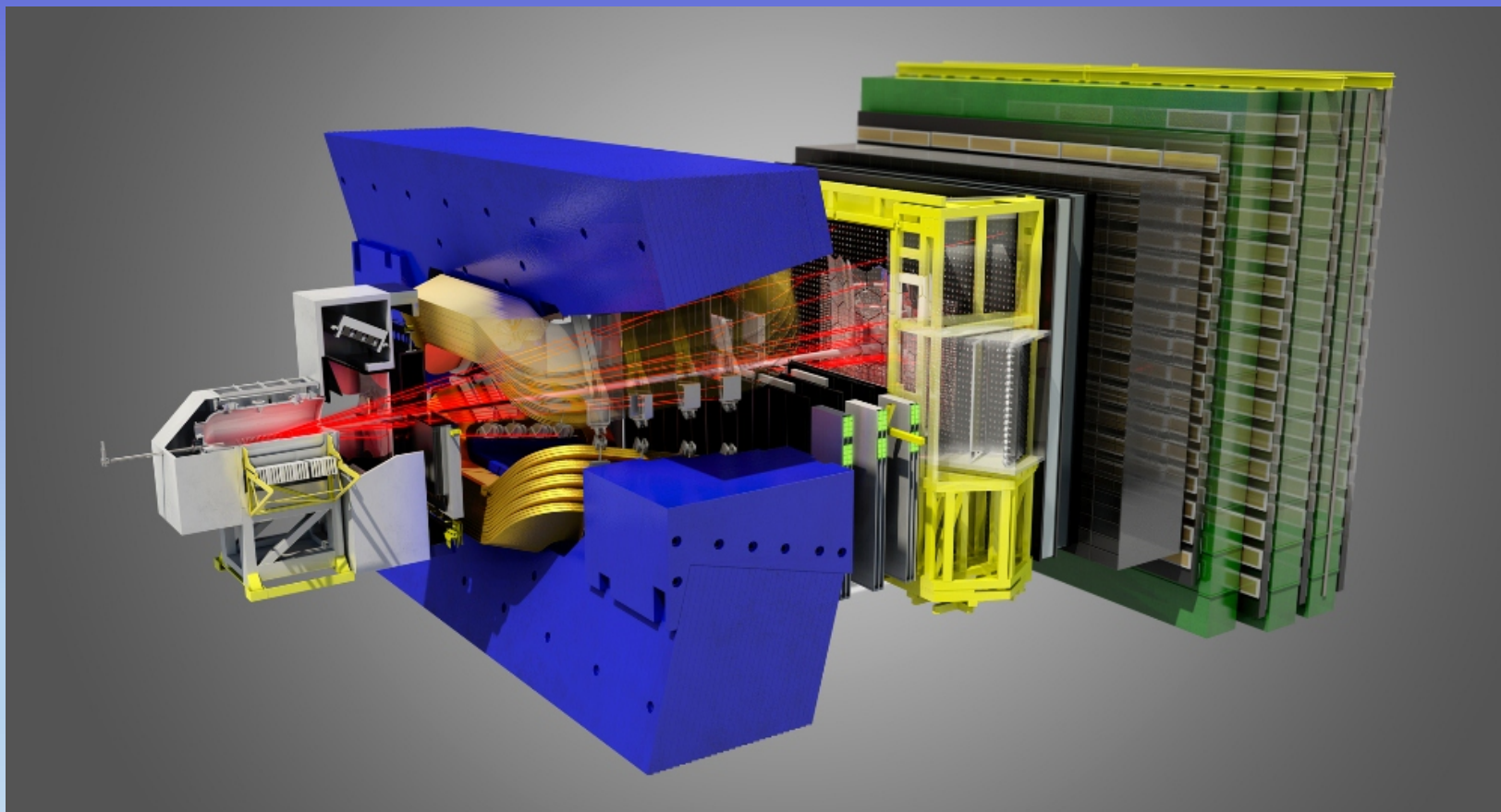


Experimental Flavour Physics



Outline

- Introduction
- The LHCb experiment
- The CKM matrix
- B mixing and CP violation
- Rare decays of B mesons
- Future plans

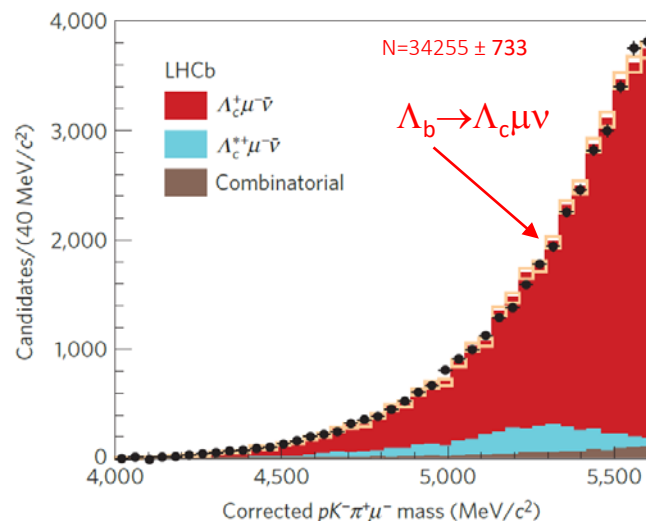
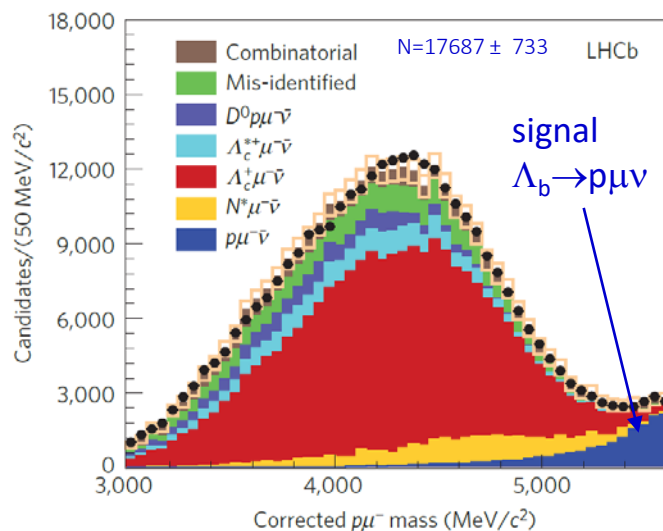
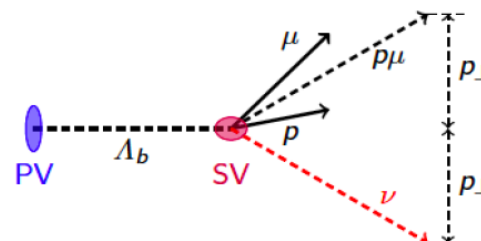
The CKM matrix

At LHCb very challenging due to the missing neutrino:

Using semileptonic decays of b-baryons:

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow p \mu^- \bar{\nu}_\mu)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \bar{\nu}_\mu)} = \frac{|V_{ub}|^2}{|V_{cb}|^2} \times \text{Ratio of form factors} \quad \leftarrow (5\% \text{ accuracy from LQCD})$$

- Use information from displaced vertex
- Select high q^2 region (theory more precise)
- Corrected mass: $m_{\text{corr}} = \sqrt{m_{h\mu}^2 + p_\perp^2} + p_\perp$



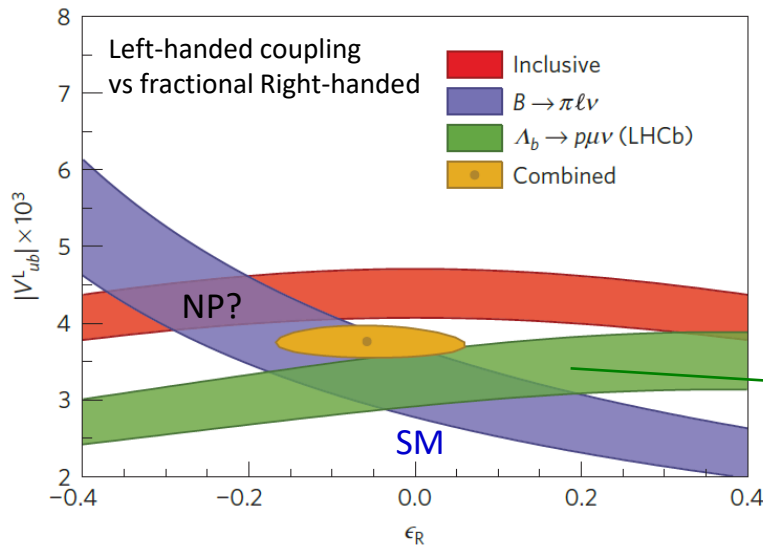
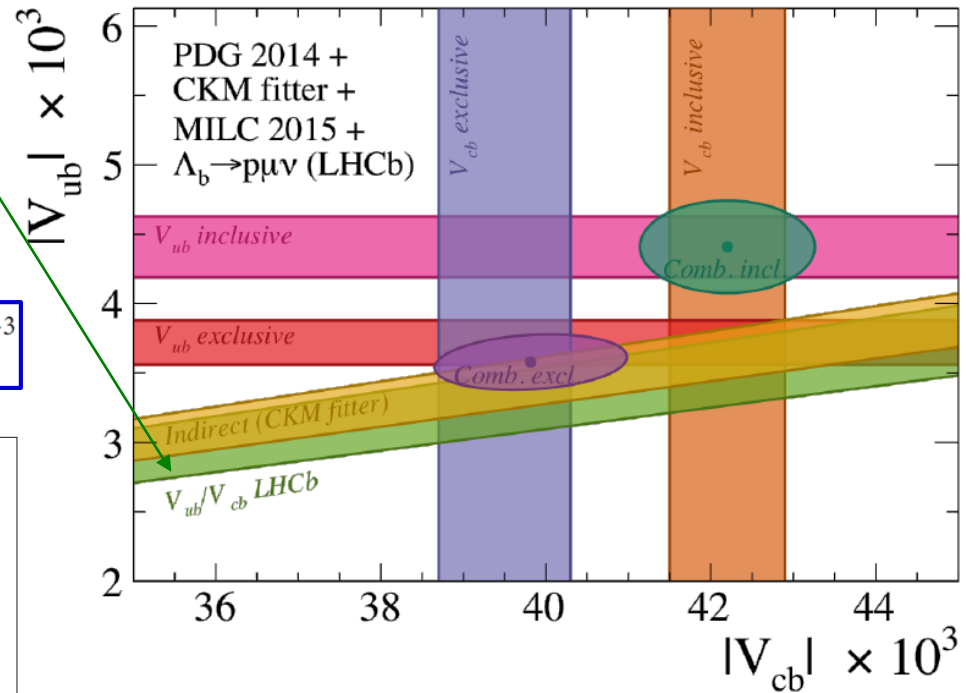
The CKM matrix

[Nature Physics 10 (2015) 1038]

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004 \pm 0.004$$

Using the world average from exclusive V_{cb} :

$$|V_{ub}| = (3.27 \pm 0.15 \pm 0.16 \pm 0.06) \times 10^{-3}$$



Disfavours New Physics models with Right-handed currents

B mixing and CP violation

Mixing of neutral B mesons governed by

Mass eigenstates:

$$|B_{L,H}\rangle = p |B^0\rangle \pm q |\overline{B}^0\rangle$$

$$i\frac{\partial}{\partial t}\begin{pmatrix} a \\ b \end{pmatrix} = H \begin{pmatrix} a \\ b \end{pmatrix} = \begin{pmatrix} M_{11} - \frac{i}{2}\Gamma_{11} & M_{12} - \frac{i}{2}\Gamma_{12} \\ M_{12}^* - \frac{i}{2}\Gamma_{12}^* & M_{22} - \frac{i}{2}\Gamma_{22} \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix}$$

p and q represent the amount of state mixing

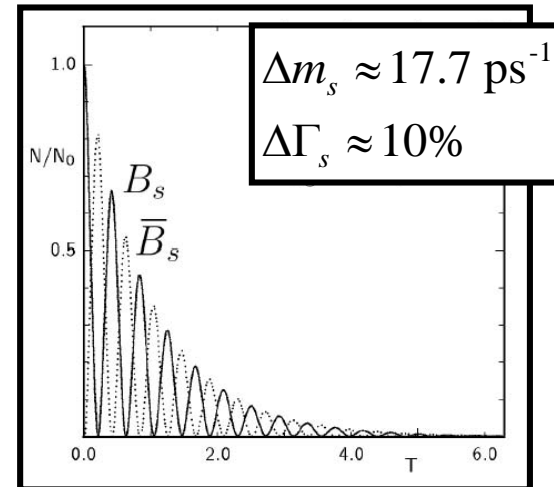
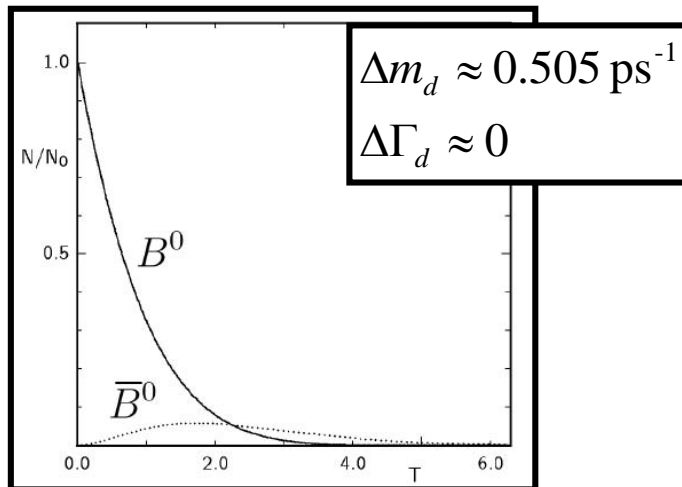
$$|p|^2 + |q|^2 = 1$$

$$|q/p| = 1$$

$$\frac{q}{p} = \sqrt{\frac{M_{12}^* - \frac{i}{2}\Gamma_{12}^*}{M_{12} - \frac{i}{2}\Gamma_{12}}}$$

$$\Delta m = m_H - m_L = 2|M_{12}|$$

$$\Delta\Gamma = \Gamma_L - \Gamma_H = 2|\Gamma_{12}|$$

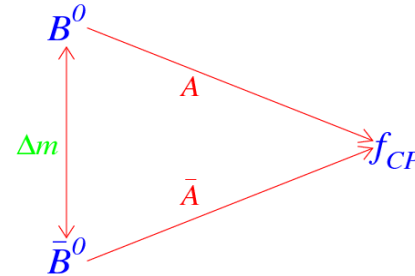


B mixing and CP violation

Decay amplitudes of flavour states decaying to the same final state f

$$A_f = \langle f | H | B^0 \rangle \quad \overline{A}_f = \langle f | H | \overline{B}^0 \rangle$$

