

An introduction to the double beta decay



F. Piquemal

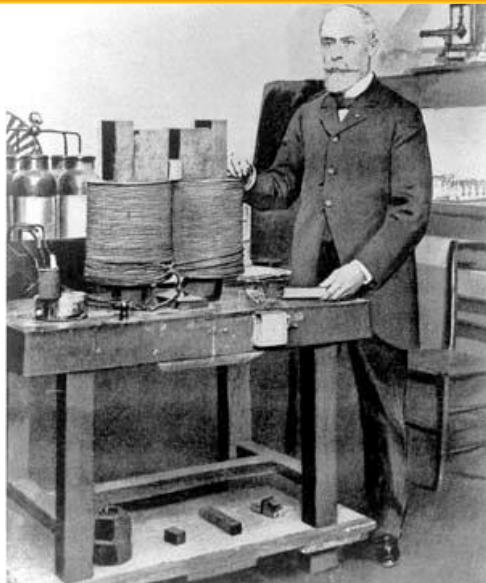
Modane Underground Laboratory (CNRS/IN2P3 and CEA/Irfu)

Particle physics school , Annecy July,24 2013

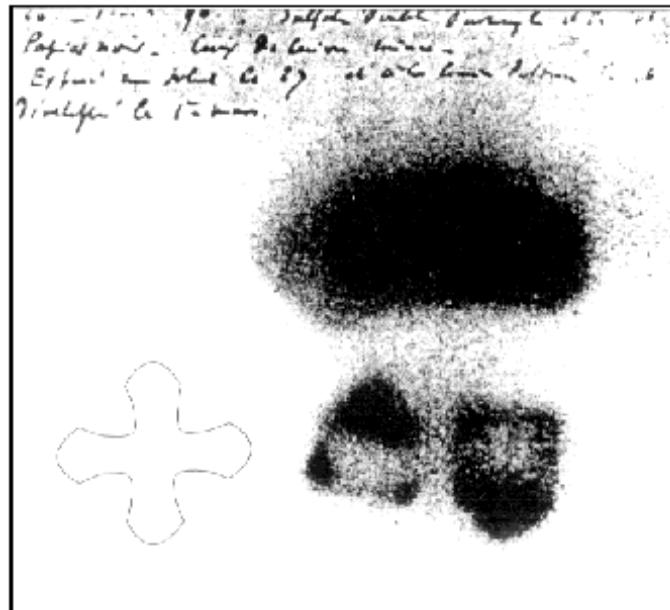
Plan

- ❑ Short history of beta decay and double beta decay
- ❑ Double beta decay and neutrino properties
- ❑ How to perform a double beta decay experiment
- ❑ The experimental challenges to look for double beta decay
- ❑ Presentation of few experiments

The beginning of the history

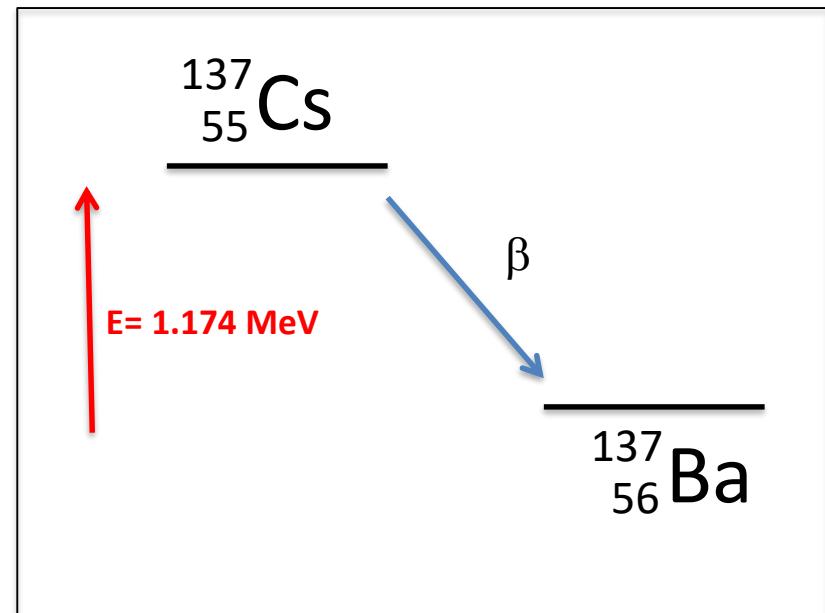
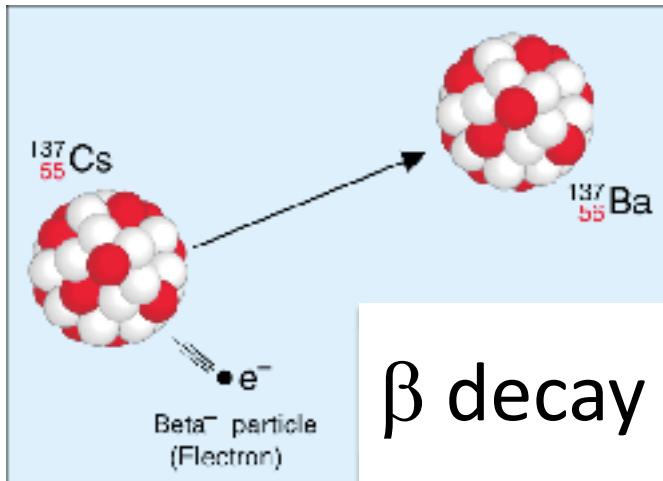
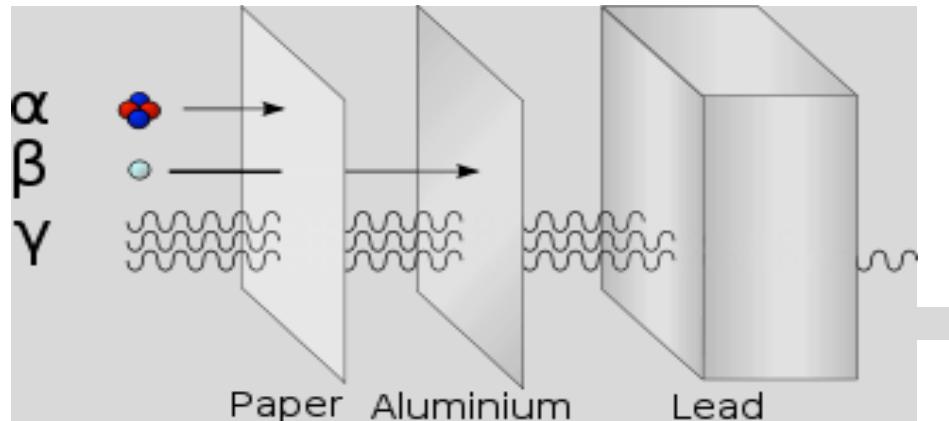


1896 - 1898:
Becquerel, Pierre and Marie Curie
discovered the radioactivity



The beginning of the history

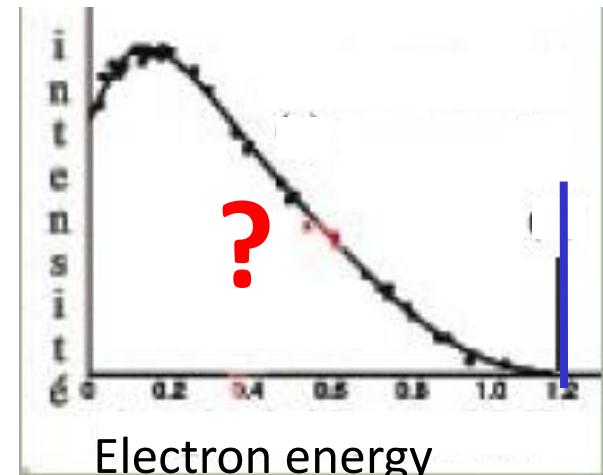
Rutherford, Chadwick,
P. et M. Curie and Villard
identified 3 kinds of radiations



The beginning of the history



1914 : Chadwick, Hahn and Meitner measured the beta energy spectrum



1914 – 1930 : Energy crisis in the subatomic world

Is there non-conservation of energy ?

The beginning of the history



1930 W. Pauli postulated the neutrino
No interaction with matter
No mass (or very small)
Fermion - spin 1/2

Physikalisches Institut
der Eidg. Technischen Hochschule
Zürich

Zürich, 4. Dez. 1930
Gloriastrasse

Dear Radioactive Ladies and Gentlemen.

As the bearer of these lines, to whom I ask you to lend most graciously your ears, will explain in greater detail, I have hit, in view of the "false" statistics of the N and Li-6 nuclei and of the continuous β -spectrum, upon a desperate expedient for saving the "Wechselsatz"[†] of statistics and energy conservation. This is the possibility that electrically neutral particles, which I shall call neutrons, might exist in the nucleus, having spin 1/2 and obeying the exclusion principle. In addition they differ from light quanta in that they do not travel at the speed of light. The mass of the neutron should be of the same order of magnitude as that of the electron and in any event no greater than 0.01 of the proton mass. The continuous β -spectrum would then be comprehensible on the assumption that on β -decay a neutron is emitted with the electron in such a way that the sum of the neutron and the electron energy is constant.

Furthermore the question arises which forces act on the neutron. For reasons of wave mechanics (the bearer of these lines knows more about this) the likeliest model for the neutron seems to me to be, that the neutron at rest is a magnetic dipole with a certain moment μ . Experiments apparently demand that the ionising effect of such a neutron is no greater than that of a γ -ray, in which case μ should be no greater than $e (10^{-13} \text{ cm})$.

For the moment I would not venture to publish anything on this notion and should like first of all to turn trustingly to you, dear Radioactives, with the question concerning the prospects for experimental verification of the existence of such a neutron if it were to have the same or perhaps a 10 times greater penetrating power as a γ -ray.

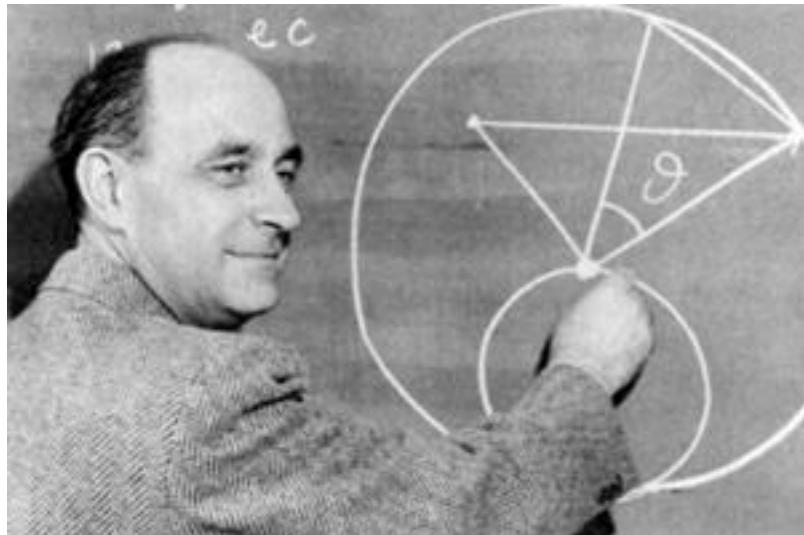
I admit that my expedient may seem rather improbable from the first, because if neutrons existed they would have been discovered long since. Nevertheless, nothing ventured nothing gained, and the seriousness of the situation with the continuous β -spectrum is illustrated by a statement by my esteemed predecessor in office, Mr. Debye, who recently told me in Brussels: "Oh, it's better to ignore that completely, just like the new taxes". We should therefore be seriously discussing every path to salvation. So, dear Radioactives, consider and judge. Unfortunately I cannot come to Tübingen in person since my presence here is essential as a result of a ball held on the night of 6th to 7th December in Zürich.

