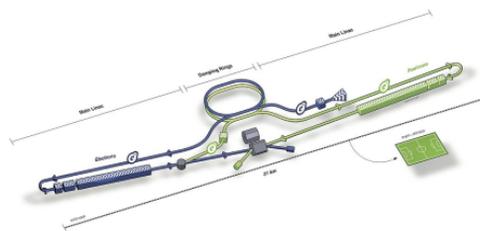


Figure: A general linear collider schematics (left) and the expected main Higgs processes (right).

Scalar extensions

While the Standard Model (SM) predicts several phenomena with an exceptional level of accuracy, for instance:

- The anomalous magnetic moment of the electron, muon.
- Several low energy processes with an incredible level of accuracy. E.g. results from the LEP experiment.

It, nevertheless, fails to account for:

- **Gravity.**
- **Dark Matter.** Several observational evidence: Galaxy rotation curves, Gravitational lensing, Cosmic microwave background, etc.
- **More CP-violation.** CP-violation from weak interactions is not enough to fulfil Sakharov's conditions.

The models under scrutiny are:

- CxSM - The Standard Model with an additional complex singlet.
- (C)2HDM - The (Complex) two Higgs doublet model.
- N2HDM - The next-to-minimal two Higgs doublet model.
- NMSSM - Next-to-minimal Super Symmetric model.

All models have at least three neutral scalars, one to be identified with the discovered Higgs.

First introduced as a scalar dark matter (DM) model.

Let $\mathbb{S} = S(x) + iA(x)$ be a complex $SU(2)_L$ singlet.

We consider the following addition to the of the SM scalar potential

$$V = \frac{m^2}{2} H^\dagger H + \frac{\lambda}{4} (H^\dagger H)^2 + \frac{\delta_2}{2} H^\dagger H |\mathbb{S}|^2 + \frac{b_2}{2} |\mathbb{S}|^2 + \frac{d_2}{4} |\mathbb{S}|^4 + \left(\frac{b_1}{4} \mathbb{S}^2 + a_1 \mathbb{S} + c.c. \right) \quad (1)$$

→ softly-broken $U(1)$ symmetry.

The new field is allowed a vacuum expectation value (VEV)

$$H = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v + h + iG^0) \end{pmatrix} \quad \text{and} \quad \mathbb{S} = \frac{1}{\sqrt{2}} [v_S + s + i(v_A + a)] \quad , \quad (2)$$

This is the broken phase of the CxSM with three physical mixed states h_1, h_2, h_3 , one identified as the 125 GeV Higgs.

(C)2HDM

(Complex) Two Higgs Doublet Model

We consider a particular case of the 2-Higgs-Doublet model (2HDM) and its complex version (C2HDM).

Both obey a discrete \mathbb{Z}_2 symmetry to eliminate tree-level flavour changing neutral currents (FCNC).

$$\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2 \quad (3)$$

The scalar potential reads

$$V = m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + h.c.) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left[\frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + h.c. \right] \quad (4)$$

- **2HDM** - The model is CP-conserving if the parameters and VEVs are real.
- **C2HDM** - The model is CP-violating if the VEVs are real but m_{12}^2 and λ_5 are complex with different phases.

The neutral VEVs of both doublets are set to

$$\sqrt{v_1^2 + v_2^2} \approx 246 \text{ GeV} \quad (5)$$

to keep the gauge bosons mass to their experimental value.

→ **Three mixed neutral scalars and a charged one.**

This model consists of an additional $SU(2)_L$ doublet and real singlet. In relation to the 2HDM, we impose a second \mathbb{Z}_2 symmetry given by

$$\Phi_S \rightarrow -\Phi_S \quad (6)$$

The scalar potential reads

$$\begin{aligned} V = & m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + h.c.) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ & + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2} [(\Phi_1^\dagger \Phi_2)^2 + h.c.] \\ & + \frac{1}{2} m_S^2 \Phi_S^2 + \frac{\lambda_6}{8} \Phi_S^4 + \frac{\lambda_7}{2} (\Phi_1^\dagger \Phi_1) \Phi_S^2 + \frac{\lambda_8}{2} (\Phi_2^\dagger \Phi_2) \Phi_S^2 \end{aligned} \quad (7)$$

After electroweak symmetry breaking (EWSB) we can parametrise the fields as follows

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \rho_1 + i\eta_1) \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \rho_2 + i\eta_2) \end{pmatrix}, \quad \Phi_S = v_S + \rho_S, \quad (8)$$