One can define
$$\lambda_f = \frac{q}{p} \frac{\overline{A}_f}{A_f}$$



$$\tau \equiv 1/\Gamma$$

$$x \equiv \Delta m/\Gamma$$

$$y \equiv \Delta\Gamma/2\Gamma$$

Time dependence of decay rate for initially pure flavour states:

$$\Gamma_f \equiv \left| \langle f | H | B^0(t) \rangle \right|^2 = \frac{1 + |\lambda_f|^2}{2} |A_f|^2 e^{-t/\tau} \left[\cosh y t / \tau + A_{\Delta f} \sinh y t / \tau + C_f \cos x t / \tau - S_f \sin x t / \tau \right]$$

$$\overline{\Gamma}_f \equiv \left| \langle f | H | \overline{B}^0(t) \rangle \right|^2 = \frac{1 + |\lambda_f|^2}{2} \left| \frac{p}{q} A_f \right|^2 e^{-t/\tau} \left[\cosh y t / \tau + A_{\Delta f} \sinh y t / \tau - C_f \cos x t / \tau + S_f \sin x t / \tau \right]$$

$$S_f \equiv \frac{2 \operatorname{Im} \lambda_f}{1 + |\lambda_f|^2}$$

$$C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

$$A_{\Delta f}^2 + S_f^2 + C_f^2 = 1$$

B mixing and CP violation

CP Violation $\rightarrow \Gamma_f \neq \bar{\Gamma}_f$

Three types:

• **CPV in Decay:** $B^0 \rightarrow f \neq \bar{B}^0 \rightarrow \bar{f}$

$$\left| \frac{\bar{A}_f}{A_f} \right| \neq 1$$

• **CPV in Mixing:** $B^0 \rightarrow \bar{B}^0 \neq \bar{B}^0 \rightarrow B^0$

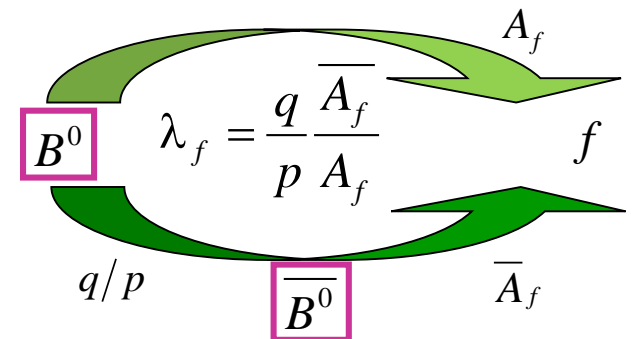
$$\left| \frac{q}{p} \right| \neq 1$$

$$\text{Im} \{ \Gamma_{12}^* M_{12} \} \neq 0$$

• **CPV in Interference between mixing and decay:**

$$|\lambda_f| = 1, \quad \text{Im} \{ \lambda_f \} \neq 0$$

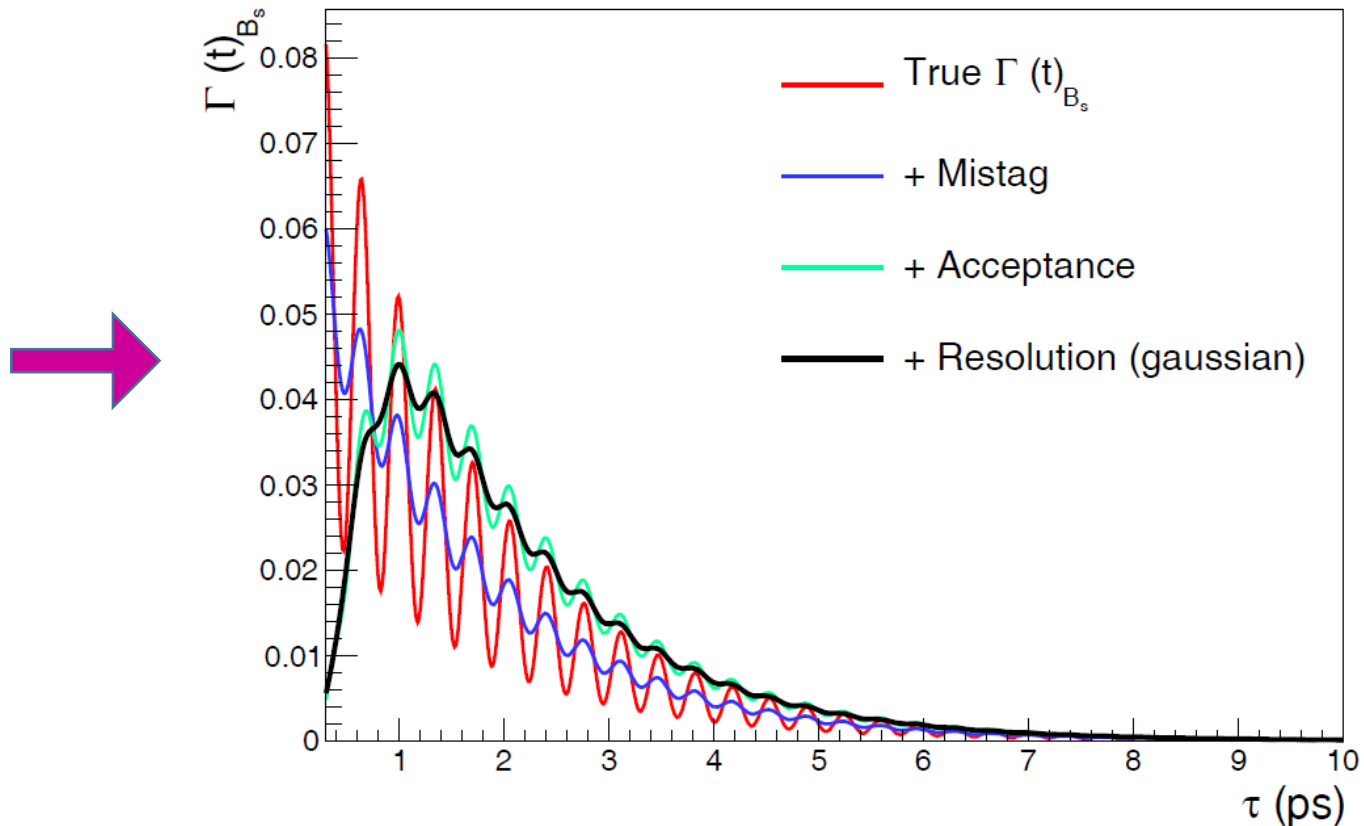
$$A_f^{CP}(t) = \frac{\Gamma_f(t) - \bar{\Gamma}_f(t)}{\Gamma_f(t) + \bar{\Gamma}_f(t)} = \frac{-C_f \cos(\Delta m t) + S_f \sin(\Delta m t)}{\cosh(\Delta \Gamma t/2) + A_{\Delta f} \sinh(\Delta \Gamma t/2)}$$



B mixing and CP violation

- Experimental effects:

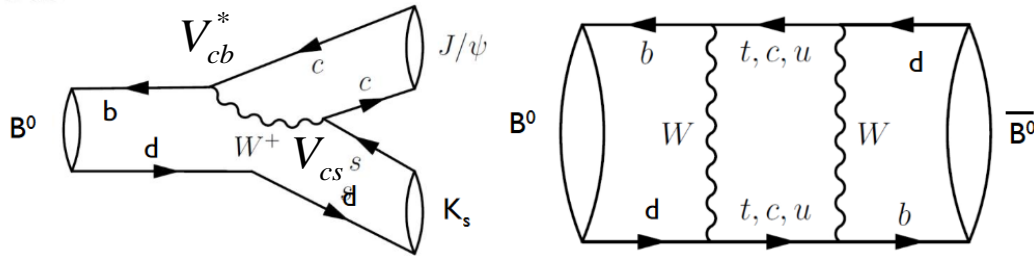
Dilution of the oscillation (lost of sensitivity of the oscillation parameters) due to reconstruction effects



B mixing and CP violation

Measuring the β angle of the CKM triangle

Golden channel: $B^0 \rightarrow J/\psi K^0$

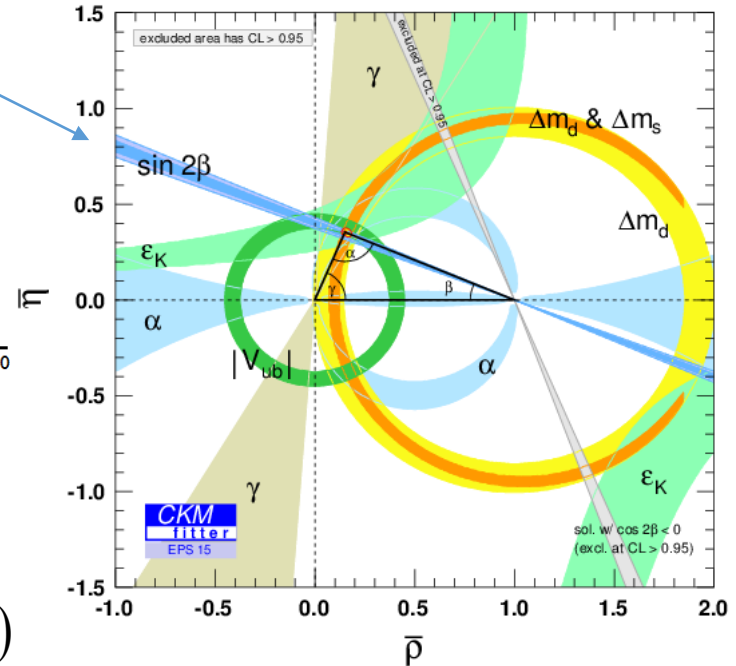


$$A_f^{CP}(t) = \frac{\Gamma_f(t) - \bar{\Gamma}_f(t)}{\Gamma_f(t) + \bar{\Gamma}_f(t)} = \frac{-C_f \cos(\Delta m t) + S_f \sin(\Delta m t)}{\cosh(\Delta \Gamma t/2) + A_{\Delta f} \sinh(\Delta \Gamma t/2)}$$

$$\sim -C_f \cos(\Delta m t) + S_f \sin(\Delta m t)$$

$C_f \sim 0$ in the SM

$$A_f^{CP}(t) \sim \sin 2\beta \sin(\Delta m t)$$



$$S_f \equiv \frac{2 \operatorname{Im} \lambda_f}{1 + |\lambda_f|^2}$$

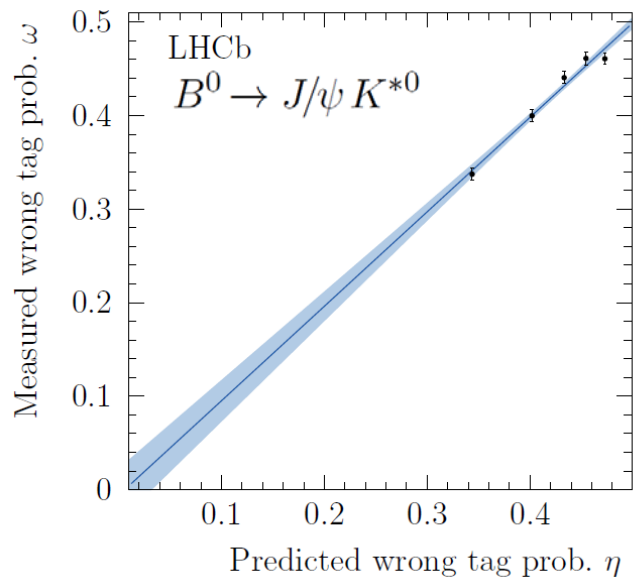
$$\operatorname{Im}\{\lambda_f\} = \operatorname{Im}\{-e^{-2i\beta}\} = \sin 2\beta$$