With kind regards to all of you and Mr. Back, I remain,
your humble servant,

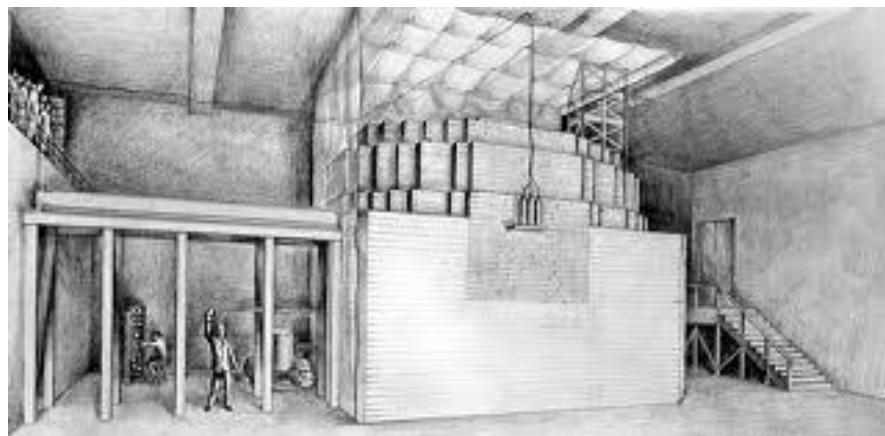
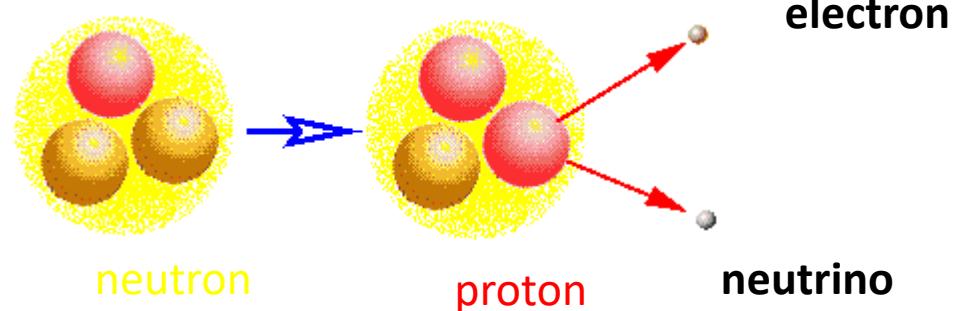
(signed) W. Pauli

[†] This states: Fermi statistics and half-numbered spin for nuclei with an odd total number of particles; Bose statistics and integer spin for nuclei with an even total number of particles.

The beginning of the history



1933 : Fermi elaborated the theory of the weak interaction

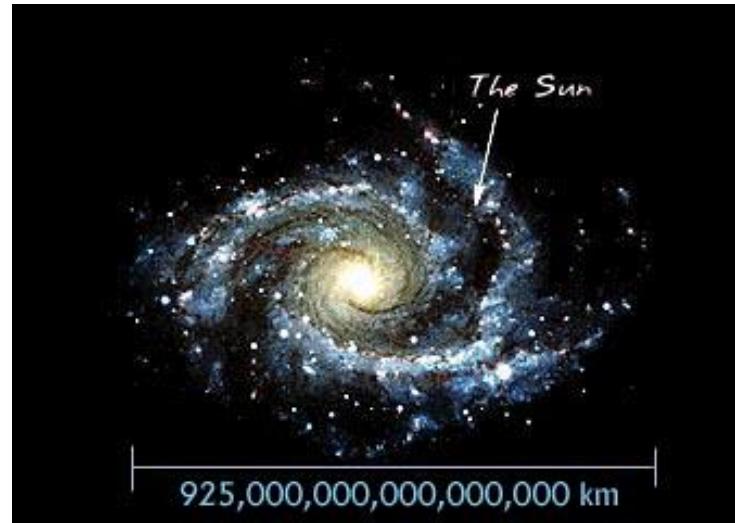


1942 : Fermi created the first nuclear reactor under the stadium of the Chicago University

The discovery of the neutrino

Neutrino Trap

← 30 000 000 000 000 km of lead →



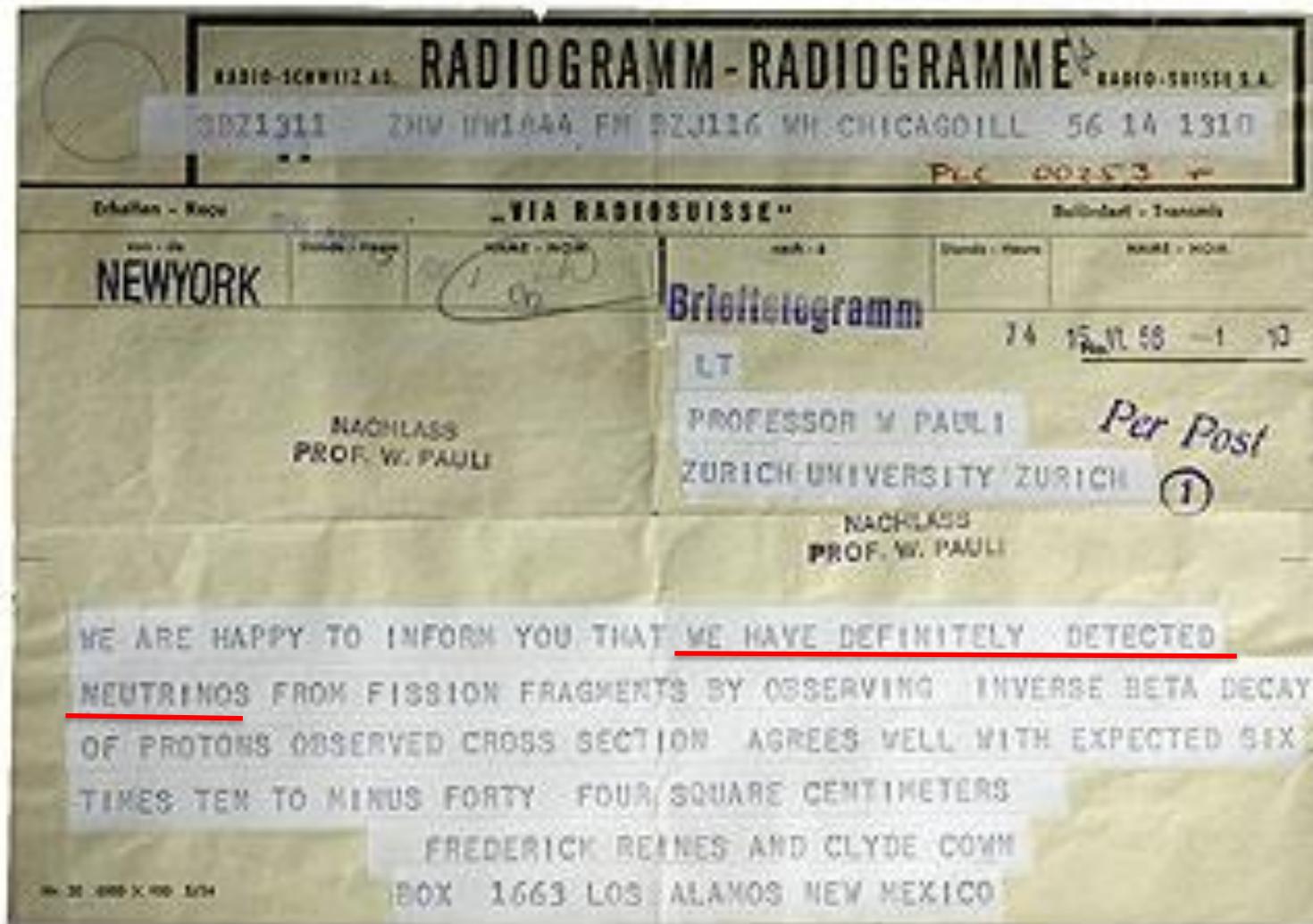
Possible neutrino interactions



To detect neutrinos: plenty of neutrinos and a lot of matter !

The discovery of the neutrino

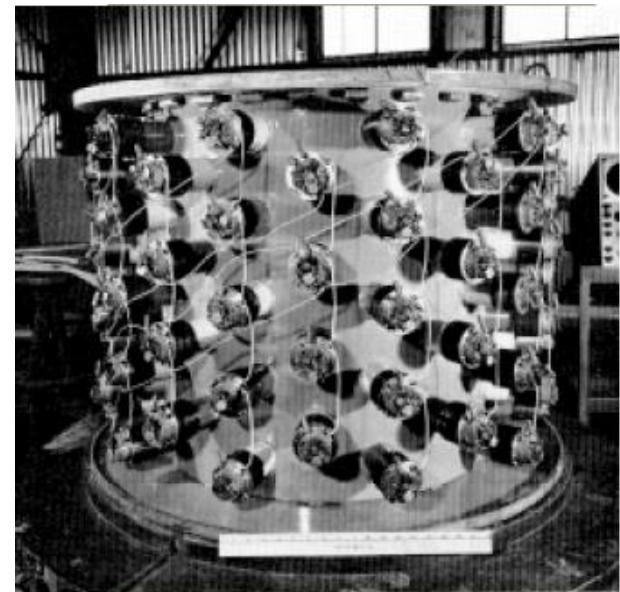
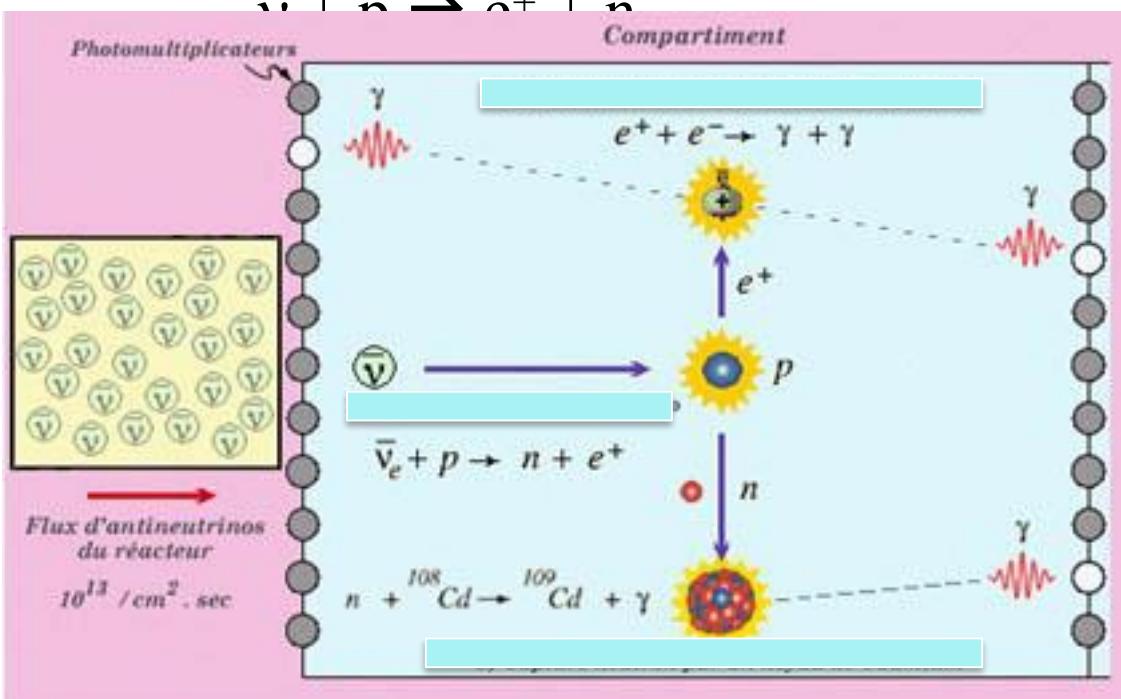
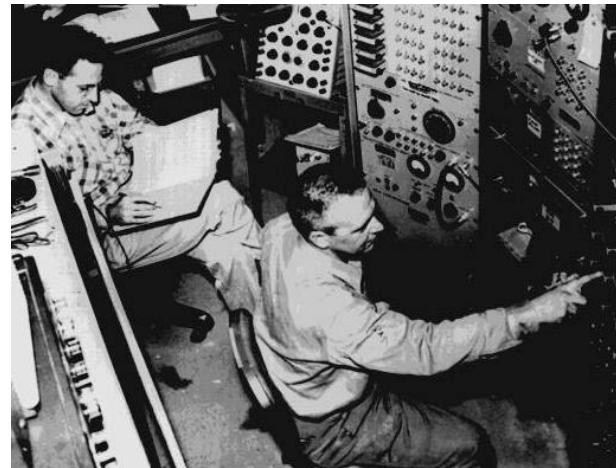
1956: Neutrino discovery by Reines and Cowan



The discovery of the neutrino



Savannah River reactor (USA)