Additional remarks

For the previous models the the rotation matrix can be parametrised as follows:

$$R = \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix} \quad (9)$$

Where $s_j \equiv \sin \alpha_j$ and $c_j \equiv \cos \alpha_j$. Without loss of generality we have:

$$-\frac{\pi}{2} \leq \alpha_i < \frac{\pi}{2}, \quad (10)$$

The Yukawa interactions can be parametrized as

$$\mathcal{L}_Y = - \sum_{i=1}^3 \frac{m_f}{v} \bar{\psi}_f [c^e(H_{if}) + ic^o(H_{if})\gamma_5] \psi_f H_i \quad (11)$$

	u -type	d -type	leptons
Type I	Φ_2	Φ_2	Φ_2
Type II	Φ_2	Φ_1	Φ_1
Lepton-specific	Φ_2	Φ_2	Φ_1
Flipped	Φ_2	Φ_1	Φ_2

The \mathbb{Z}_2 symmetry preventing FCNCs reduces the possibilities of the doublet-fermions Yukawa interactions.

Any super symmetric model requires the introduction of two doublets. If an additional singlet is present, the μ problem is solved dynamically.

After EWSB, in the CP-conserving NMSSM we have

- Three CP-even and two CP-odd scalars.
- A pair of charged Higgs.

The NMSSM superpotential reads in terms of the hatted superfields

$$\mathcal{W} = \lambda \widehat{S} \widehat{H}_u \widehat{H}_d + \frac{\kappa}{3} \widehat{S}^3 + h_t \widehat{Q}_3 \widehat{H}_u \widehat{t}_R^c - h_b \widehat{Q}_3 \widehat{H}_d \widehat{b}_R^c - h_\tau \widehat{L}_3 \widehat{H}_d \widehat{\tau}_R^c \quad (12)$$

where only the third generation of fermions is present, for simplicity. We expand the fields analogously around their VEVs

$$H_d = \begin{pmatrix} (v_d + h_d + ia_d)/\sqrt{2} \\ h_d^- \end{pmatrix}, H_u = \begin{pmatrix} h_u^+ \\ (v_u + h_u + ia_u)/\sqrt{2} \end{pmatrix}, S = \frac{v_s + h_s + ia_s}{\sqrt{2}} \quad (13)$$

→ **Equivalent to a type II 2HDM.**

Parameter Scan



Parameter space scanner of a general (up to dimension 4) scalar potential. [R. Costa, R. Guedes, M.

Mühlleitner, M. O. P. Sampaio, R. Santos, J. Wittbrodt. JHEP 1703 (2017) 094.]

Provides interfaces with the following HEP codes: HiggsBounds/Signals, SuperISO, SusHi, HDECAY and MicrOMEGAS.

→ Enables easy model implementation through Mathematica notebooks.

→ User analysis can be easily set in premade C++ templates.

→ I am responsible for the maintenance and upgrade of the code. Updated HB5/HS2 interface and implementation of new scalar and vector DM models.

Available at: <https://scanners.hepforge.org/>

Going through a major core upgrade, with faster tools for numerical scans, better user interface, implementation of electric dipole moments (EDM) constraints, among others.

→ One of the physical Higgs is to be identified with the discovered one. Fixing its mass to

$$m_{h_{125}} = 125.09 \text{ GeV} \quad (14)$$

→ Other two can have a mass in the range of]30,1000[GeV, except on $m_{h_{125}} \pm 5$ GeV window. No degeneracy.

Theoretical constraints:

- Boundedness from below.
- Perturbative unitarity.
- Vacuum is global minimum.

Experimental constraints:

- Maximum 2σ deviation for the S,T and U electroweak precision observables.
- Production and decay rates under the 95% C.L. limits from LEP, Tevatron and LHC.
- For the NMSSM we also impose upper bounds on the relic density and direct detection rates for dark matter.

Constraint on the SM-like Higgs

Consider the *worst* scenario: that measurement of the SM-like Higgs boson couplings does not deviate from SM predictions. Given the precision what is the parameter space left for these models?

$$\kappa_{Hii} = \sqrt{\frac{\Gamma_{Hii}^{BSM}}{\Gamma_{Hii}^{SM}}} = 1 \quad (15)$$

Parameter	Relative precision		
	350 GeV 500 fb $^{-1}$	+1.4 TeV +1.5 ab $^{-1}$	+3.0 TeV +2.0 ab $^{-1}$
κ_{HZZ}	0.43%	0.31%	0.23%
κ_{HWW}	1.5%	0.15%	0.11%
κ_{Hbb}	1.7%	0.33%	0.21%
κ_{Hcc}	3.1%	1.1%	0.75%
κ_{Htt}	—	4.0%	4.0%
$\kappa_{H\tau\tau}$	3.4%	1.3%	<1.3%
$\kappa_{H\mu\mu}$	—	14%	5.5%
κ_{Hgg}	3.6%	0.76%	0.54%
$\kappa_{H\gamma\gamma}$	—	5.6%	< 5.6%