B mixing and CP violation

Count number of tagged signal events reconstructed as function of time

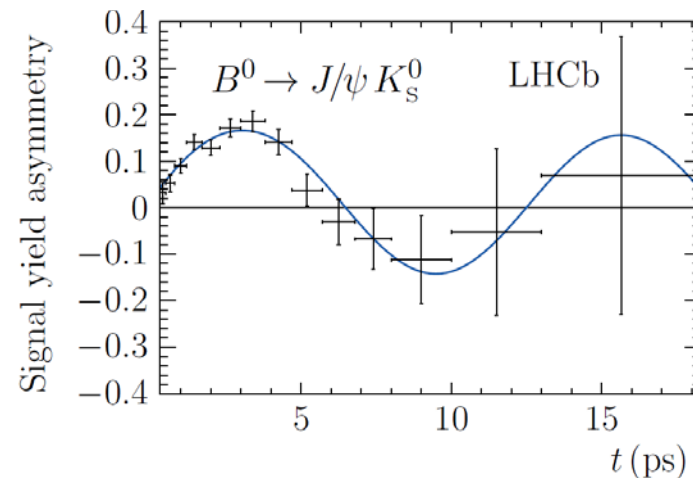
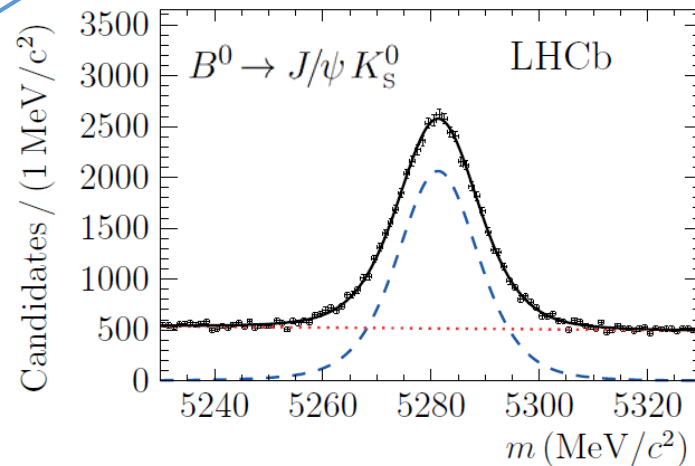
$$A_{CP}(t) = \frac{N(B_{tag} = B^0) - N(B_{tag} = \bar{B}^0)}{N(B_{tag} = B^0) + N(B_{tag} = \bar{B}^0)} \approx \pm \{(1 - 2\omega) \times \sin 2\beta \times \sin(\Delta m \Delta t)\} \otimes R(\Delta t)$$

Flavour mistag calibrated
using a control sample
flavour specific ($K^{*0} \rightarrow K^- \pi^+$)



$$\omega = (35.62 \pm 0.12) \%$$

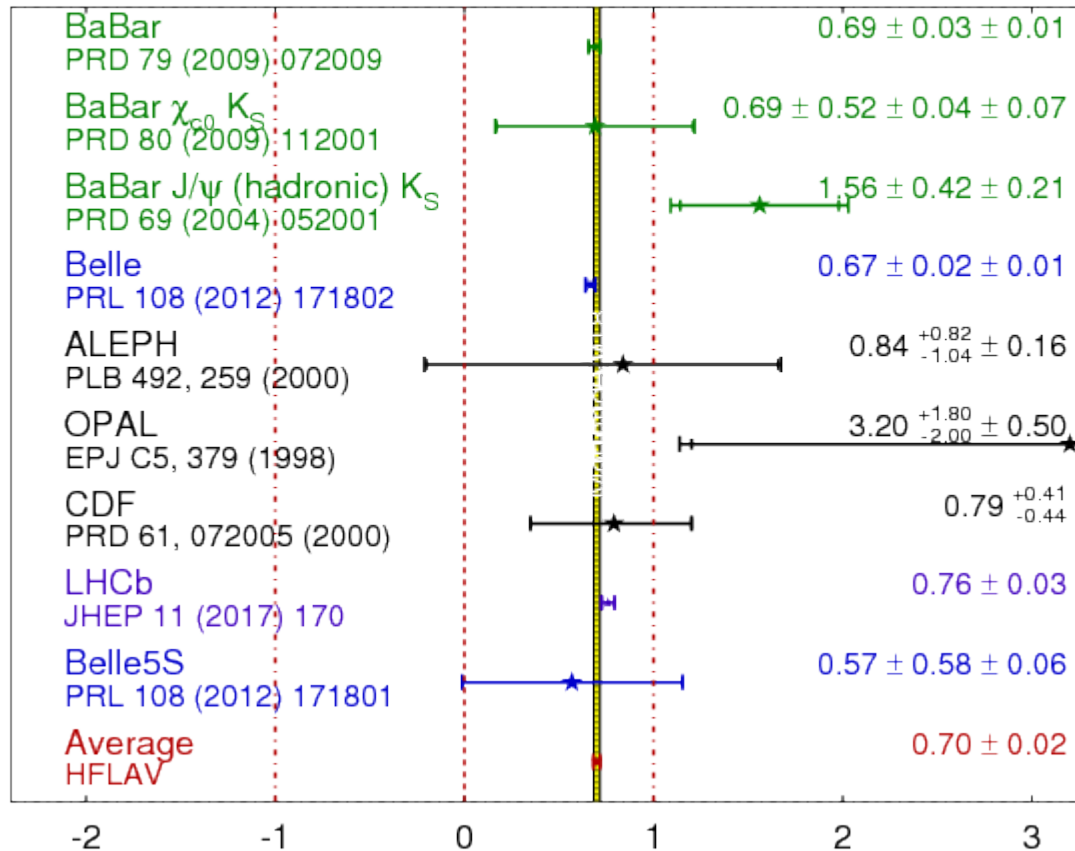
$$\epsilon_{tag} = (36.54 \pm 0.14) \%$$



B mixing and CP violation

$$\sin(2\beta) \equiv \sin(2\phi_1)$$

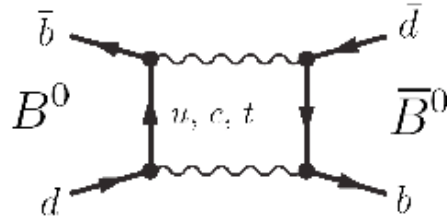
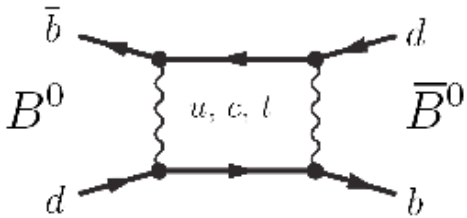
HFLAV
Moriond 2018
PRELIMINARY



B mixing and CP violation

Measuring the other side of the CKM triangle

- Through the mass difference Δm_d , Δm_s in the box diagrams:

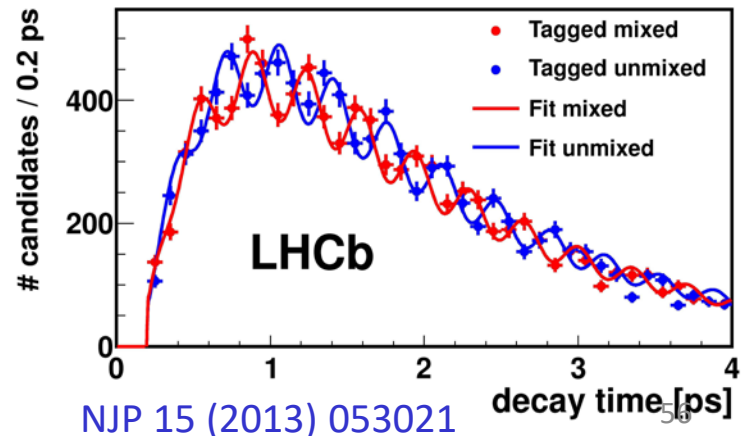
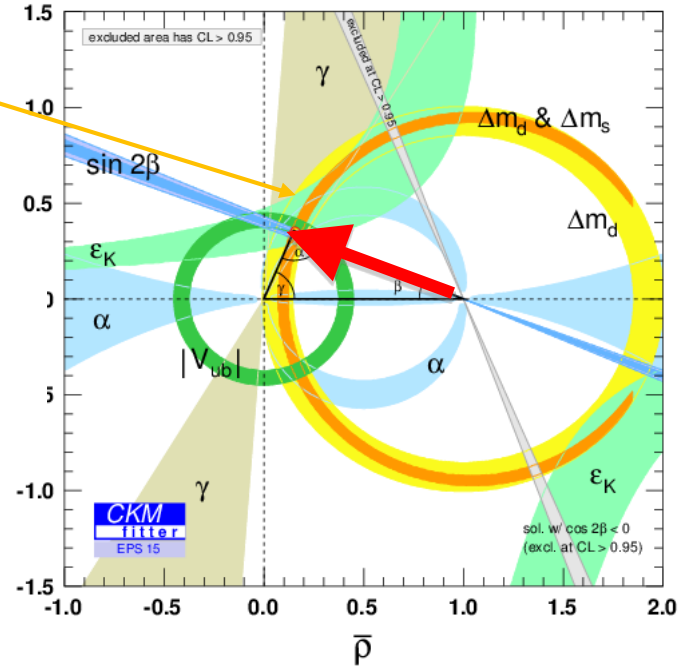


The time-dependent asymmetry $A(t)$ of $B_{d,s}$ events that changed flavour (mixed) or not (unmixed) is:

$$A_{mix}(t) \frac{N^{unmix}(t) - N^{mix}(t)}{N^{unmix}(t) + N^{mix}(t)} = \cos \Delta mt$$

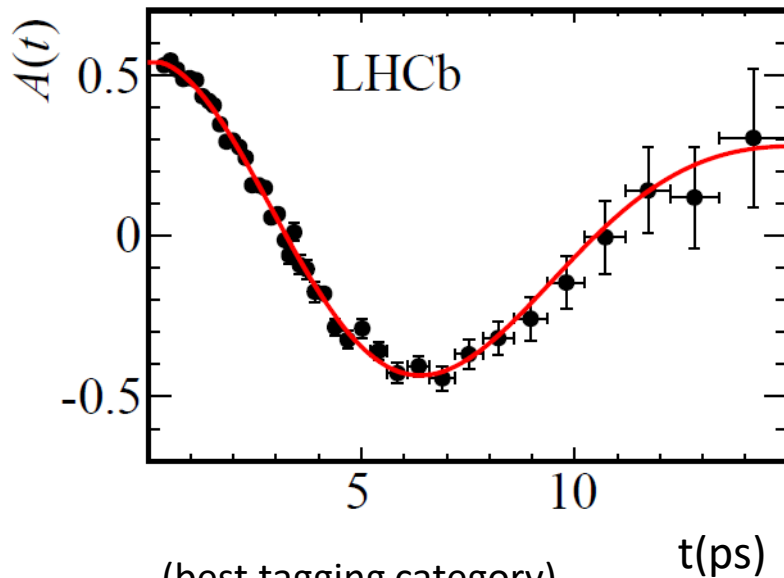
with experimental effects:

$$= \{(1 - 2\omega) \times \cos \Delta m \Delta t\} \otimes R(\Delta t)$$



B mixing and CP violation

Measuring the other side of the CKM triangle

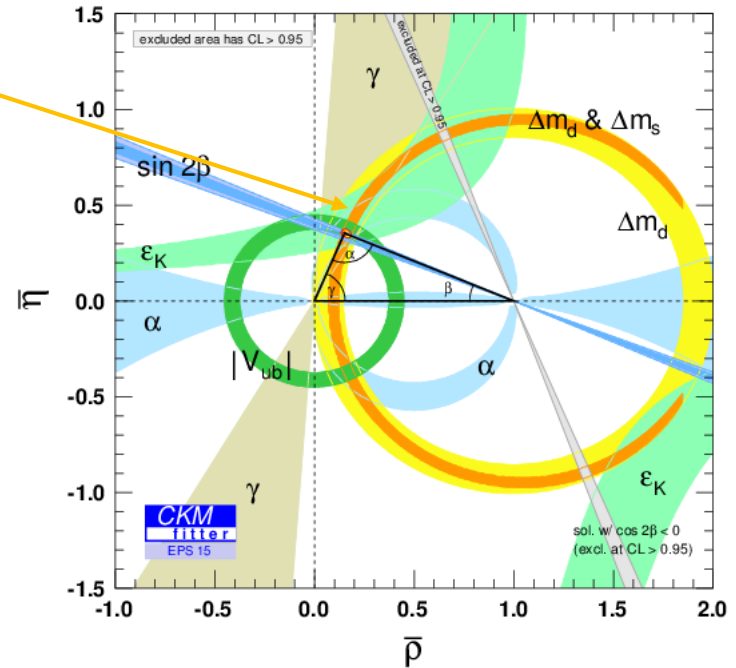


(best tagging category)

[EPJ C (2016) 76]

$$\Delta m_d = (0.5050 \pm 0.0021 \pm 0.0010) \text{ ps}^{-1}$$

$$\Delta m_s = (17.768 \pm 0.023 \pm 0.006) \text{ ps}^{-1}$$



$$\frac{\Delta m_d}{\Delta m_s} = \frac{m_{B_d} f_{B_d}^2 \hat{B}_{B_d} |V_{td}|^2}{m_{B_s} f_{B_s}^2 \hat{B}_{B_s} |V_{ts}|^2}$$

error from theory

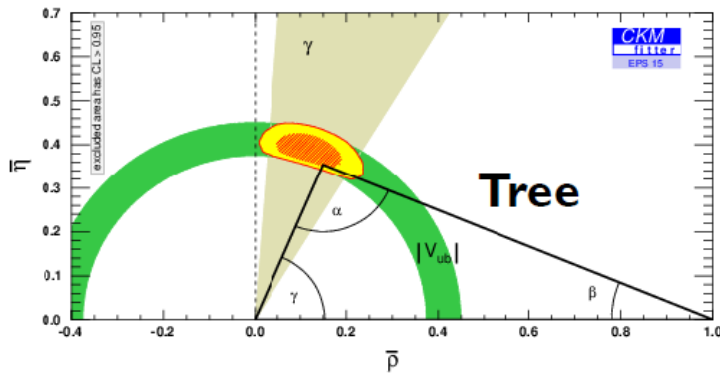
$$|V_{td}/V_{ts}| = 0.216 \pm 0.001 \pm 0.011$$

Q : Could you infer the top mass from the measured Δm_d ?