Poltergeist detector

Ettore Majorana

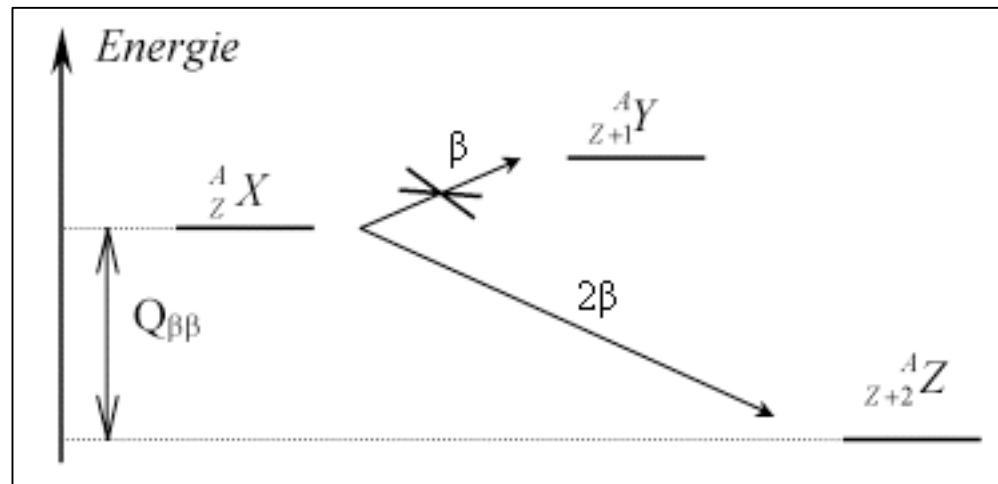


**1937: Ettore Majorana proposed a theory for neutral particle which can be its own anti-particle
Neutrino = anti-neutrino ?**

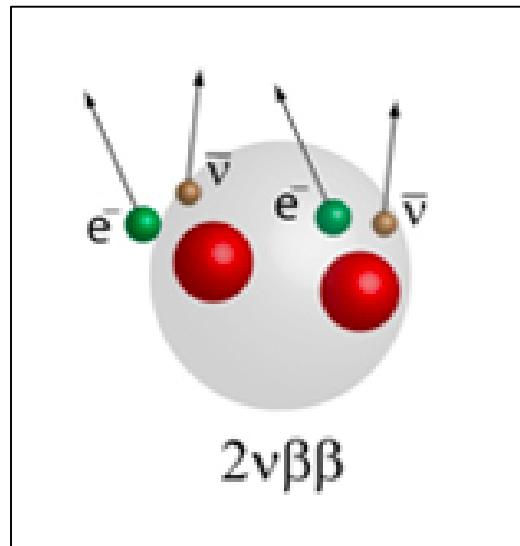
Fermi: «There are several categories of scientists: those who do their best, and those of the first plan, which make important discoveries ... And then there are the geniuses, like Galileo and Newton, Ettore was one of them ...»

Is the neutrino at the origin of the matter

The beginning of the history



1935: Maria Goeppert-Mayer postulates the existence of the double beta decay, second order process of the beta decay

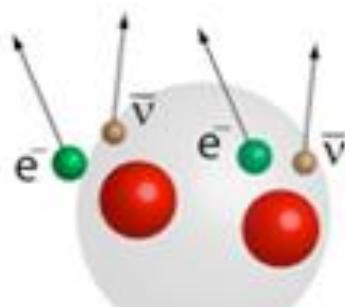


The beginning of the history

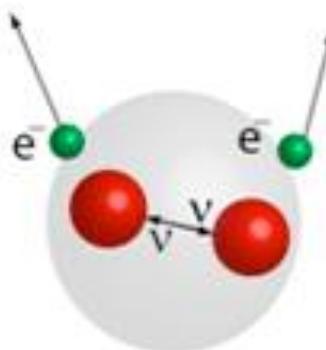


Scanned at the American
Institute of Physics

1939: Wendell Hinkle Furry demonstrates that if the neutrino is a Majorana particle (neutrino = anti-neutrino) then a new radioactivity can occur:
The neutrinoless double beta decay



$2\nu\beta\beta$



$0\nu\beta\beta$

Elementary particles

Quarks



up



down



charm



strange



top



bottom

Leptons



e - neutrino
1956



electron



μ - neutrino
1963



muon



τ - neutrino
2000



tau

matière

And also the anti-matter

Mass of particles

e-neutrino
 μ -neutrino
 τ -neutrino

Electron

Up

Down Strange

Muon

Tau

Bottom

Charm

Top



INTERACTION

MEDIATOR

RELATIVE STRENGTH

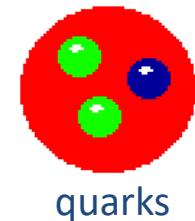
Range (m)

STRONG

GLUONS

~ 1

$\sim 10^{-15}$

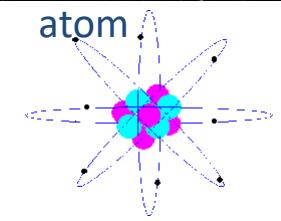


ELECTRO-MAGNETIC

PHOTON

$\sim 10^{-2}$

infinite

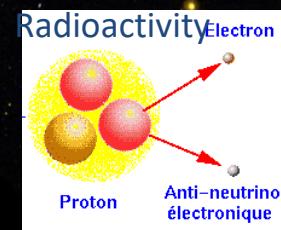


WEAK INTERACTION

w^+, w^-, z^0

$\sim 10^{-8}$

$\sim 10^{-18}$



GRAVITATION

GRAVITON ?

$\sim 10^{-38}$

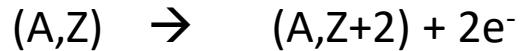
infinite



Neutrinoless double beta decay and neutrino properties

What can we learn with neutrinoless double beta decay about neutrino properties

$\beta\beta(0\nu)$ forbidden by Standard Model



L=0

L=2

$\Delta L=2$



L=0

L=2 L=-2 $\Delta L=0$

Test of a theory beyond the Standard Model of particle physics

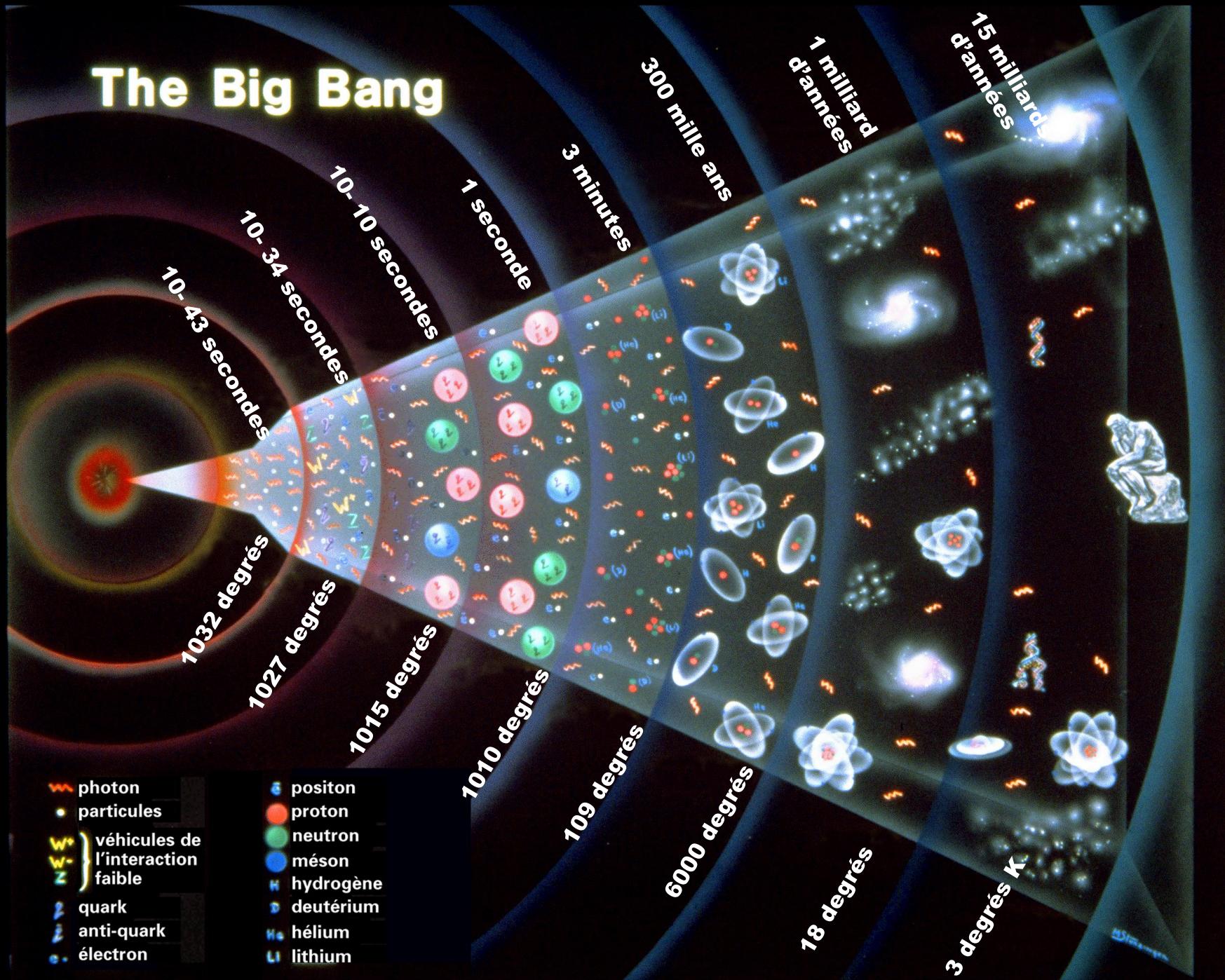
Nature of the neutrino: a Dirac particle ($\text{neutrino} \neq \text{antineutrino}$) ?

or

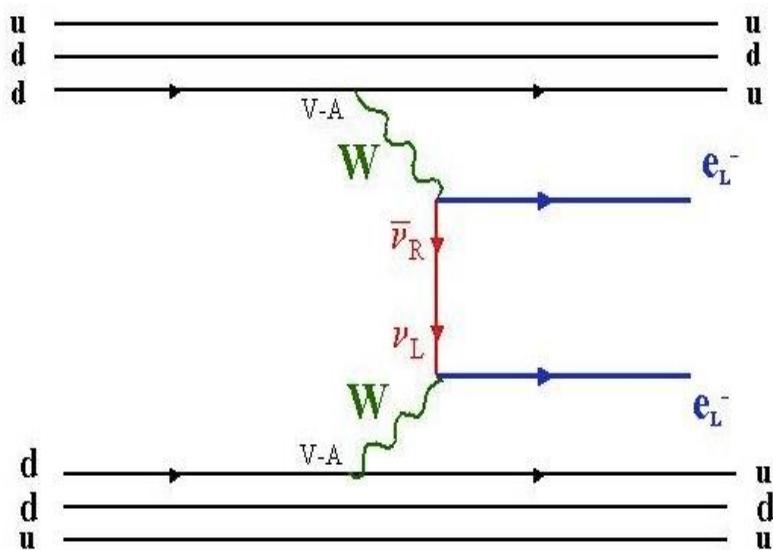
a Majorana particle ($\text{neutrino} = \text{antineutrino}$) ?

Strong impact on particle physics and in cosmology

The Big Bang



Neutrinoless double beta decay and neutrino properties



Phase space factor

$$T_{1/2}^{-1} = F(Q_{\beta\beta}^5, Z) |M|^2 \langle m_\nu \rangle^2$$

Nuclear matrix element

Effective mass:

$$\langle m_\nu \rangle = m_1 |U_{e1}|^2 + m_2 |U_{e2}|^2 \cdot e^{i\alpha_1} + m_3 |U_{e3}|^2 \cdot e^{i\alpha_2}$$

$|U_{ei}|$: mixing matrix element
 α_1 et α_2 : Majorana phase

Neutrinoless double beta decay and neutrino properties

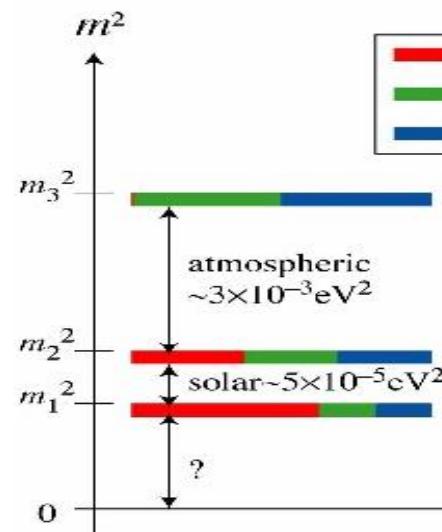
absolute mass ?