Table: Results of the model-dependent global Higgs fit on the expected precisions of the κ_{Hii} . [CLICdp, E. Sicking, Nucl. Part. Phys. Proc. 273-275, 801 (2016)]

→ Benchmark scenarios: **Sc1** (350 GeV), **Sc2** (1.4 TeV) and **Sc3** (3.0 TeV).

In the broken phase, the singlet admixture is given by

$$\Sigma_i^{C \times SM} = (R_{i2})^2 + (R_{i3})^2 \quad (16)$$

The maximum allowed singlet admixture is given by the lower bound on the global signal strength μ which at present is

$$\Sigma_{\max \text{ LHC}}^{C \times SM} \approx 1 - \mu_{\min} \approx 11\% . \quad (17)$$

Let us consider the case where the discovered Higgs is very SM-like when measured at CLIC

$$\kappa_{H_{sm}ii} = 1 \quad (18)$$

Within the most accurate measurements this would lead to

- **CLIC Sc1** - Most accurate $\rightarrow \kappa_{HZZ}$

$$\Sigma_{\max \text{ CLIC@350GeV}}^{C \times SM} \approx 0.85\% , \quad (19)$$

- **CLIC Sc3** - Most accurate $\rightarrow \kappa_{HWW}$

$$\Sigma_{\max \text{ CLIC@3TeV}}^{C \times SM} \approx 0.22\% . \quad (20)$$

Because of CP-violation an additional effect constrains this model: The electric dipole moment (EDM).

→ They affect differently the model depending on which type of Yukawa interactions are considered.

$$\mathcal{L}_Y = - \sum_{i=1}^3 \frac{m_f}{v} \bar{\psi}_f [c^e(H_i f f) + ic^o(H_i f f)\gamma_5] \psi_f H_i, \quad (21)$$

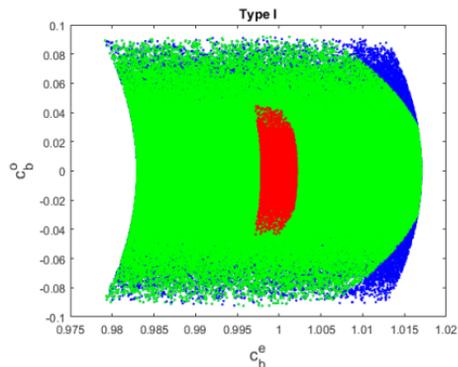
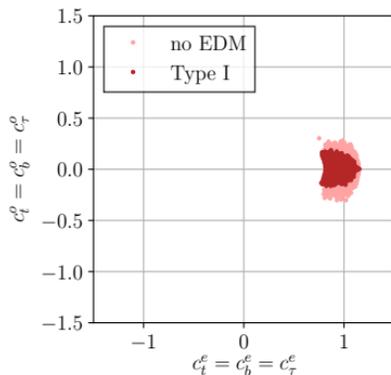
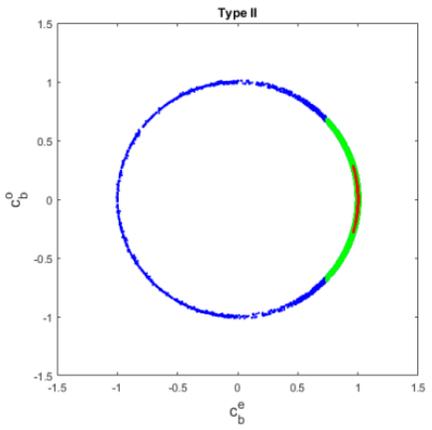
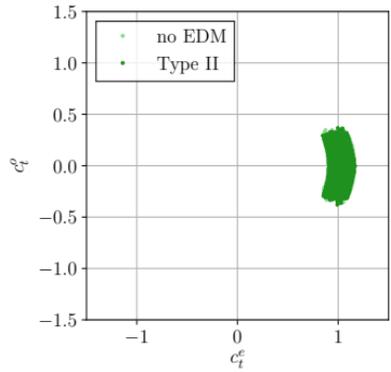
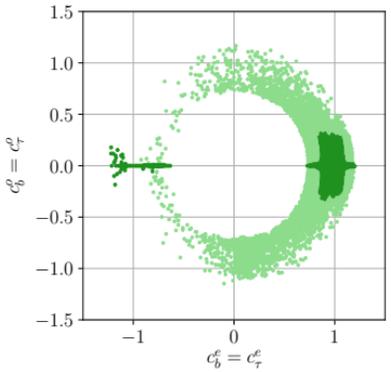
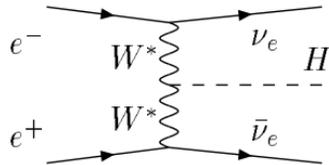
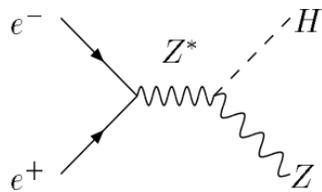