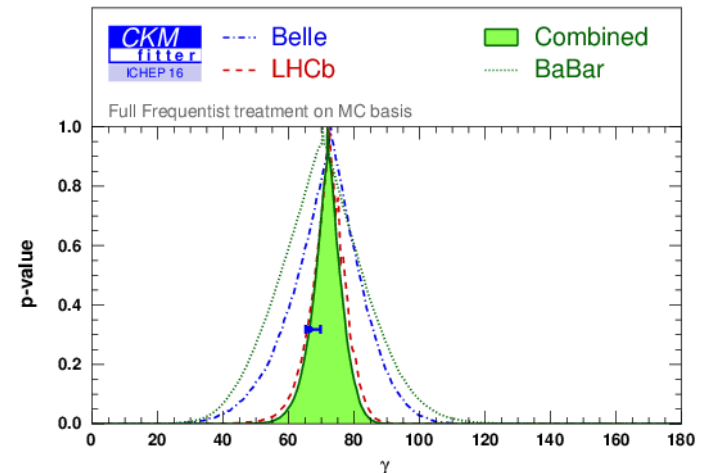
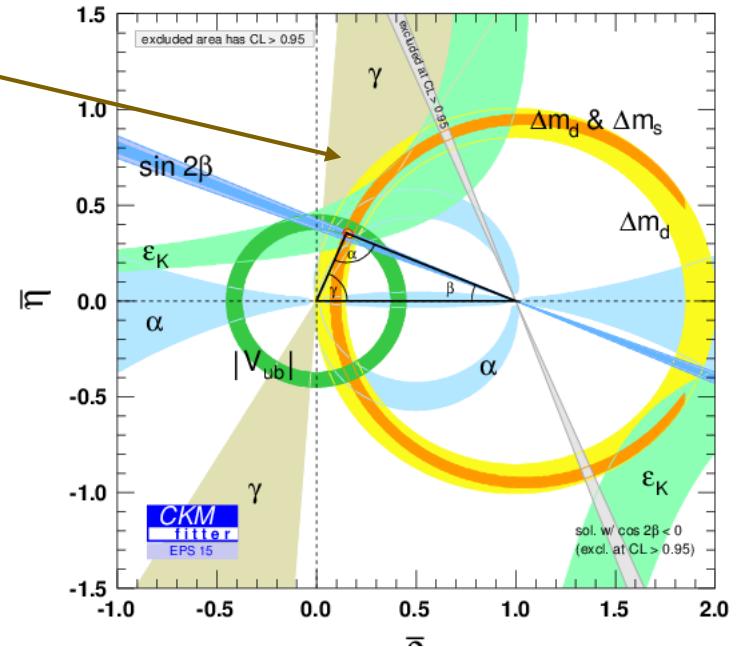
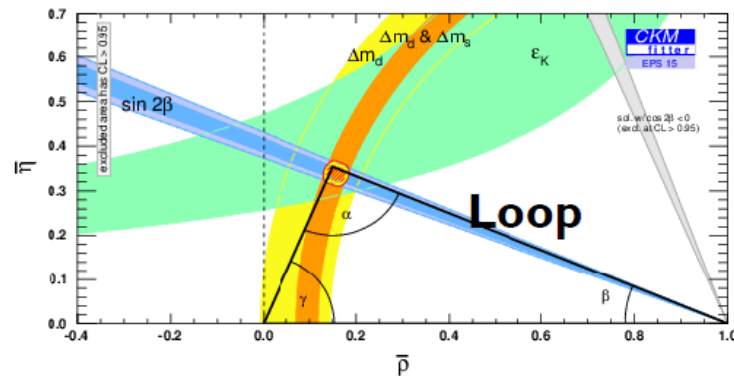
B mixing and CP violation

Measuring the γ angle of the CKM triangle

Key to determine the apex from tree level processes, with V_{ub} is the “reference clock”



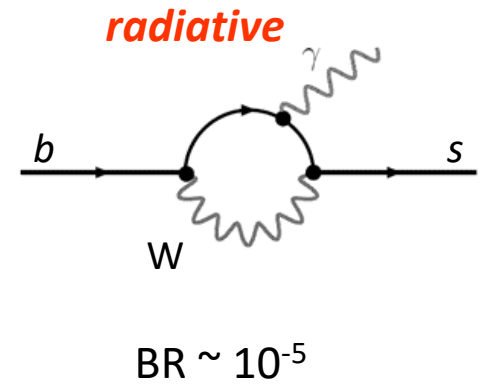
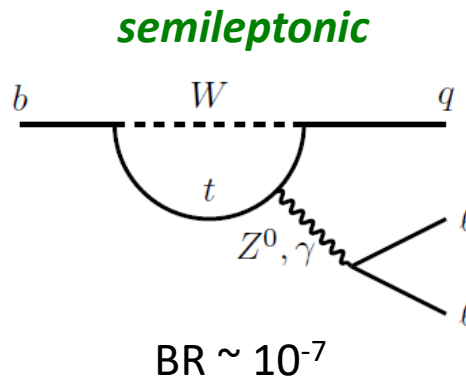
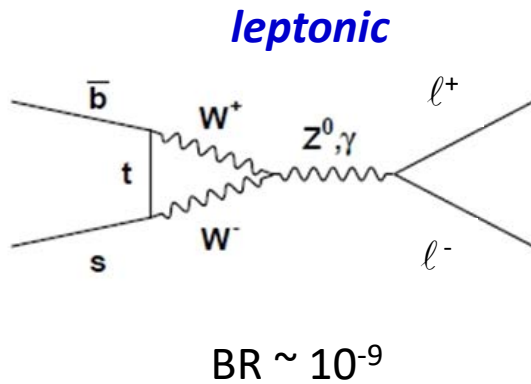
To be compared with constraints from loop processes:



$$\gamma = 72.2^{+5.3}_{-5.8}$$

Rare decays

- Processes very suppressed, go through loop diagrams: branching fractions (BR) $10^{-5} - 10^{-10}$
- Highly sensitive to New Physics: if one finds more events than expected \rightarrow new particles



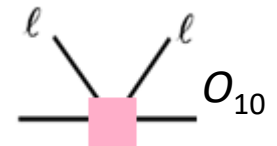
Experimentally \rightarrow leptons/photons with high transverse momenta

Theoretically \rightarrow observables can be calculated in terms of Wilson coefficients

$$\text{Ex: } \Gamma(B_s^0 \rightarrow \mu^+ \mu^-) \sim \frac{G_F^2 \alpha^2}{64 \pi^3} m_{B_s}^2 f_{B_s}^2 |V_{tb} V_{ts}|^2 |2m_\mu C_{10}|^2$$



Hadronic uncertainties in decay constants or form factors



Rare decays: leptonic

One of the most relevant channels:

$$B_s \rightarrow \mu^+ \mu^-$$

→ FCNC + helicity suppressed → **Very Rare decay**:

→ Standard Model prediction:

[PRL 112 101801 (2014)]

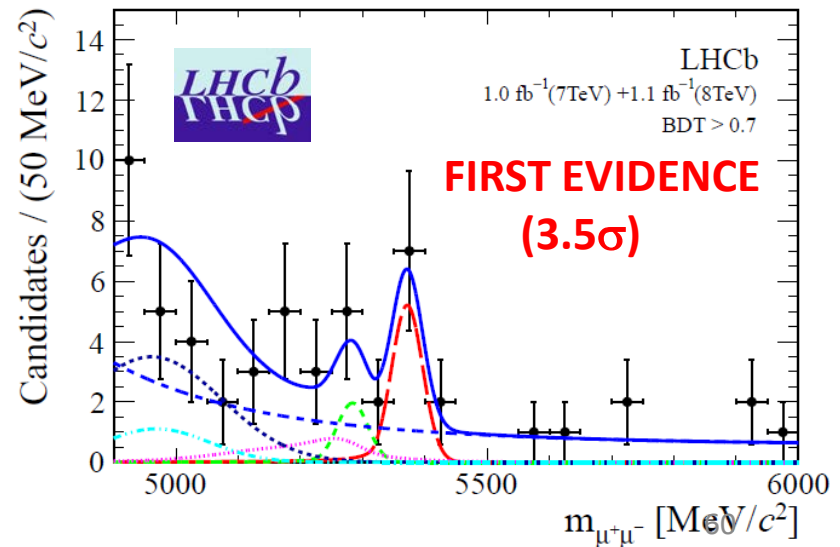
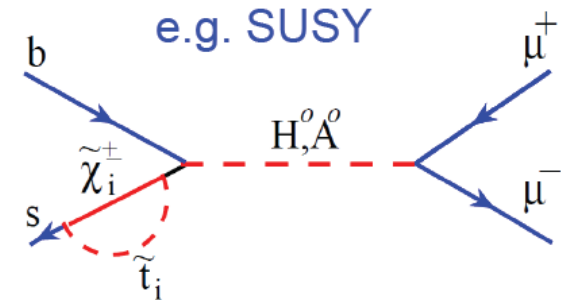
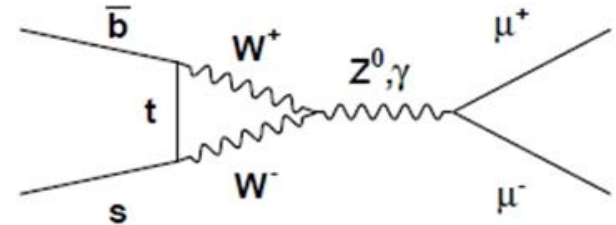
$$\mathcal{B}(B_s^0 \rightarrow \mu\mu) = (3.65 \pm 0.23) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu\mu) = (1.06 \pm 0.09) \times 10^{-10}$$

→ Enhanced by New Physics models
(e.g. SUSY $\sim \text{tg}^6 \beta / m_A^4$)

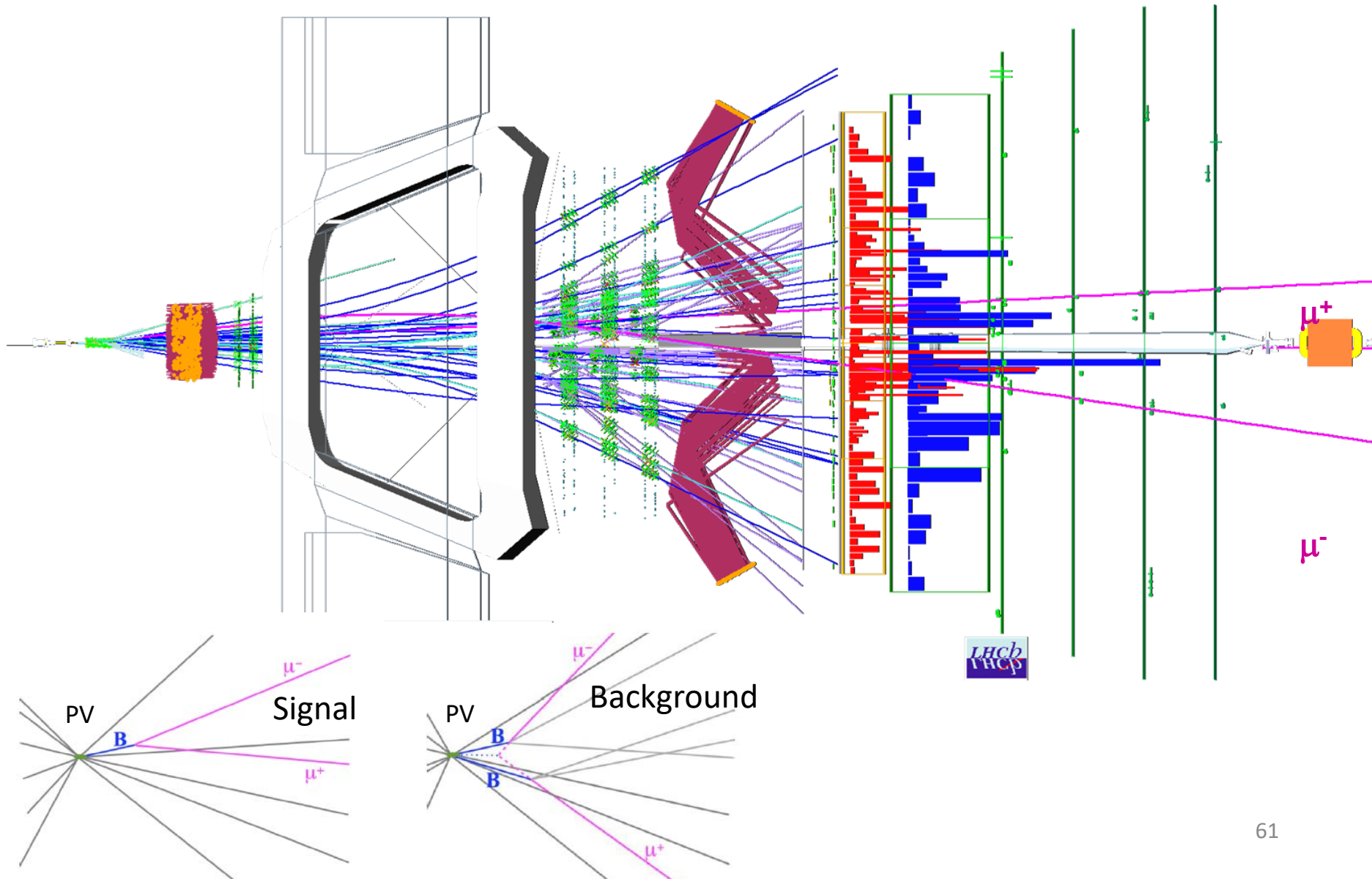
→ First evidence by LHCb in 2012!