Tritium decay $m_{\nu_e} < 2.3 \text{ eV}$

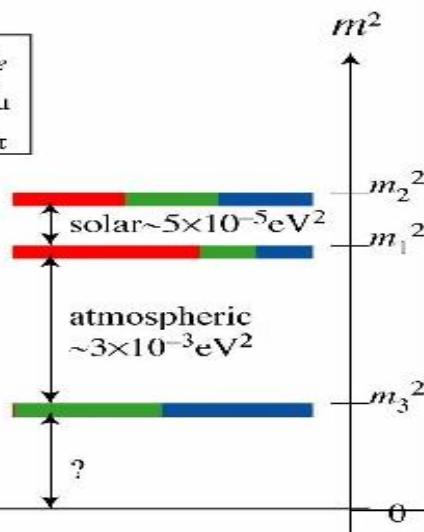
Cosmology $\sum m_i < \sim 1 \text{ eV}$

$\beta\beta(0\nu)$ $\langle m_\nu \rangle < 0.2\text{-}0.5 \text{ eV}$

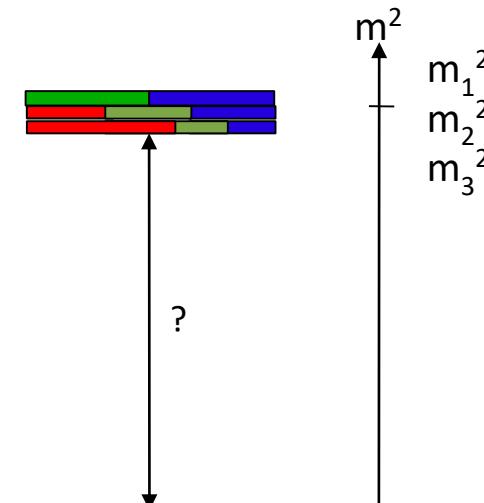
Mass scale ?



Normal hierarchy
 $m_1 > m_2 \sim m_3$



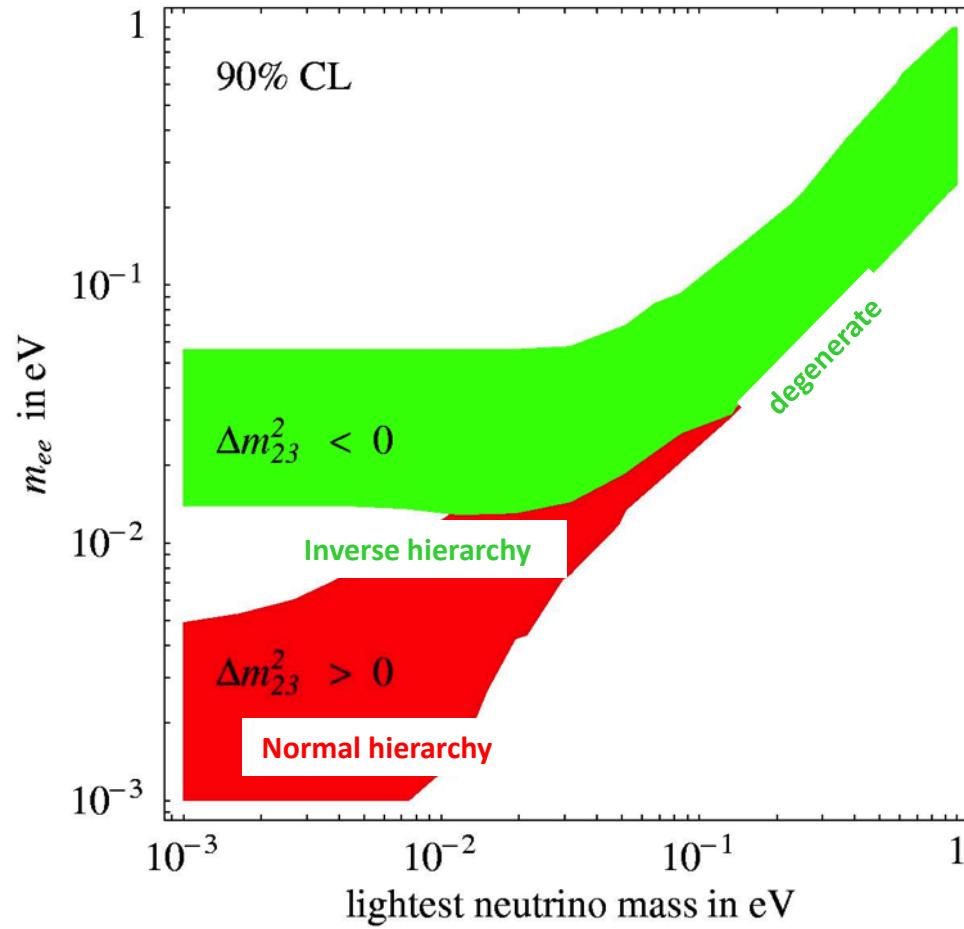
Inverted hierarchy
 $m_2 \sim m_1 > m_3$



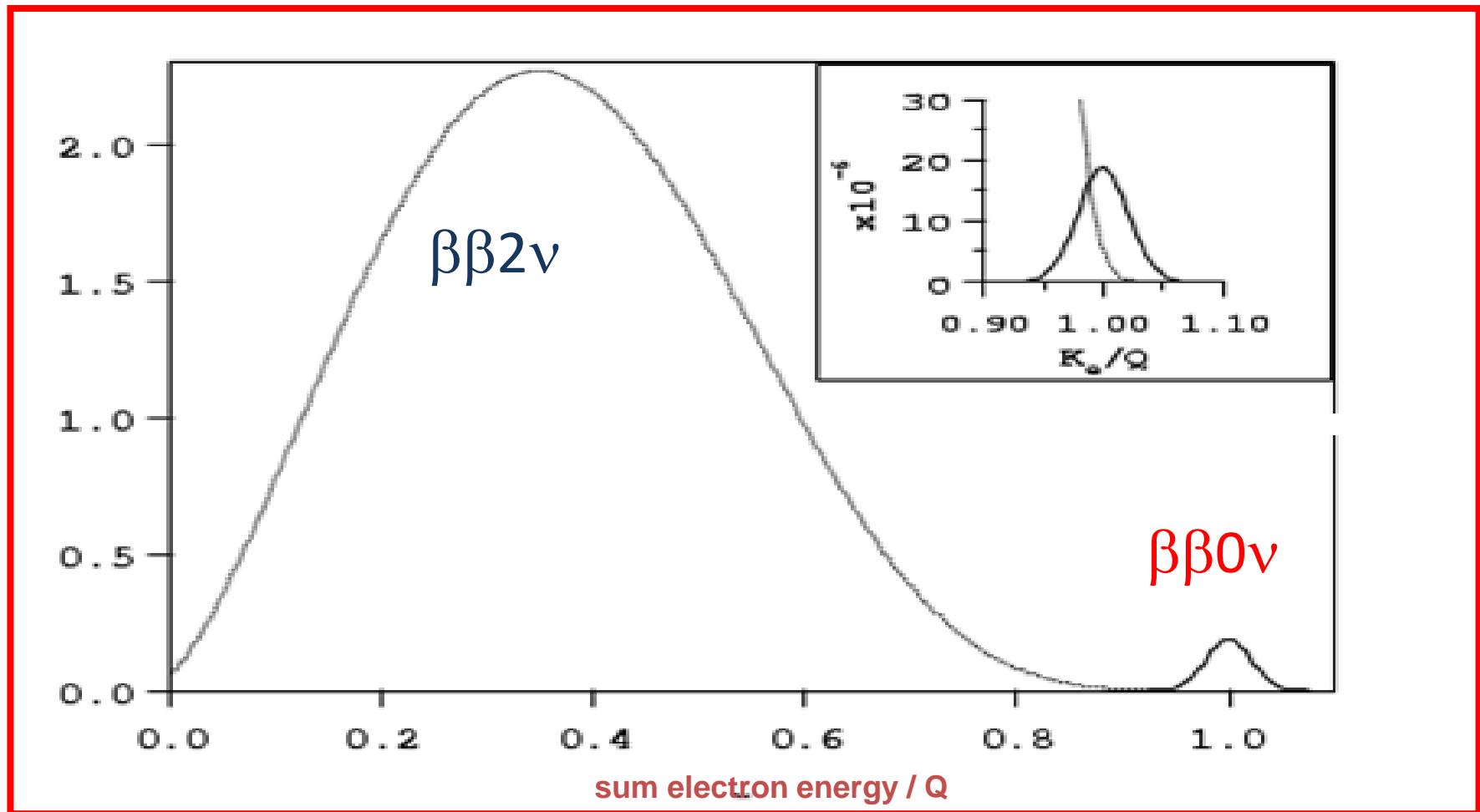
Degenerate
 $m_1 \approx m_2 \approx m_3 \gg |m_i - m_j|$

Neutrinoless double beta decay and neutrino properties

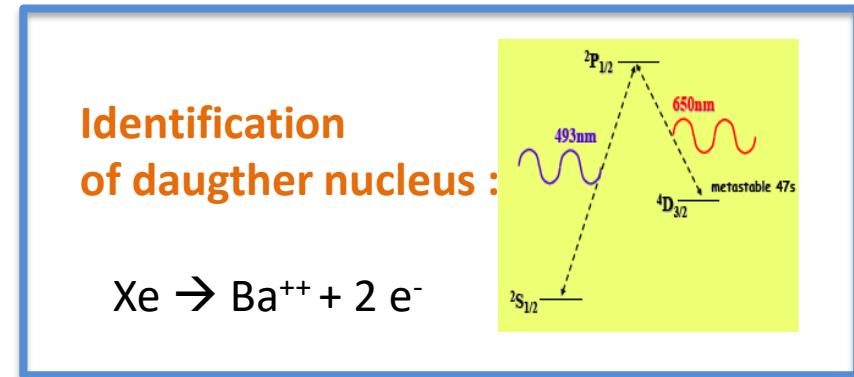
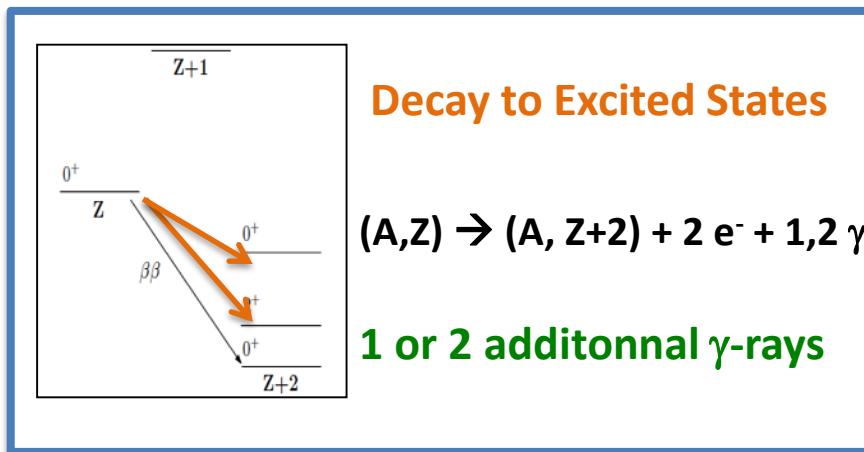
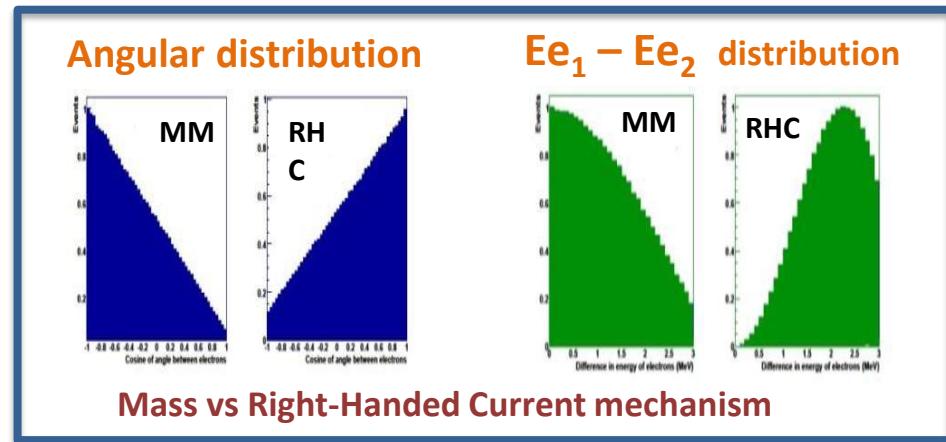
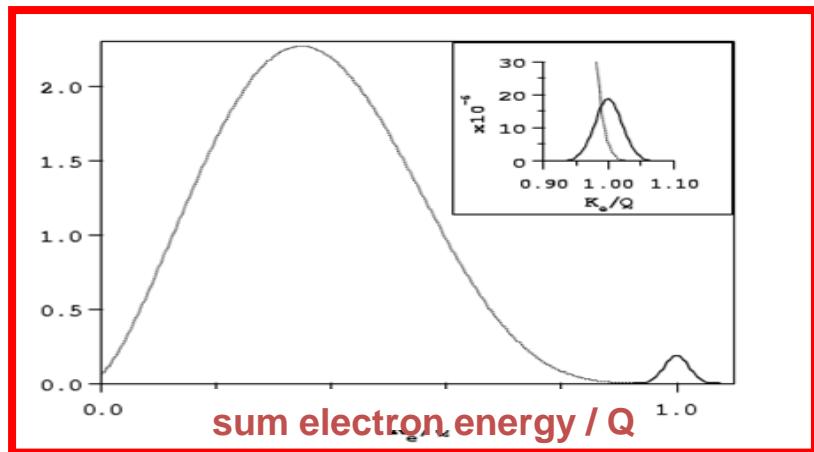
$$\langle m_\nu \rangle = \left| \sum_i U_{ei} m_i \right| = \left| \cos^2 \theta_{13} (m_1 \cos^2 \theta_{12} + m_2 e^{2ia} \sin^2 \theta_{12}) + m_3 e^{2i\beta} \sin^2 \theta_{13} \right|$$