Figure: CP-odd (c_b^o) vs. CP-even (c_b^e) (right) Yukawa couplings for the C2HDM Type I. Current EDM bounds [D. Fontes et al., JHEP 02, 073 (2018)] (left) and CLIC expected bounds (right). The blue points are for Sc1 but without the constraints from κ_{Hgg} and $\kappa_{H\gamma\gamma}$; the green points are for Sc1 including κ_{Hgg} and the red points are for Sc3 including κ_{Hgg} and $\kappa_{H\gamma\gamma}$.

Type II



Main production modes at lower energies:



WW-fusion becomes main production with higher energies.

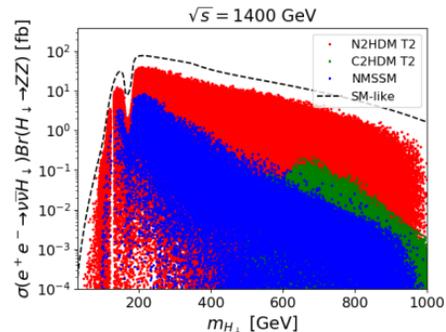
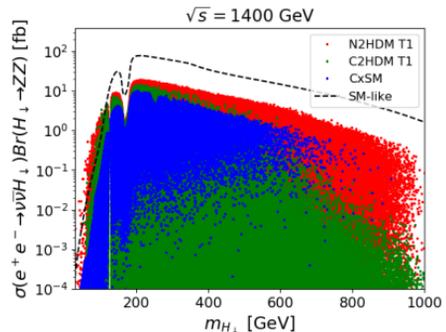
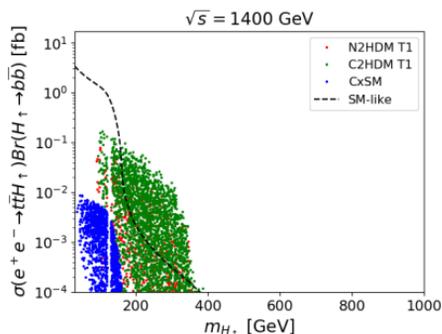
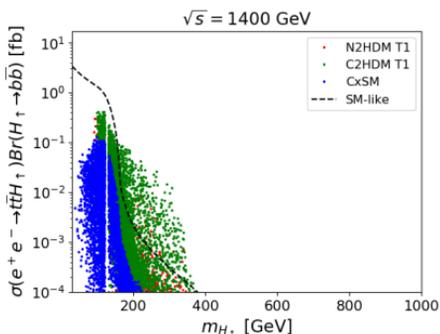
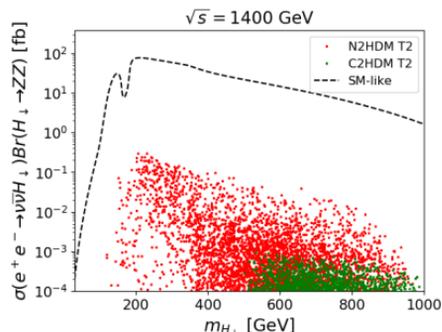
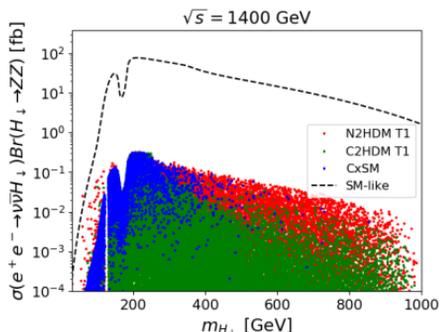


Figure: Total rate for $e^+e^- \rightarrow \nu\bar{\nu}H_{\downarrow} \rightarrow \nu\bar{\nu}ZZ$ as a function of the lighter Higgs boson mass for $\sqrt{s} = 1.4$ TeV.