[LHCb, PRL110 (2013)021801] (2fb⁻¹)



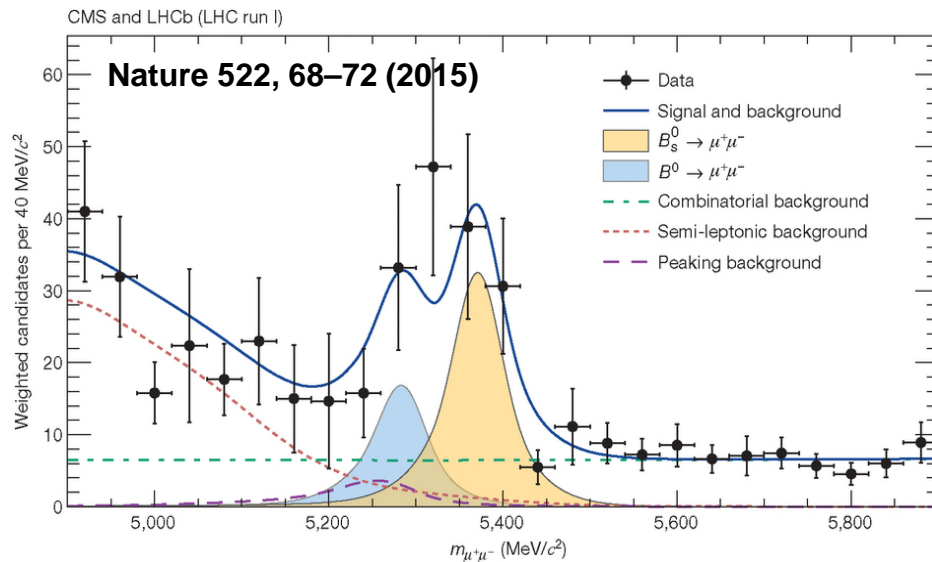
Rare decays: leptonic

$B_s \rightarrow \mu^+ \mu^-$ event



CMS + LHCb

Rare decays: leptonic



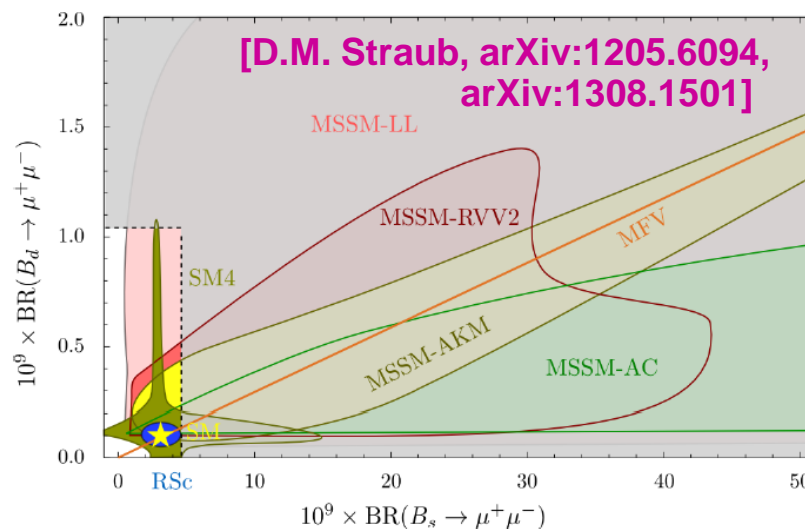
$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = 2.8_{-0.6}^{+0.7} \times 10^{-9}$$

6.2 σ

$$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-) = 3.9_{-1.4}^{+1.6} \times 10^{-10}$$

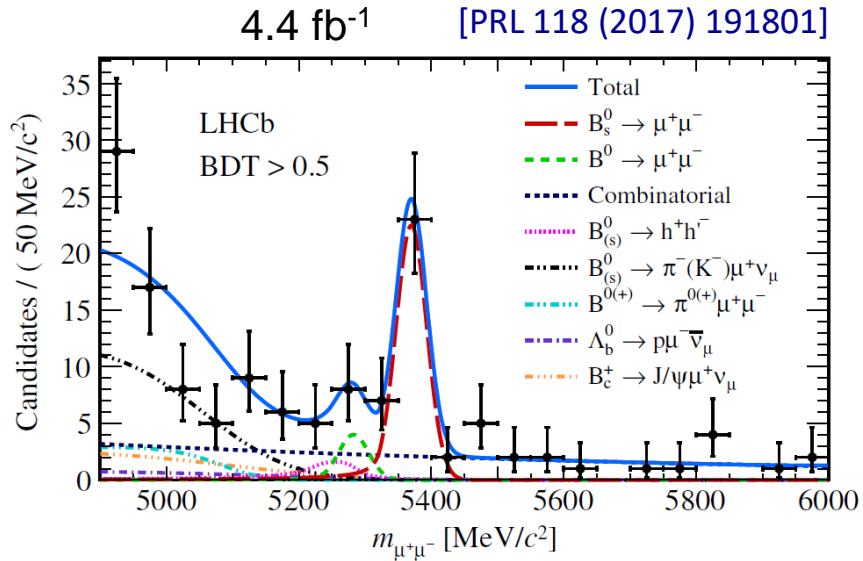
3.2 σ

- Known as “the New Physics killer”:



Rare decays: leptonic

Updated results:



$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (3.0 \pm 0.6^{+0.3}_{-0.2}) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-) < 3.4 \times 10^{-10} \text{ at 95\%}$$

→ In agreement with the SM

→ Theoretical uncertainties ($f_{B(s)}$, V_{CKM}) well below statistical uncertainty

- $B_s \rightarrow \tau^+\tau^-$ also searched for at LHCb:

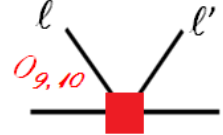
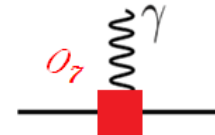
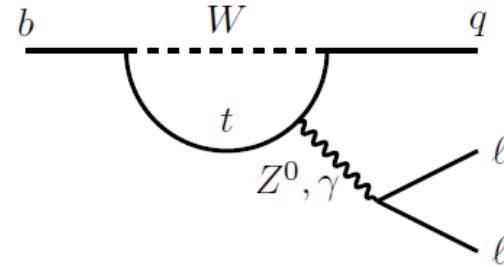
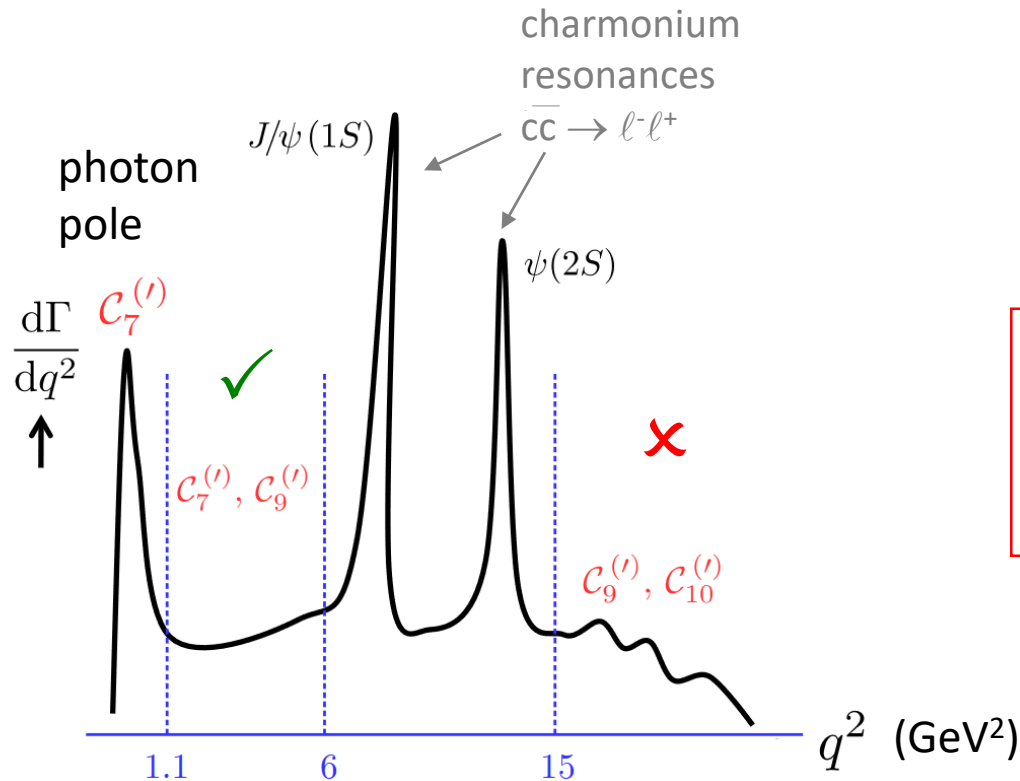
$$\mathcal{B}(B_s^0 \rightarrow \tau^+\tau^-) < 6.8 \times 10^{-3} \text{ at 95\%}$$

[arXiv:1703.02508 [hep-ex]]

Rare decays: semileptonic

Differential branching fraction: $d\Gamma/dq^2$

Each q^2 region probes different processes



SM values ($\mu=m_b$):

- $C_7 \sim -0.33$
- $C_9 \sim 4.27$
- $C_{10} \sim -4.17$

(Everything else small or negligible)

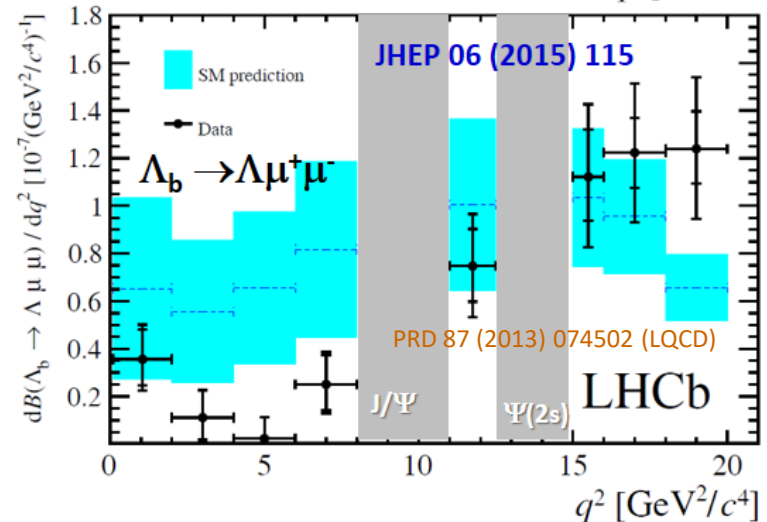
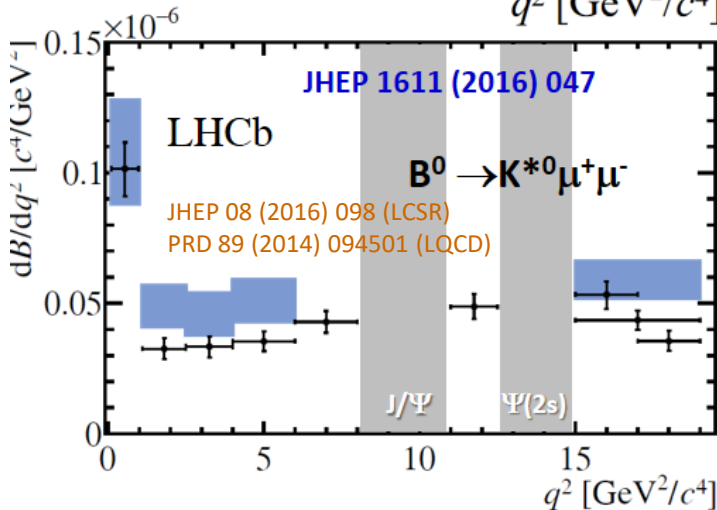
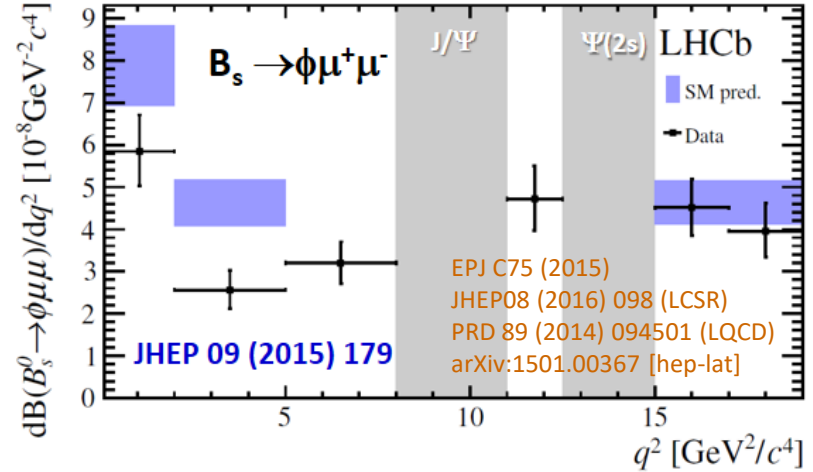
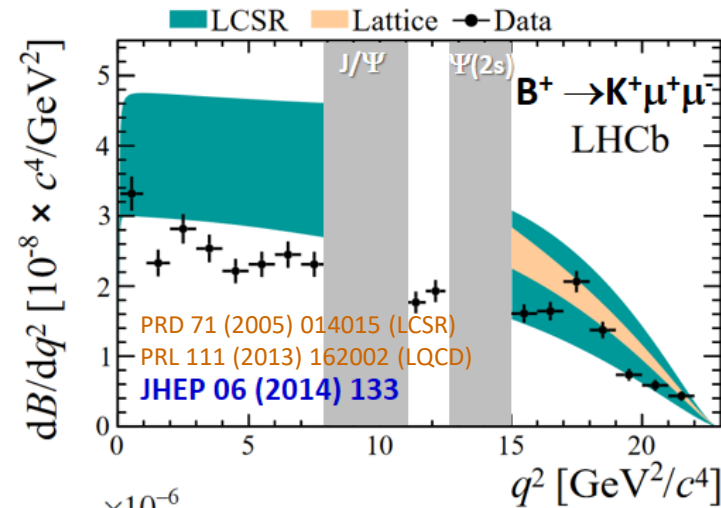
$$C_i = C_i^{\text{SM}} + C_i^{\text{NP}}$$