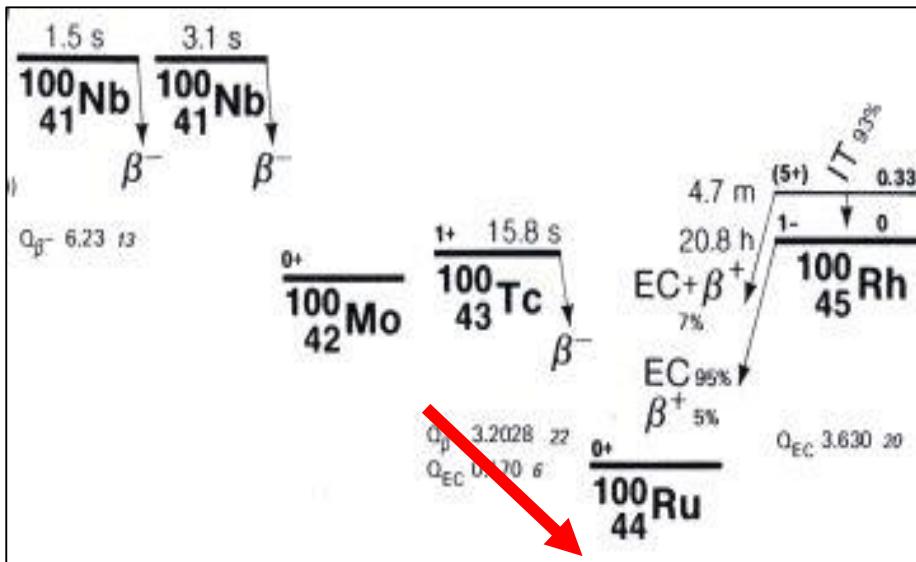
Double beta decay observables



Double beta decay observables



Double beta decay emitters



Single beta decay forbidden (energy)
or strongly suppressed by large angular
momentum change

Transition	$Q_{\beta\beta}$ (keV)	Abundance (%)
$^{146}\text{Nd} \rightarrow ^{146}\text{Sm}$	56 ± 5	17
$^{98}\text{Mo} \rightarrow ^{98}\text{Ru}$	112 ± 7	24
$^{80}\text{Se} \rightarrow ^{80}\text{Kr}$	130 ± 9	50
$^{122}\text{Sn} \rightarrow ^{122}\text{Te}$	364 ± 4	4.6
$^{204}\text{Hg} \rightarrow ^{204}\text{Pb}$	416 ± 2	7
$^{192}\text{Os} \rightarrow ^{192}\text{Pt}$	417 ± 4	41
$^{186}\text{W} \rightarrow ^{186}\text{Os}$	490 ± 2	29
$^{114}\text{Cd} \rightarrow ^{114}\text{Sn}$	534 ± 4	29
$^{170}\text{Er} \rightarrow ^{170}\text{Yd}$	654 ± 2	15
$^{134}\text{Xe} \rightarrow ^{134}\text{Ba}$	847 ± 10	10
$^{232}\text{Th} \rightarrow ^{232}\text{U}$	858 ± 6	100
$^{128}\text{Te} \rightarrow ^{128}\text{Xe}$	868 ± 4	32
$^{46}\text{Ca} \rightarrow ^{46}\text{Ti}$	987 ± 4	-
$^{70}\text{Zn} \rightarrow ^{70}\text{Ge}$	1001 ± 3	0.6
$^{198}\text{Pt} \rightarrow ^{198}\text{Hg}$	1048 ± 4	7
$^{176}\text{Yb} \rightarrow ^{176}\text{Hf}$	1079 ± 3	13
$^{238}\text{U} \rightarrow ^{238}\text{Pu}$	1145 ± 2	99
$^{94}\text{Zr} \rightarrow ^{94}\text{Mo}$	1145 ± 2	17
$^{154}\text{Sm} \rightarrow ^{154}\text{Gd}$	1252 ± 2	23
$^{86}\text{Kr} \rightarrow ^{86}\text{Sr}$	1256 ± 5	17
$^{104}\text{Ru} \rightarrow ^{104}\text{Pd}$	1299 ± 4	19
$^{142}\text{Ce} \rightarrow ^{142}\text{Nd}$	1418 ± 3	11
$^{160}\text{Gd} \rightarrow ^{160}\text{Dy}$	1729 ± 1	22
$^{148}\text{Nd} \rightarrow ^{148}\text{Sm}$	1928 ± 2	6
$^{110}\text{Pd} \rightarrow ^{110}\text{Cd}$	2013 ± 19	12
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	2040 ± 1	8
$^{124}\text{Sn} \rightarrow ^{124}\text{Te}$	2288 ± 2	6
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	2479 ± 8	9
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	2533 ± 4	34
$^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$	2802 ± 4	7
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	2995 ± 6	9
$^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$	3034 ± 6	10
$^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$	3350 ± 3	3
$^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$	3667 ± 2	6
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	4271 ± 4	0.2

35 $\beta\beta$ emitters but only about 10 can be experimentally studied

Expected half-lifes

<i>Isotope</i>	<i>Q-value (keV)</i>	<i>Nat. abund. (%)</i>	<i>(PS 0v)⁻¹ (yrs x eV²)</i>	<i>(PS 2v)⁻¹ (yrs)</i>
Ca 48	4271	0.187	4.10E24	2.52E16
Ge 76	2039	7.8	4.09E25	7.66E18
Se 82	2995	9.2	9.27E24	2.30E17
Zr 96	3350	2.8	4.46E24	5.19E16
Mo 100	3034	9.6	5.70E24	1.06E17
Pd 110	2013	11.8	1.86E25	2.51E18
Cd 116	2802	7.5	5.28E24	1.25E17
Sn 124	2288	5.64	9.48E24	5.93E17
Te 130	2529	34.5	5.89E24	2.08E17
Xe 136	2479	8.9	5.52E24	2.07E17
Nd 150	3367	5.6	1.25E24	8.41E15

$$T_{1/2} = \ln 2 \cdot a \cdot N_A \cdot M \cdot t / N_{\beta\beta}$$

1 decay/y for $10^{24} - 10^{25}$ nuclei
 1 decay/y for ~ 10 moles (1 kg)

a: isotopic abundance

N_A : Avogadro number

M: mass

T: time

$N_{\beta\beta}$: number of decays

Basic principle for a neutrinoless double beta decay experiment

$$\left(T_{1/2}^{0n}\right)^{-1} = G^{0n} \left|M^{0n}\right|^2 \frac{\alpha \langle m_n \rangle^2}{\beta \frac{m_e}{\theta}}$$

G^{0n} : Phase space factor function of $Q_{\beta\beta}^{-5}$ and Z

M^{0n} : Nuclear Matrix Element

$\langle m_n \rangle$ = effective neutrino mass

Expected half-life $> 10^{25}$ years \rightarrow High number of nuclei \rightarrow isotopic enrichment

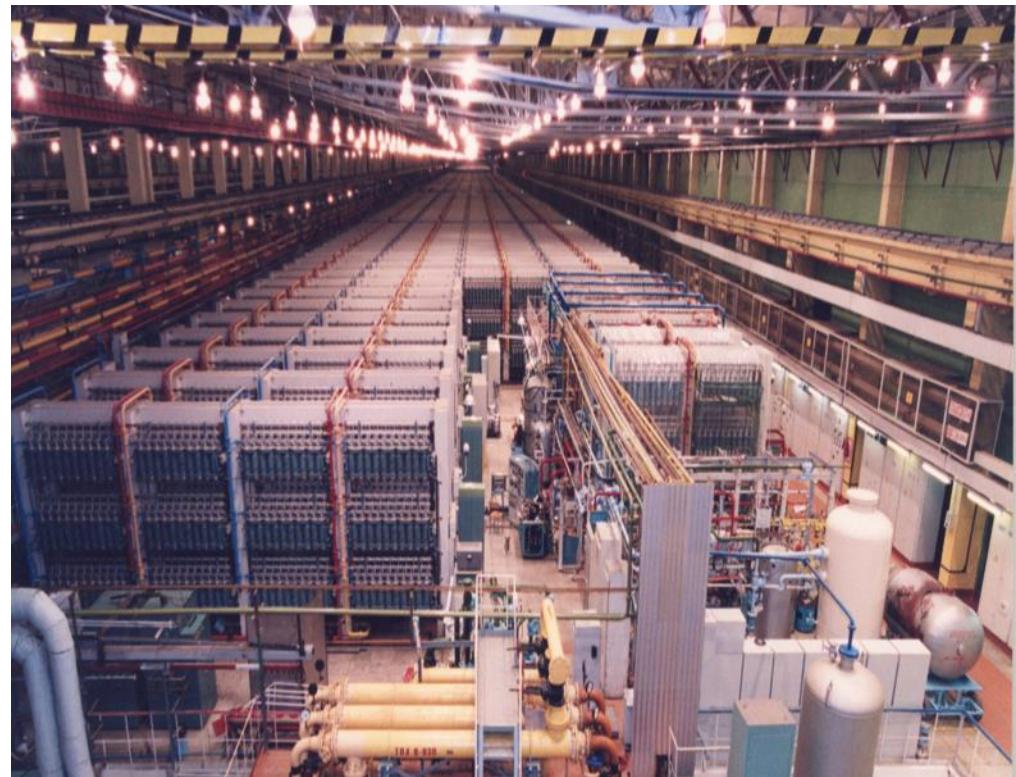
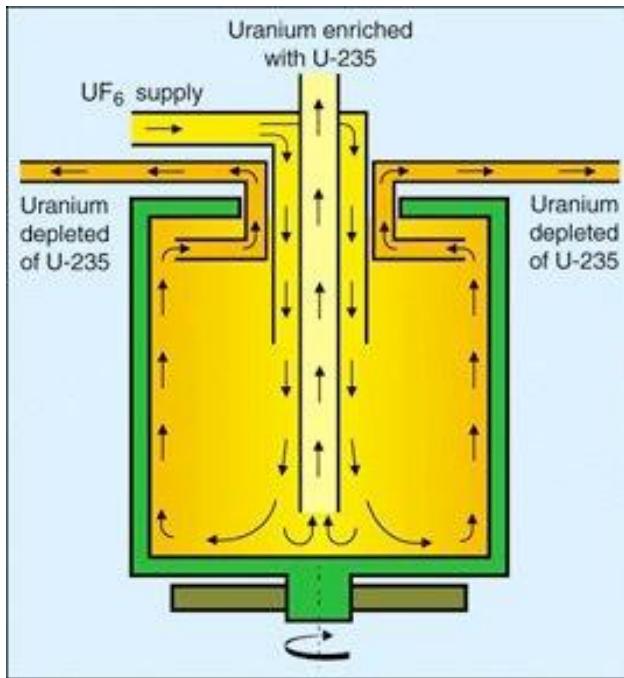
High transition energy ($Q_{\beta\beta}$)