→ Effect of Sc1 on the signal rates:



- The CxSM is the most constrained due to the fewer degrees of freedom.
- Associated production rivals the other production modes when considering Sc1.

Published: Phys. Rev. D 99, 055013 (2019).

We have studied several BSM scalar extensions: CxSM, (C)2HDM, N2HDM (Type I and II) and the NMSSM at the future Compact Linear Collider, using the expected benchmarks for energies of 350, 1400, 3000 GeV.

- These benchmarks were used to constrain the 125 GeV Higgs to be very SM-like, and see the possible deviations from CP-even and doublet-like structure still available.
- We show that CLIC results constrain further the singlet admixture and CP-odd component.

On the second part we studied the possibility of finding and studying additional Higgs bosons at CLIC through Higgstrahlung, WW-fusion and associated production.

- Checking if the models can be disentangled with the discovery of a new particle in the first stage.
- Verified the remaining parameter space, in case of no new physics in the first run.
- NMSSM was gone, maybe new particle to be discovered?

Thank you!



Figure: Left to right: P. Ferreira, R. Santos, M. Mühlleitner, J. Wittbrodt, D. Azevedo.

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Duarte
Azevedo

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Backup

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CxSM

The VEVs v_A and v_S are varied in the range

$$1 \text{ GeV} \leq v_A, v_S < 1.5 \text{ TeV} . \quad (22)$$

The mixing angles $\alpha_{1,2,3}$ vary within the limits

$$-\frac{\pi}{2} \leq \alpha_{1,2,3} < \frac{\pi}{2} . \quad (23)$$

(C)2HDM

The angles vary in the range

$$0.5 \leq t_\beta \leq 35 \quad -\frac{\pi}{2} \leq \alpha_{1,2,3} < \frac{\pi}{2} . \quad (24)$$

The value of $\text{Re}(m_{12}^2)$ is in the range

$$0 \text{ GeV}^2 \leq \text{Re}(m_{12}^2) < 500000 \text{ GeV}^2 . \quad (25)$$

(...) The charged Higgs mass is chosen in the range

$$\begin{aligned} 80 \text{ GeV} &\leq m_{H^\pm} < 1 \text{ TeV} \text{ (Type I)} \\ 580 \text{ GeV} &\leq m_{H^\pm} < 1 \text{ TeV} \text{ (Type II)} \end{aligned} \quad (26)$$

One of the H_i is restricted to

$$\begin{aligned} 30 \text{ GeV} &\leq m_{H_i} < 1 \text{ TeV} \text{ (Type I)} \\ 500 \text{ GeV} &\leq m_{H_i} < 1 \text{ TeV} \text{ (Type II)} \end{aligned} \quad (27)$$

N2HDM

$$\begin{aligned} -\frac{\pi}{2} &\leq \alpha_{1,2,3} < \frac{\pi}{2} & 0.25 &\leq t_\beta \leq 35 \\ 0 \text{ GeV}^2 &\leq \text{Re}(m_{12}^2) < 500000 \text{ GeV}^2 & 1 \text{ GeV} &\leq v_S \leq 1.5 \text{ TeV} , \\ 30 \text{ GeV} &\leq m_{H_i \neq h_{125}}, m_A \leq 1 \text{ TeV} & & \\ 80 \text{ GeV} &\leq m_{H^\pm} < 1 \text{ TeV} \text{ (type I)} & 580 \text{ GeV} &\leq m_{H^\pm} < 1 \text{ TeV} \text{ (type II)} \end{aligned} \quad (28)$$

Parameters Range 3/3

NMSSM

For the NMSSM we used `NMSSMTools` for computation of the particle spectrum and its higher order corrections. It also enables a cross-check with:

- Low energy observables.
- HiggsBounds.
- MicrOMEGAs.

Signal strengths are computed from the SM processes multiplied by the effective couplings calculated with `NMSSMTools`.

Parameter range:

	t_β	λ	κ	M_1	M_2	M_3	A_t	A_b	A_τ	$m_{\tilde{Q}_3}$	$m_{\tilde{L}_3}$	A_λ	A_κ	μ_{eff}
	in TeV													
min	1	0	-0.7	0.1	0.2	1.3	-6	-6	-3	0.6	0.6	-2	-2	-5
max	50	0.7	0.7	1	2	7	6	6	3	4	4	2	2	5

Table: Input parameters for the NMSSM scan.

Perturbative unitarity is ensured by enforcing the rough constraint

$$\lambda^2 + \kappa^2 < 0.7^2 \quad (29)$$