(Primed $C'_i \rightarrow$ right handed currents:
suppressed in SM)



Rare decays: semileptonic

- Differential decay width as function of $q^2 = m_{\mu\mu}^2$



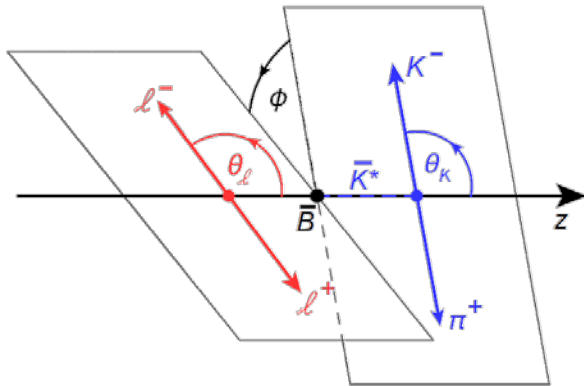
Theory affected by hadronic uncertainties: LCSR + LQCD



Rare decays: semileptonic

- Angular distribution in $B \rightarrow K^* \ell^- \ell^+ : q^2$ and three angles

$$\frac{1}{d\Gamma/dq^2 d\cos\theta_\ell d\cos\theta_K d\phi dq^2} \frac{d^4\Gamma}{dq^2} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi \right. \\ \left. + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$



$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$

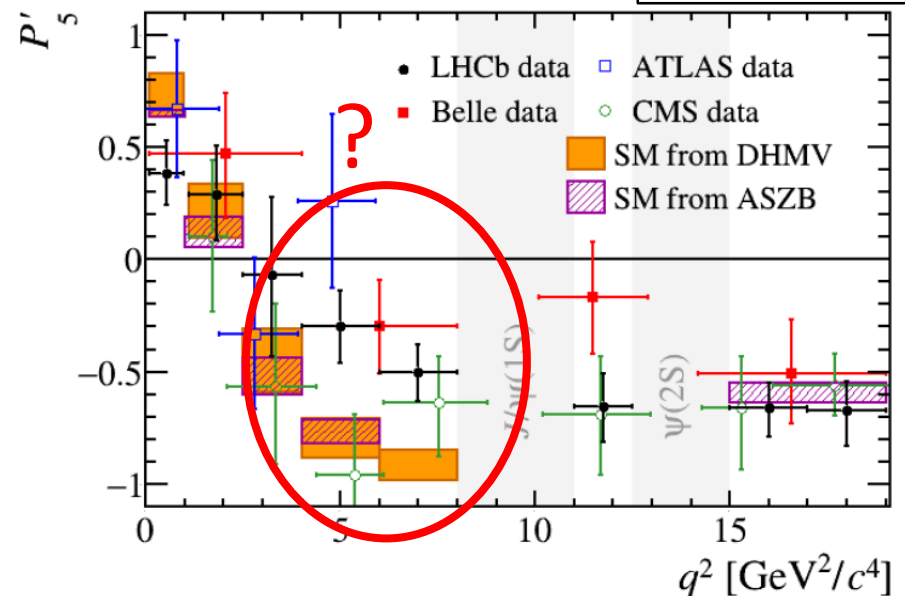
Functions of q^2 and Wilson coef. C_i

Optimized observables:
cancellation of form factor
dependencies: P'_i

[Descotes-Genon et al, JHEP 05 (2013) 137]

→ Deviation from SM $\sim 3\sigma$

- JHEP 02 (2016) 104
- PRL 118 (2017) 111801
- ATLAS-CONF-2017-023
- CMS-PAS-BPH-15-008



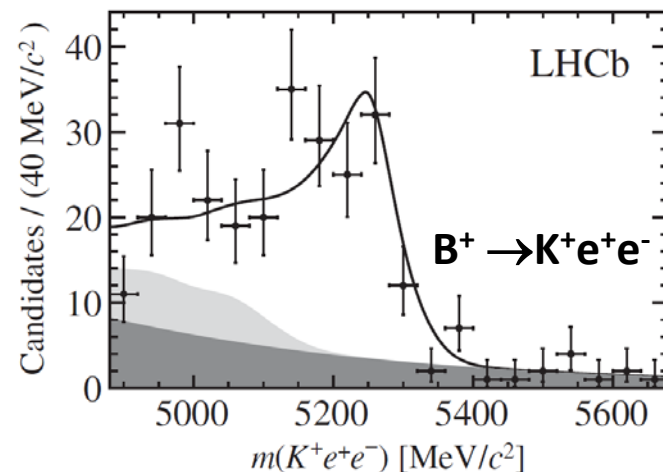
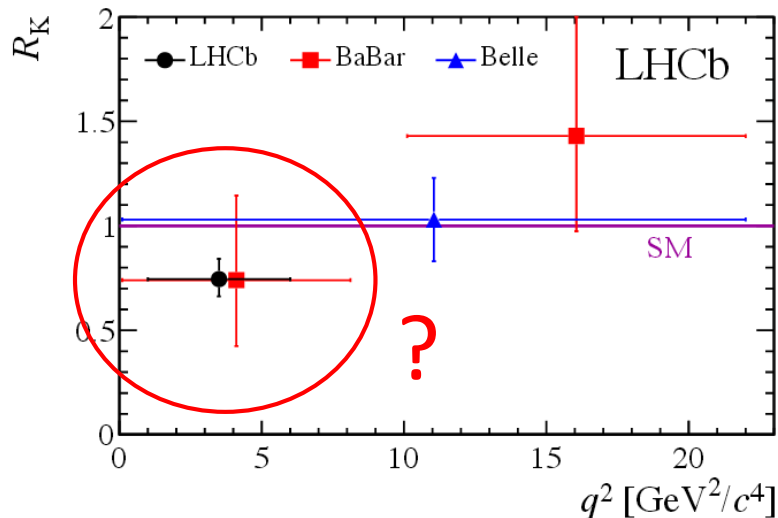


Rare decays: semileptonic

- In the SM all leptons are expected to behave in the same way:

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)} = 1.000 + \mathcal{O}(m_\mu^2/m_b^2) \text{ (SM)}$$

- Experimentally, use the $B^+ \rightarrow K^+ J/\psi (\rightarrow e^+ e^-)$ and $B^+ \rightarrow K^+ J/\psi (\rightarrow \mu^+ \mu^-)$ to perform a double ratio
- Precise theory prediction due to **cancellation of hadronic form factor uncertainties**



$1 \text{ GeV} < q^2 < 6 \text{ GeV}$ [PRL 113 (2014) 151601]

$$R_K = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{syst})$$

→ Consistent, but lower, than the SM at **2.6σ**

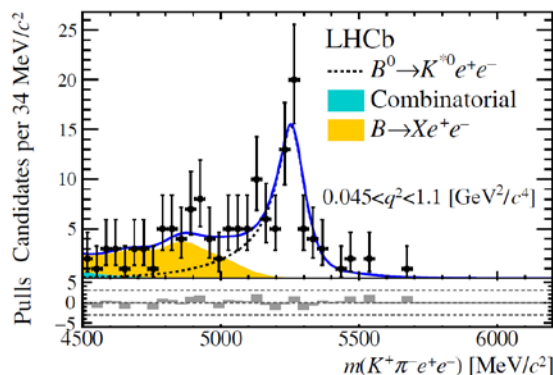


Rare decays: semileptonic

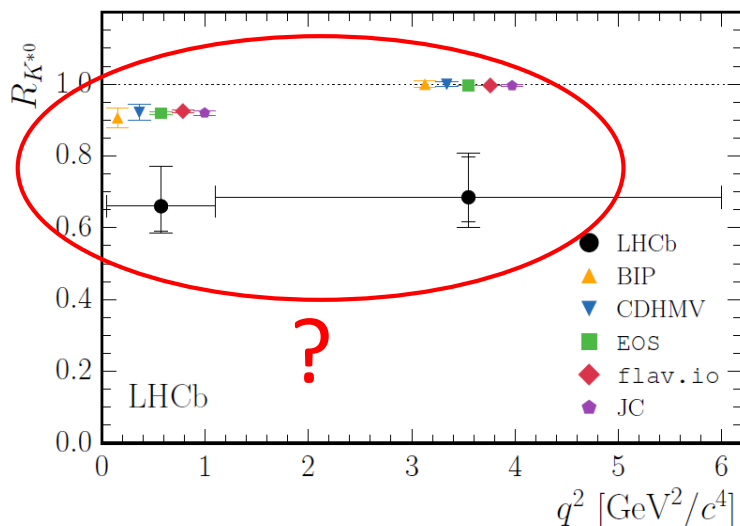
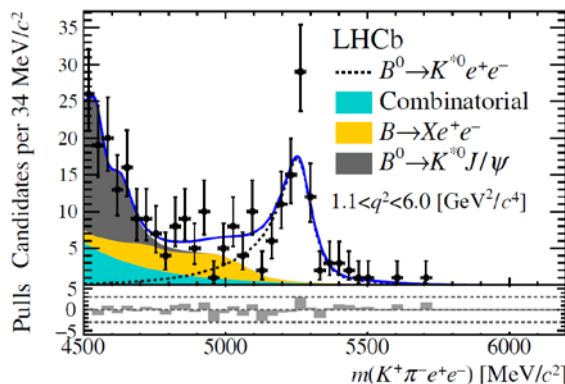
$$\mathcal{R}_{K^{*0}} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)}$$

[arXiv:1705.05802 [hep-ex]]

0.045 GeV < q² < 1.1 GeV



1.1 GeV < q² < 6 GeV



Low q²: SM = 0.922(22)

$$\mathcal{R}_{K^{*0}} = 0.66 \pm 0.11 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

Central q²: SM = 1.000(6)

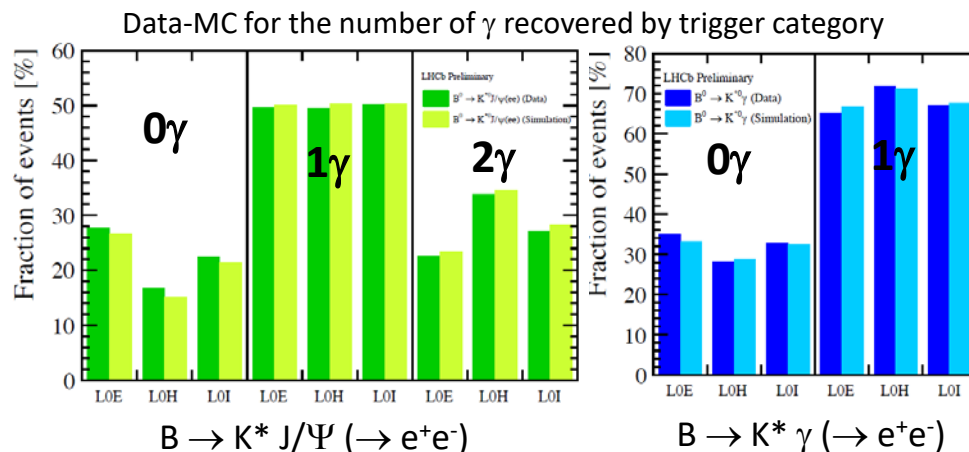
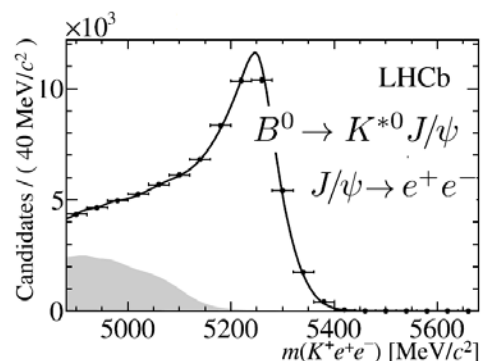
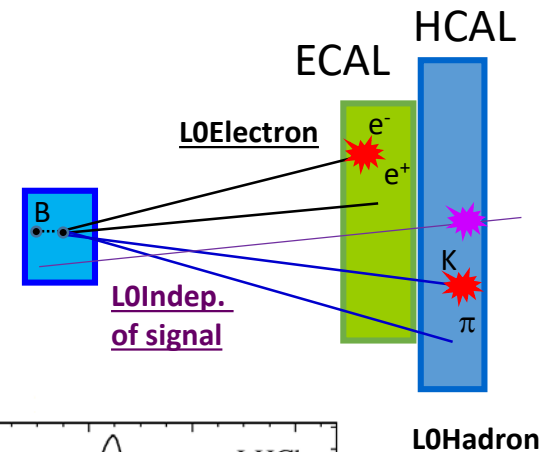
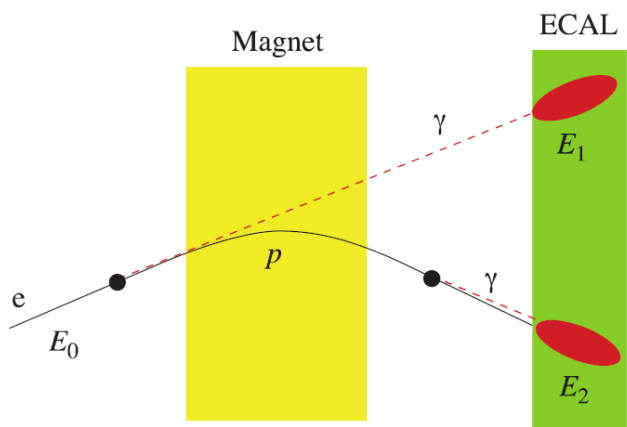
$$\mathcal{R}_{K^{*0}} = 0.69 \pm 0.11 \text{ (stat)} \pm 0.05 \text{ (syst)}$$