Good energy resolution

Rejection of background coming from natural radioactivity

Choice of the nucleus \rightarrow experimental technique

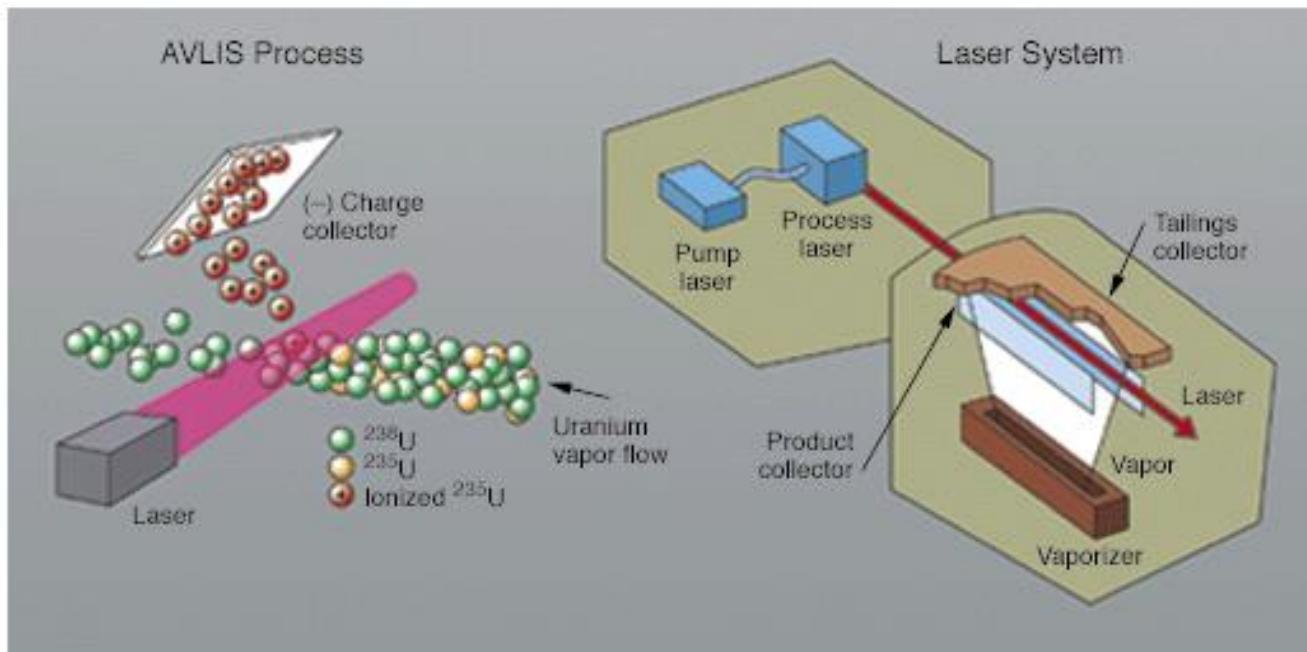
Isotopic enrichment



**ECP (Electro-Chemical Plant, Svetlana)
Zelenogorsk (Siberia)**

**Enrichment mainly made by centrifugation: need gaseous form for the isotope
 ^{136}Xe , ^{100}Mo , ^{82}Se , ^{76}Ge ,**

Isotopic enrichment



Enrichment ^{48}Ca , ^{150}Nd , ^{96}Zr possible in principle



Measured experimental half-life

$$T_{1/2}^{0\nu}(y) \propto \frac{\varepsilon}{A} M \cdot t$$

NO Background

M: masse (g)

ε : efficiency

$k_{C.L.}$: Confidence level

N_A : Avogadro number

t: time (y)

N_{Bckg} : Background events ($\text{keV}^{-1} \cdot \text{g}^{-1} \cdot \text{y}^{-1}$)

ΔE : energy resolution (keV)

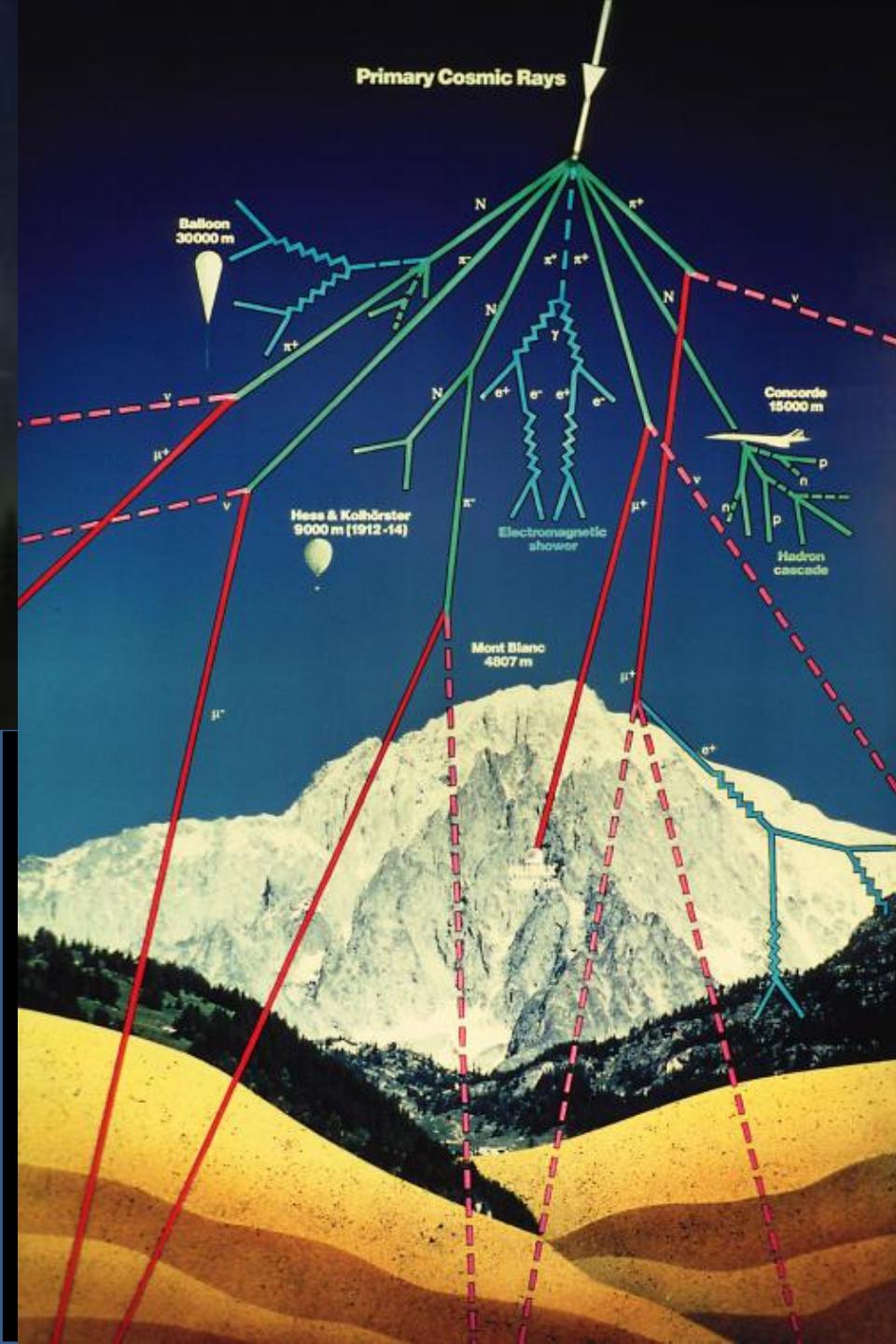
$$T_{1/2}^{0\nu}(y) > \frac{\ln 2 \cdot N_A}{k_{C.L.}} \cdot \frac{\varepsilon}{A} \cdot \sqrt{\frac{M \cdot t}{N_{Bckg} \cdot \Delta E}}$$

With background

Source of background from natural radioactivity

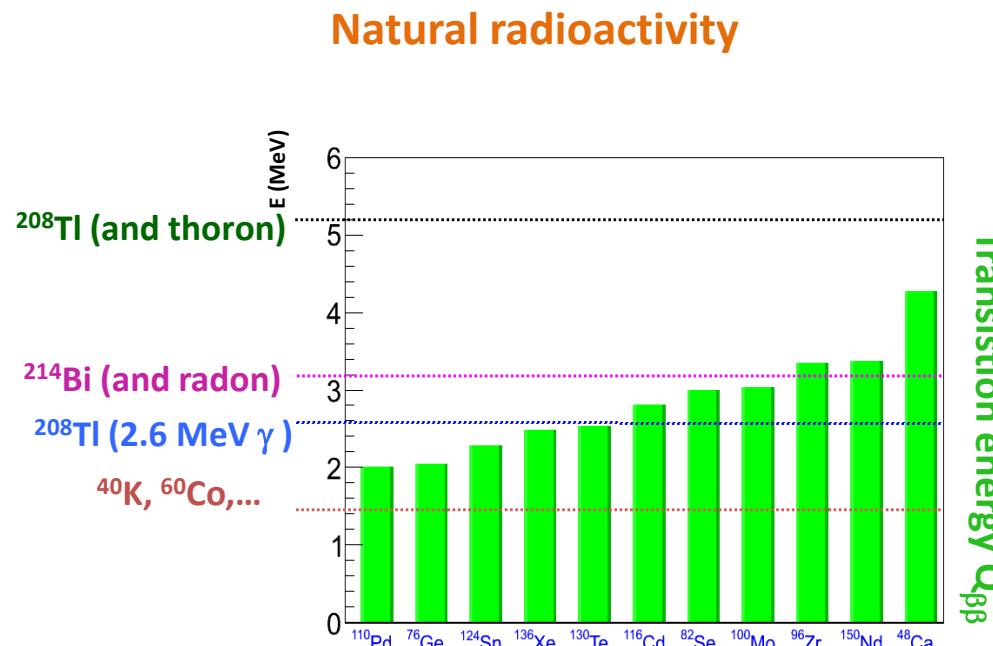
Such experiment cannot be performed at the sea level because of cosmic rays





Source of background from natural radioactivity

The radiations from the natural radioactivity can mimic double beta decay when they interact inside the detectors

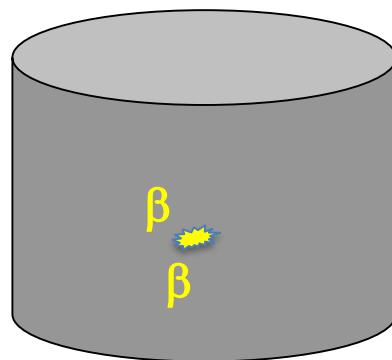


Detectors installed underground
Selection of all materials used in the detectors
Shielding against gamma-ray from the rocks
Suppression of radon

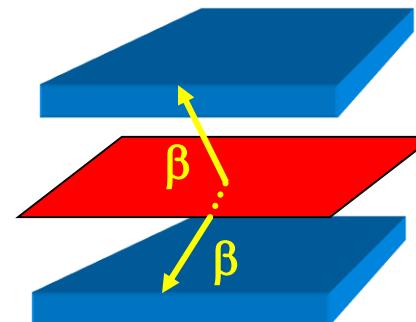
Source of background from natural radioactivity

Different strategies are possible to minimize the background

Detector: very accurate measurement of the energy to see the peak
or detection of the two emitted neutrino to reduce background

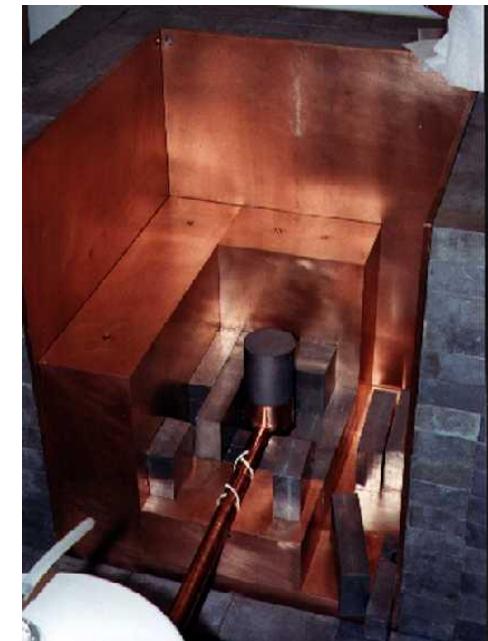
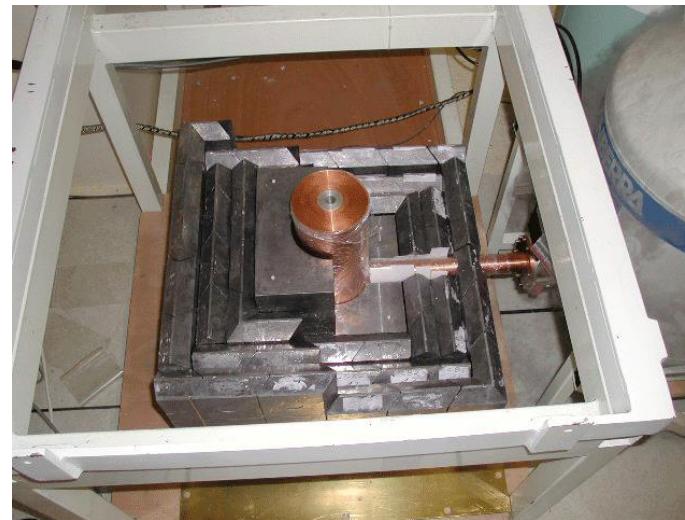
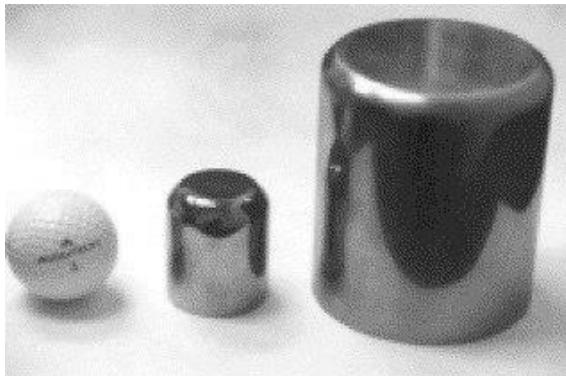


Calorimetric measurement



Electron detection

Ge experiment: Heidelberg Moscow

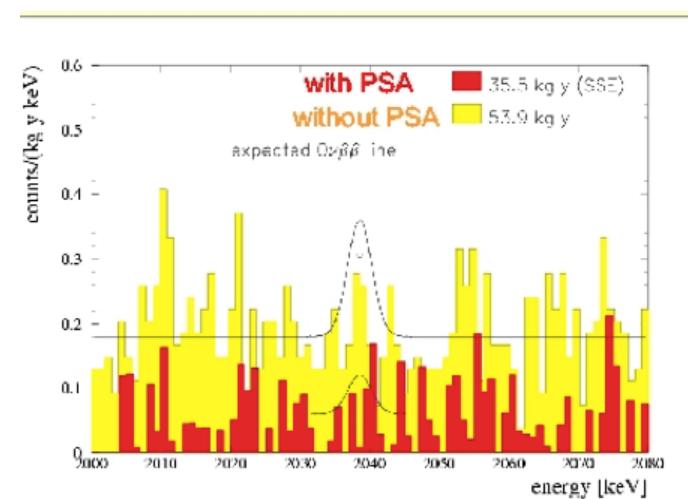


Ge detector works as semi-conductor at the liquid nitrogen temperature (-172° C)

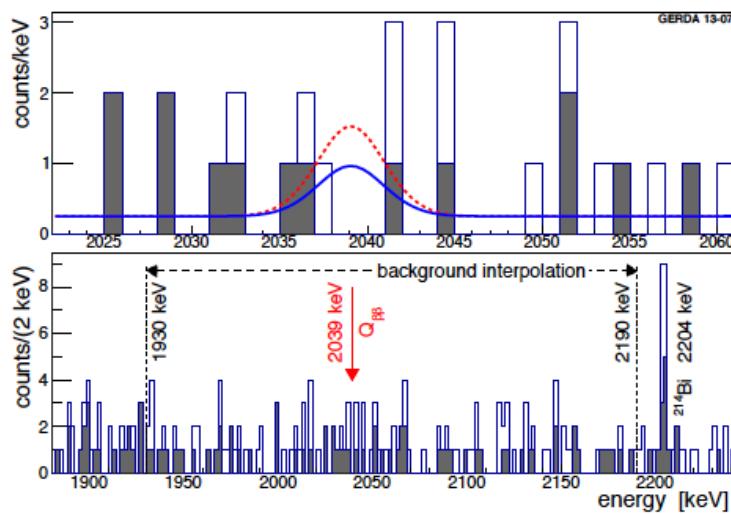
Very good energy resolution

$$T_{1/2} > 1.9 \cdot 10^{25} \text{ yr}$$

$$\langle m_\nu \rangle < 0.2 - 0.5 \text{ eV}$$



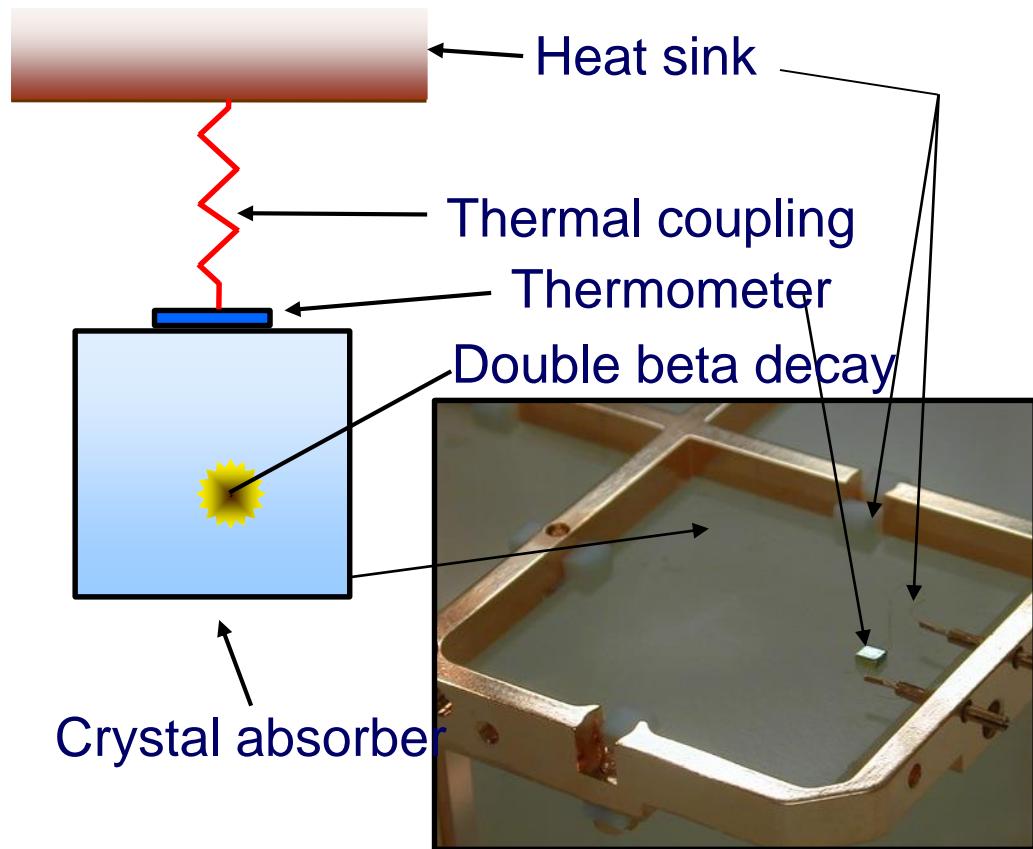
Ge experiment: GERDA experiment



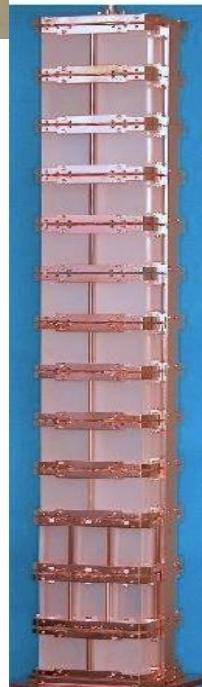
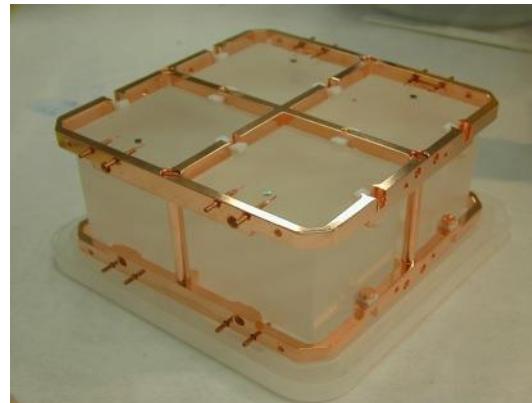
$T_{1/2} > 3 \cdot 10^{25} \text{ yr}$

$\langle m_\nu \rangle < 0.2 - 0.4 \text{ eV}$

Bolometers : Cuoricino experiment



Very good energy resolution



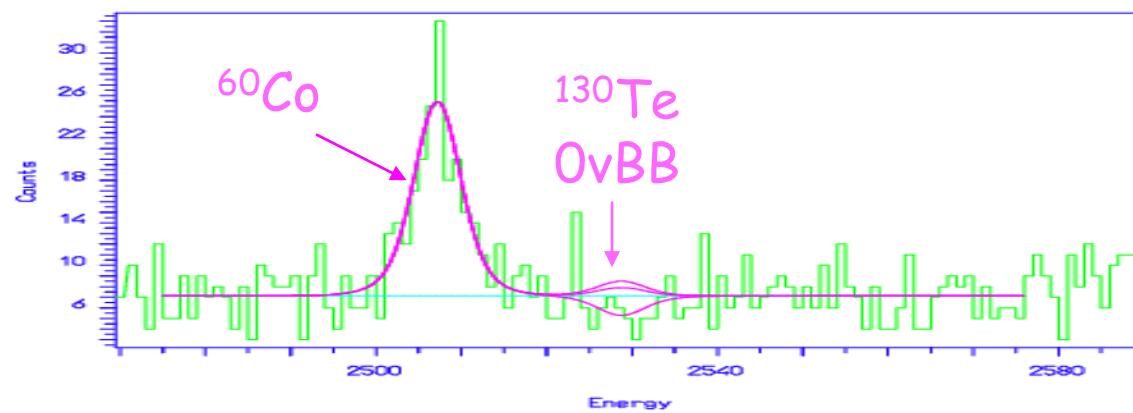
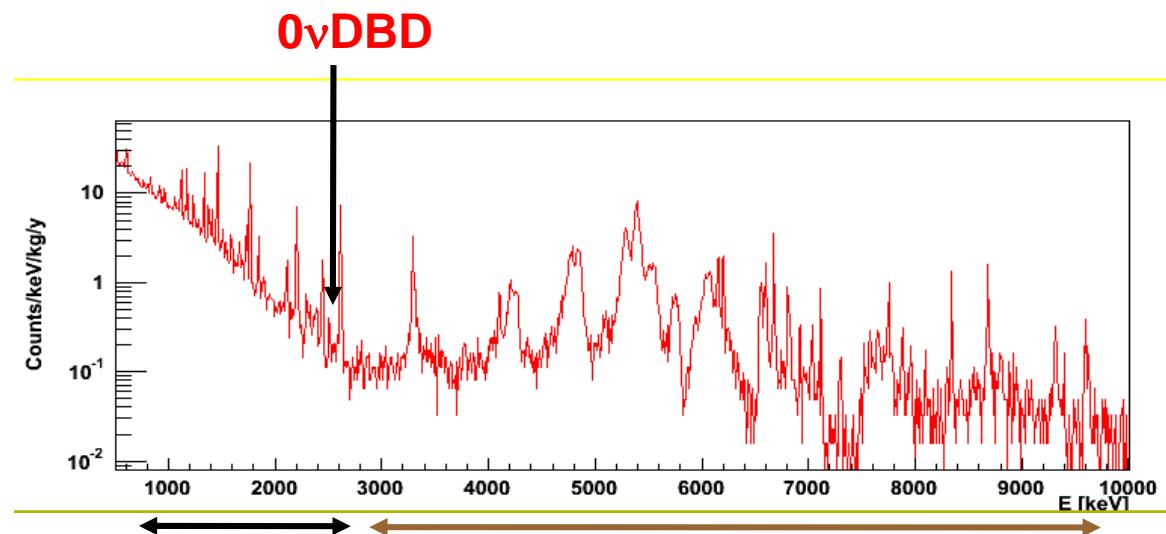
example: 750 g of TeO_2 @ 10 mK