→ Consistent, but lower than the SM at
2.1-2.3σ (low q²) and **2.4-2.5σ** (central q²)

Rare decays

Quick note on experimental issues:

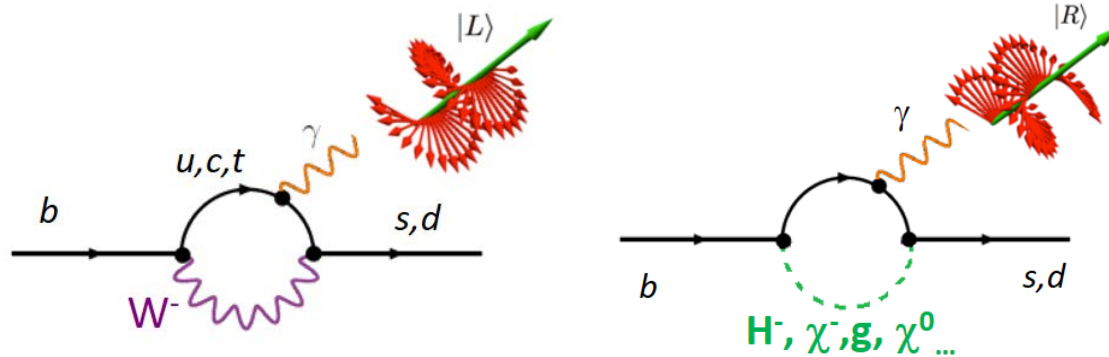
- LHCb is far better with muons than electrons
- *Trigger*, reconstruction, selection and particle identification are harder with electrons
- Mass resolution affected by *e bremsstrahlung* → need energy recovery
- Mass shape modelled according to the number of *bremsstrahlung* recovered



Rare decays: radiative

Probing the spin structure of the photon: $B_s \rightarrow \phi \gamma$

- In the Standard Model photons emitted in $b \rightarrow s \gamma$ transitions are left-handed polarized
- New particles in the loop could add right-handed contributions



- The polarization of the photon can be inferred from the time evolution of the B_s decay

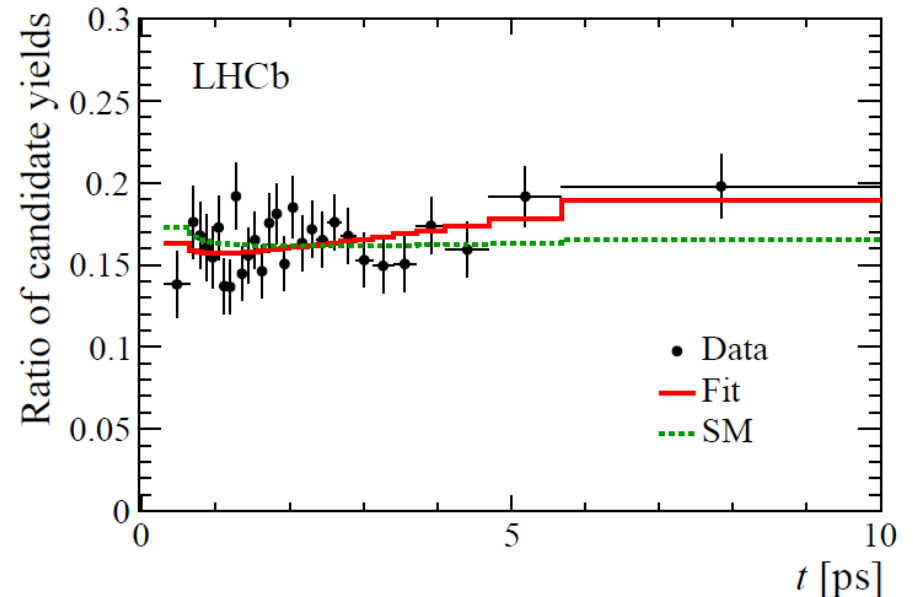
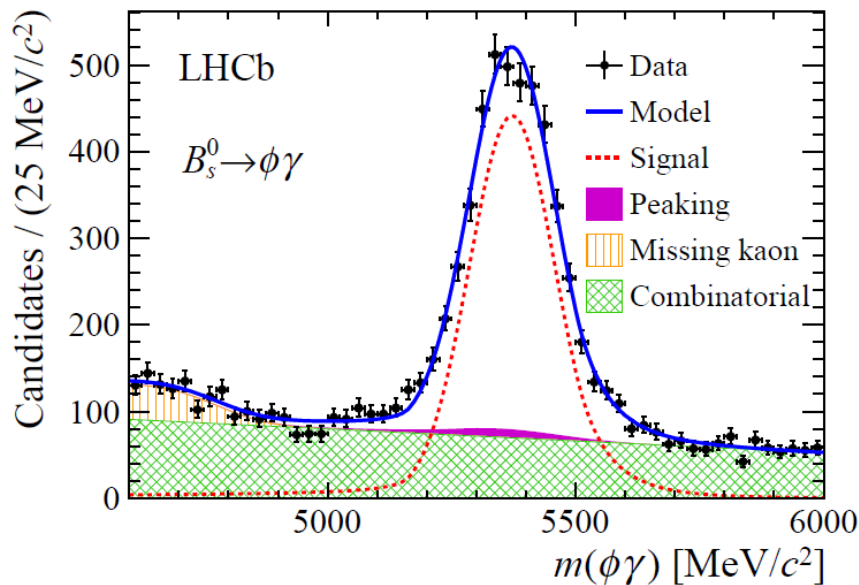
$$\Gamma_{B_s^0}(t) = |A|^2 e^{-\Gamma_s t} \left(\cosh \frac{\Delta\Gamma_s t}{2} - \mathcal{A}^\Delta \sinh \frac{\Delta\Gamma_s t}{2} \right)$$

Related to the ratio of right to left handed amplitudes

Rare decays: radiative

This sensitivity comes from the effect of the mixing of $B_s \rightarrow \phi \gamma$ and $\bar{B}_s \rightarrow \phi \gamma$ with $\phi \rightarrow K^+ K^-$

Use a control channel with no sensitivity to the photon polarization
(ex: a flavor specific channel $B \rightarrow K^* \gamma$, with $K^* \rightarrow K \pi^+$)



$$\mathcal{A}^\Delta = -0.98^{+0.46}_{-0.52} +0.23_{-0.20}$$

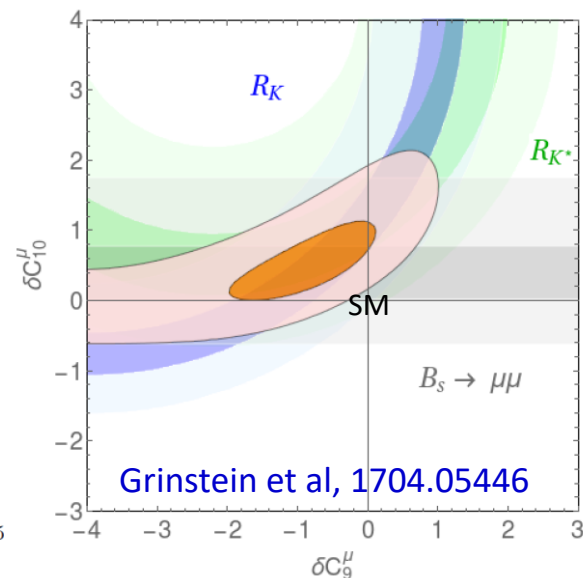
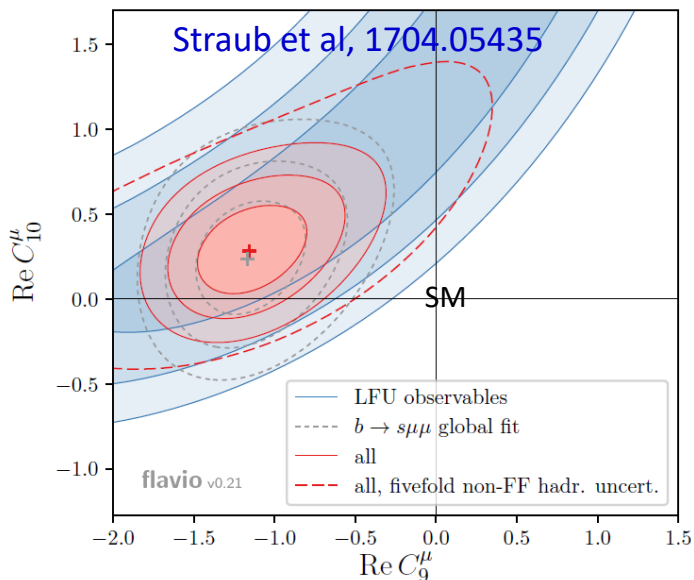
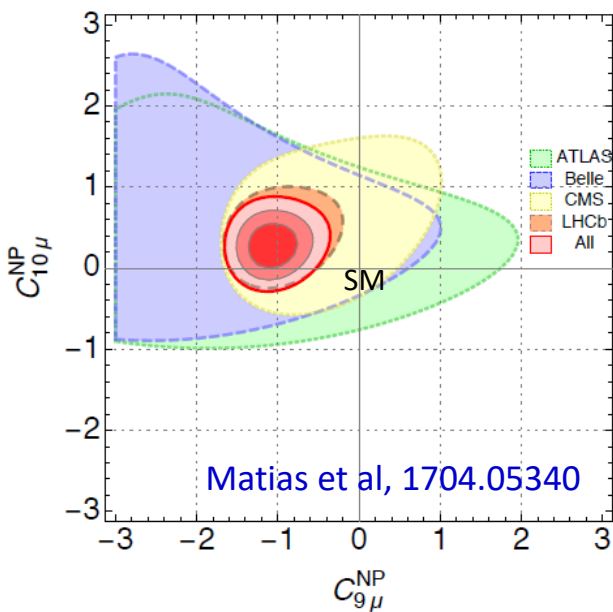
[PRL 118 (2017) 021801]

$$\mathcal{A}_{\text{SM}}^\Delta = 0.047^{+0.029}_{-0.025} \rightarrow \text{Compatible with the SM within } 2\sigma$$



Rare decays

Global fits (some cases with more than 100 observables)



New Physics hypothesis preferred over SM by more than 4 - 5 σ

Main effect on the $C_{9\mu}$ coefficient: $4.27^{\text{SM}} - 1.1^{\text{NP}}$

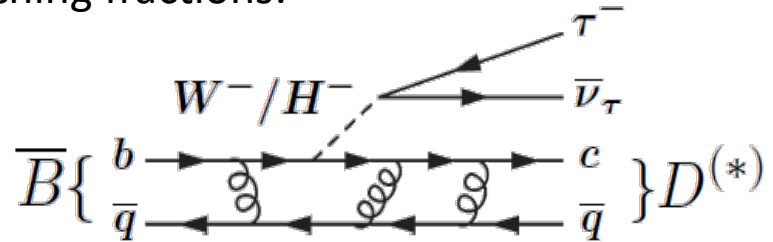
Triggered models with Z', leptoquarks (LQ), and composite Higgs

Lepton flavour universality

- Another test of lepton universality (now at tree level):

Ratio of semi-tauonic and semi-muonic branching fractions:

$$\mathcal{R}(D^*) = \frac{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \mu^- \bar{\nu}_\mu)}$$



Sensitive to charged Higgs bosons and leptoquarks

SM predictions very precise : (V_{cb} and form factors (partially) cancel)

$$\mathcal{R}(D)_{\text{SM}} = 0.299 \pm 0.003$$

$$\mathcal{R}(D^*)_{\text{SM}} = 0.252 \pm 0.003$$



BaBar measured an excess of $\bar{B}^0 \rightarrow D^{(*)} \tau^- \bar{\nu}_\tau$ (**3 σ away from SM**) [[PRD 88 \(2013\) 072012](#)]
[[Nature 546\(2017\)227](#)]



LHCb has performed two analyses:

- $\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$, with $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$ [[PRL 115 \(2015\) 111803](#)]
- $B^0 \rightarrow D^{*-} \tau^+ \nu$, with $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \pi^{(0)} \bar{\nu}_\tau$ [[JHEP 08 \(2017\) 055](#)]

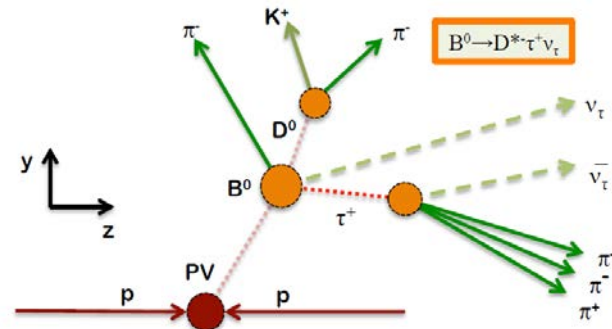
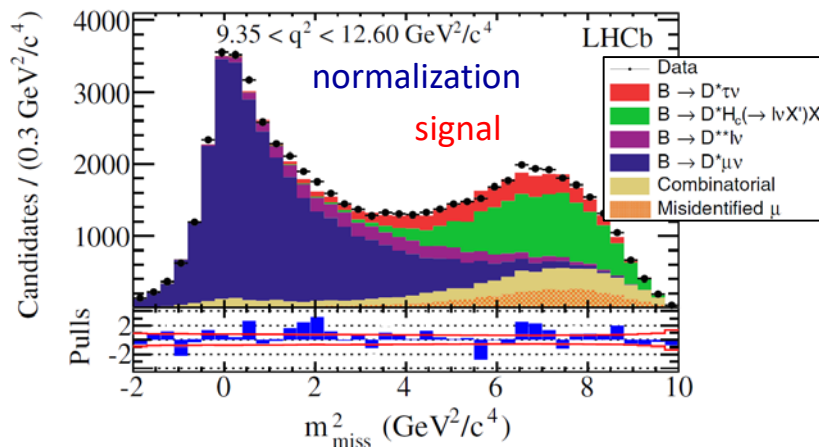


Lepton flavour universality

- Using $\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$
- Information from the missing mass squared $m_{\text{miss}}^2 = (P_B - P_{D^*} - P_\mu)^2$ and muon energy in several q^2 bins

$$\mathcal{R}(D^*) = 0.336 \pm 0.027(\text{stat}) \pm 0.030(\text{syst})$$

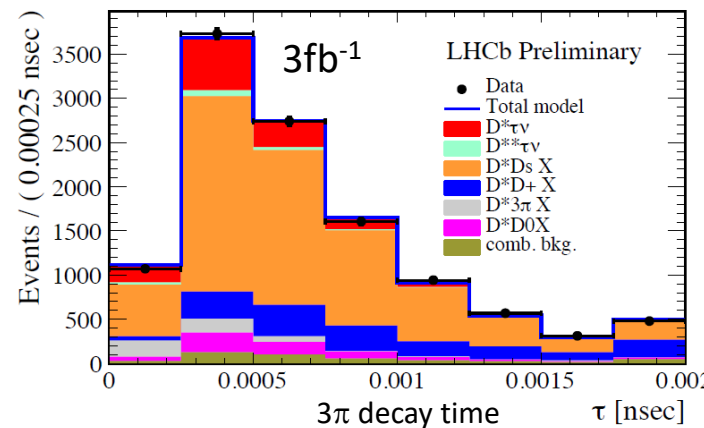
[PRL 115 (2015) 111803]



- New analysis by LHCb: using $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau$
- Information from the position of the three pions
- Normalized to $B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+$

$$\mathcal{R}(D^{*-}) = 0.285 \pm 0.019 \pm 0.025 \pm 0.014$$

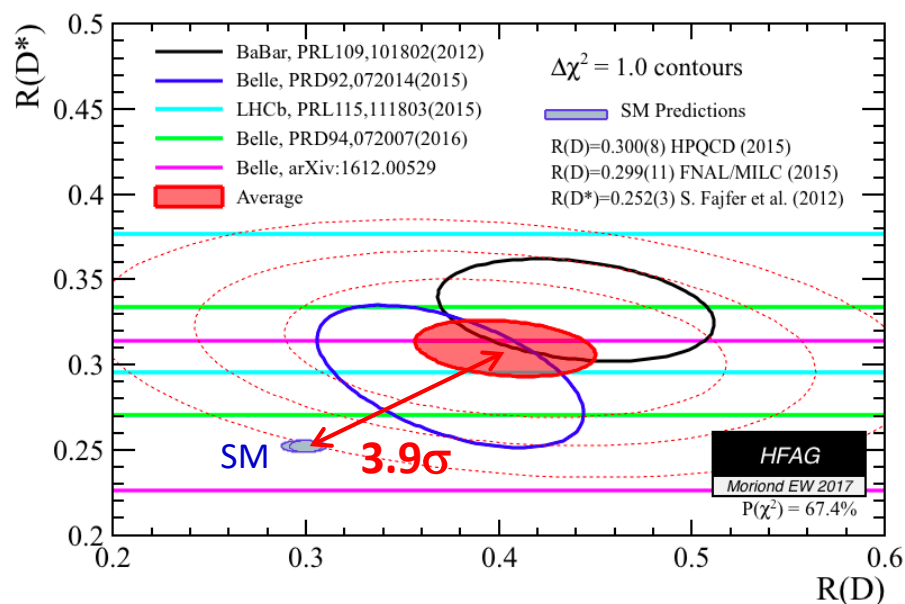
[JHEP 08 (2017) 055]



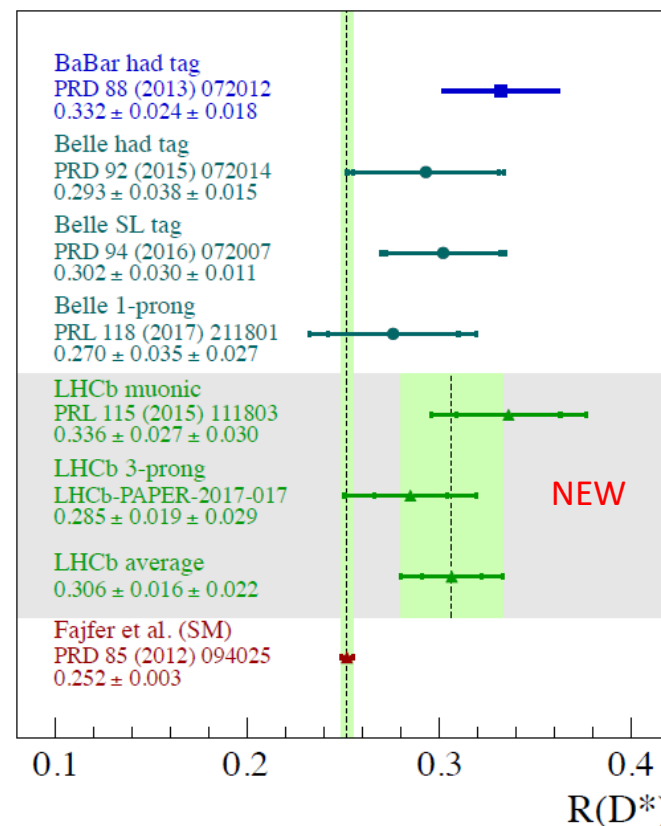


Lepton flavour universality

- Global picture of R_D and R_{D^*}



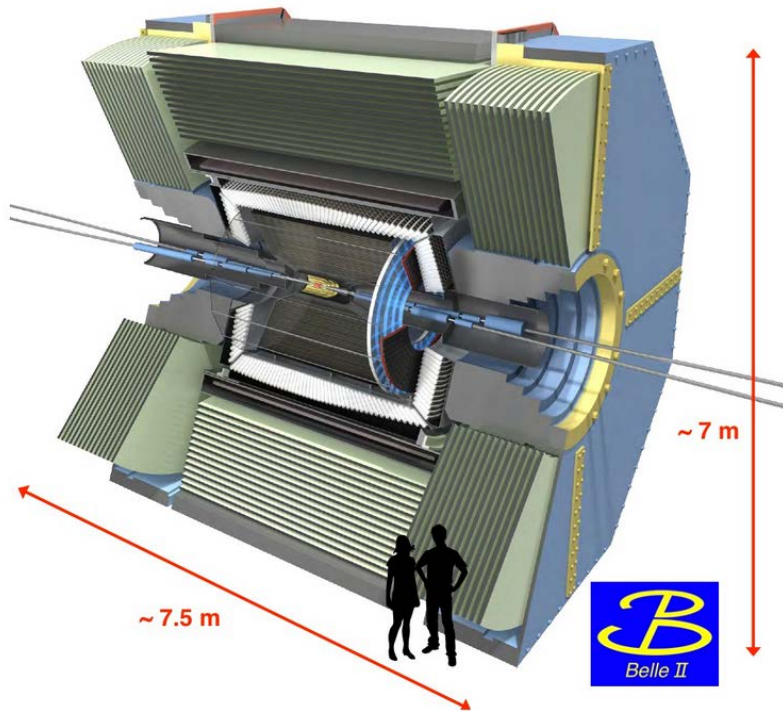
→ About 4σ deviation from SM



Future plans

Belle II

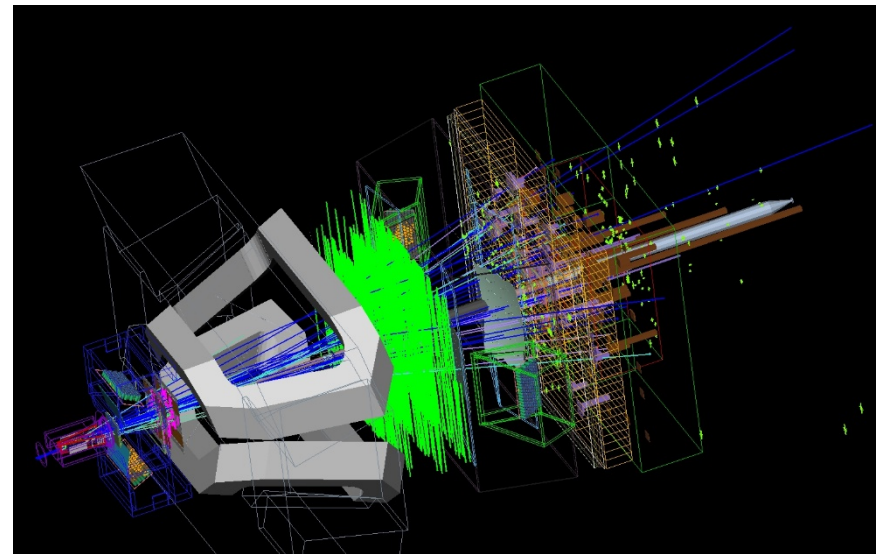
e⁺e⁻ asymmetric collider (SuperKEK)
at the Y(4S) energy in Tsukuba, Japan



Starting now !

LHCb Upgrade

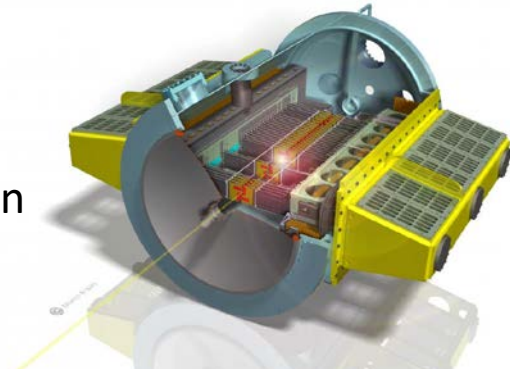
Improved trigger, improved detector



Starting in 2019

Future plans

- At present we did not find evidence for New Physics, but some “anomalies” (let’s cross fingers!!)
- Standard Model deviations are expected to be small
- Most of the measurements are limited by the statistical precision



	LHC era		High-lumi LHC era		
	2010-2012	2015-2018	2020-2022	2025-2028	2030+
ATLAS & CMS	25 fb ⁻¹	100 fb ⁻¹	300 fb ⁻¹	→	3000 fb ⁻¹
LHCb	3 fb ⁻¹	8 fb ⁻¹	23 fb ⁻¹	46 fb ⁻¹	100 fb ⁻¹
Belle II		0.5 ab ⁻¹	25 ab ⁻¹	50 ab ⁻¹	-

Remember that we have 10^{11} $b\bar{b}$ pairs/fb !
(At Belle II: 10^9 $B\bar{B}$ pairs/ab)

Future plans

Complementarity:

LHCb

ATLAS & CMS

- Rare decays: $B_{d,s} \rightarrow \mu\mu$
- B_s system
- b-baryons
- Spectroscopy

- CKM phases (β, γ)
 - Gluonic penguins
 - EW penguins
 - Charm physics
 - Semileptonics: Mixing, A_{SL}
- } Some only LHCb, some only Belle II

On-going

Belle II

- Semileptonics: V_{xb}
- $B \rightarrow \tau \nu$, $D \tau \mu$
- $B \rightarrow K^* \nu \nu$
- τ -physics

Let's hope!