$$C \sim T^3 \text{ (Debye)} \Rightarrow C \sim 2 \times 10^{-9} \text{ J/K}$$

$$1 \text{ MeV } \gamma\text{-ray} \Rightarrow \Delta T \sim 80 \mu\text{K}$$

$$\Rightarrow \Delta U \sim 10 \text{ eV}$$

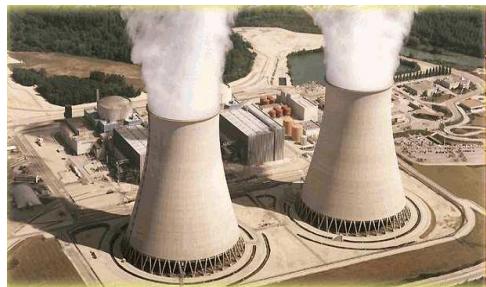
Bolometers : Cuoricino experiment



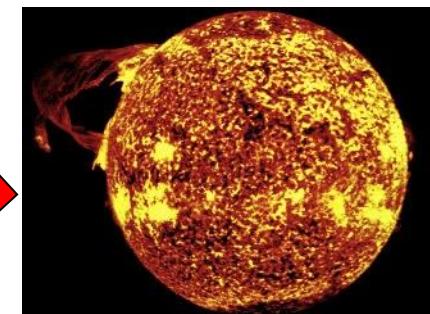
$T_{1/2} > 6 \cdot 10^{24} \text{ yr}$

$\langle m_\nu \rangle < 0.1 - 0.7 \text{ eV}$

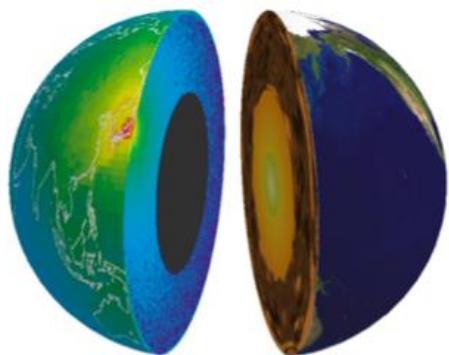
Large liquid scintillator experiment: KamLAND-ZEN



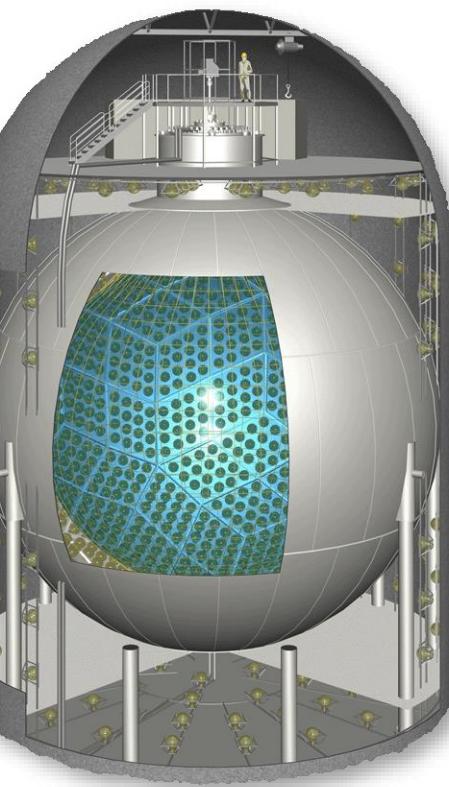
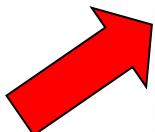
Reactors



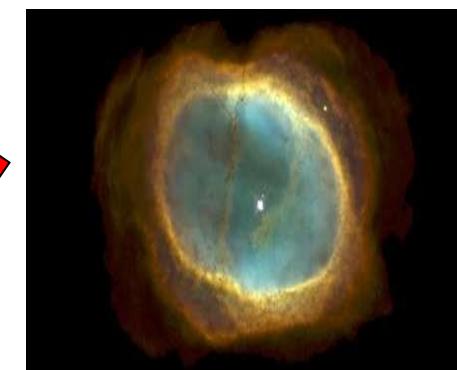
Solar neutrinos



Geoneutrinos

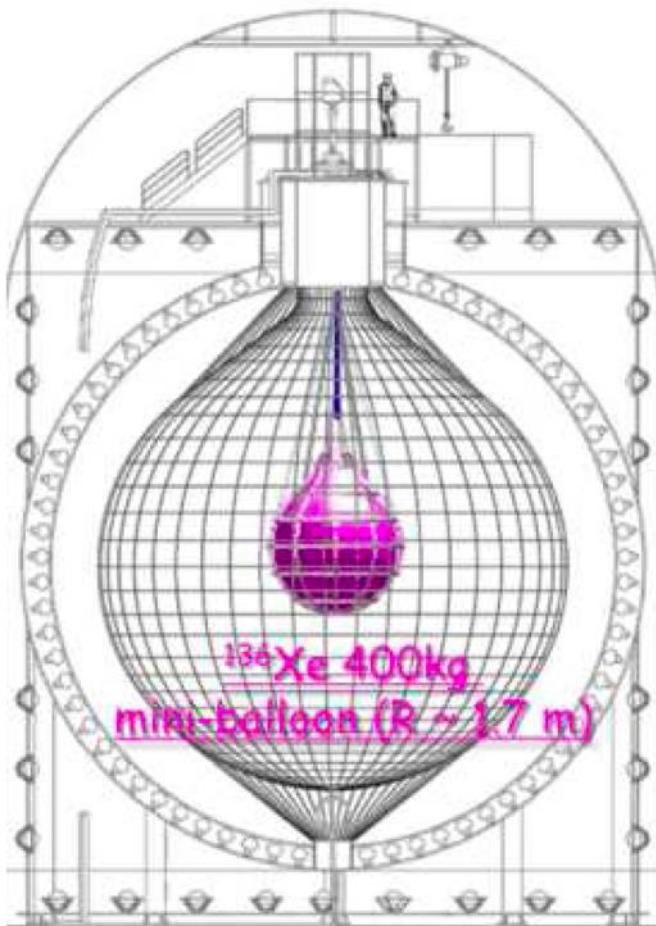


KamLAND detector



Supernovae neutrinos

Large liquid scintillator experiment: KamLAND-ZEN

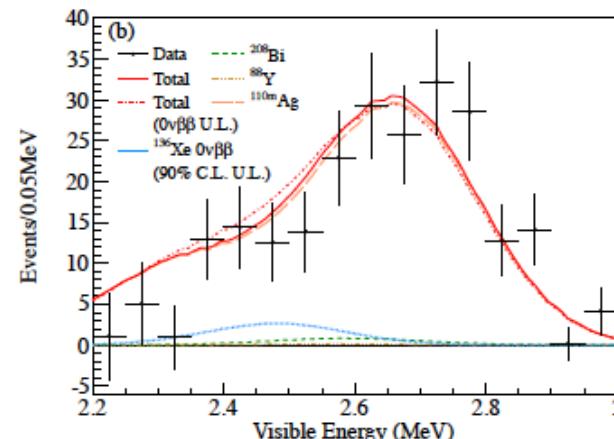
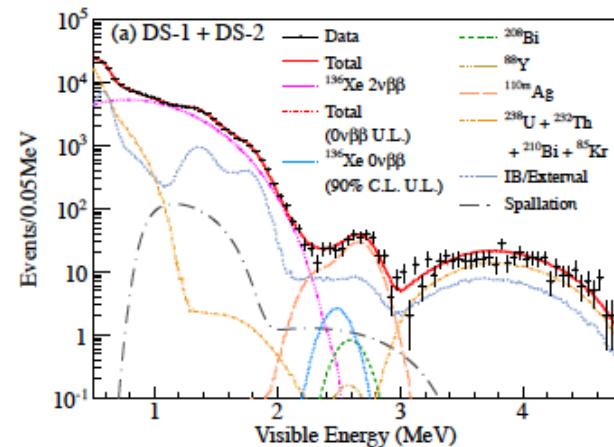


$T_{1/2} > 2.0 \cdot 10^{25}$ yr

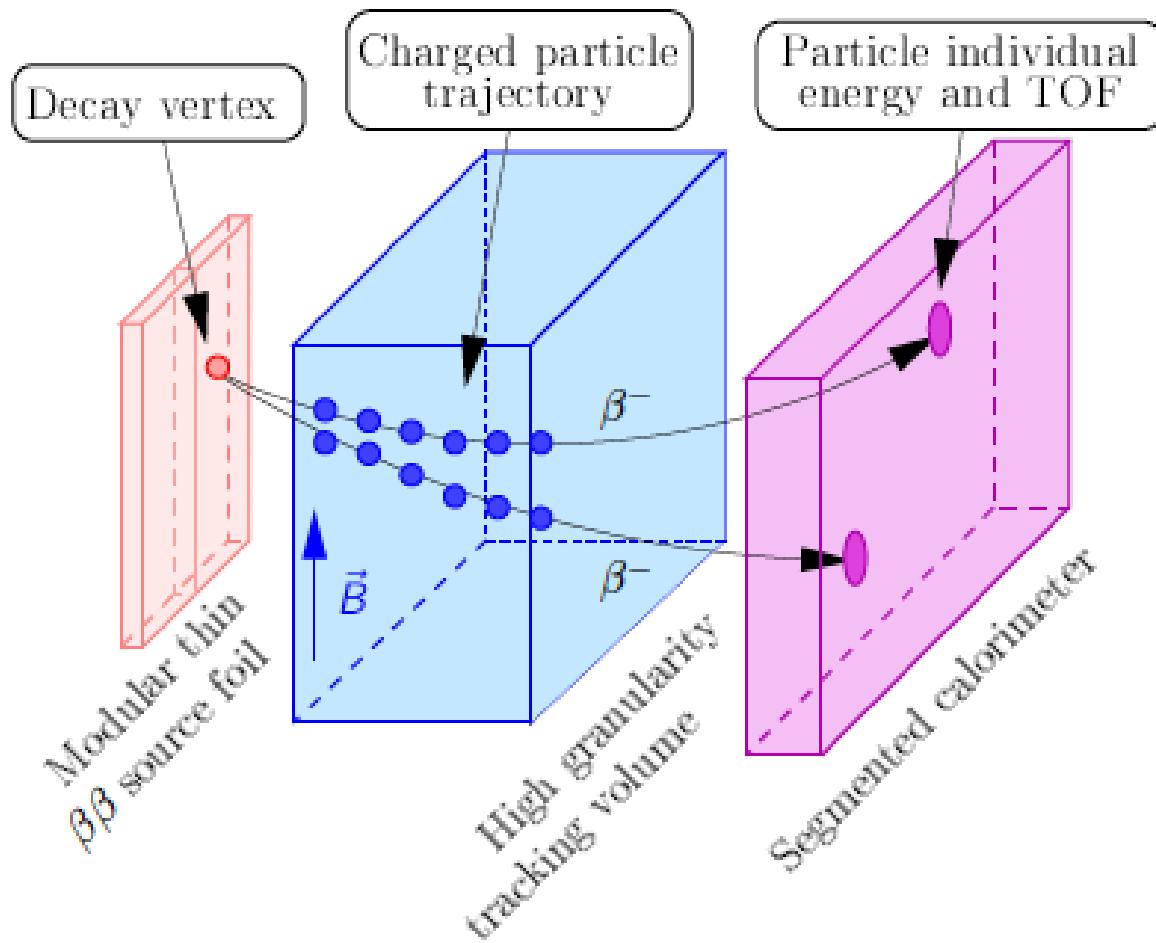
$\langle m_\nu \rangle < 0.2 - 0.3$ eV

Dissolution of ^{136}Xe inside a balloon of liquid scintillator

Possibility to dissolve very large mass

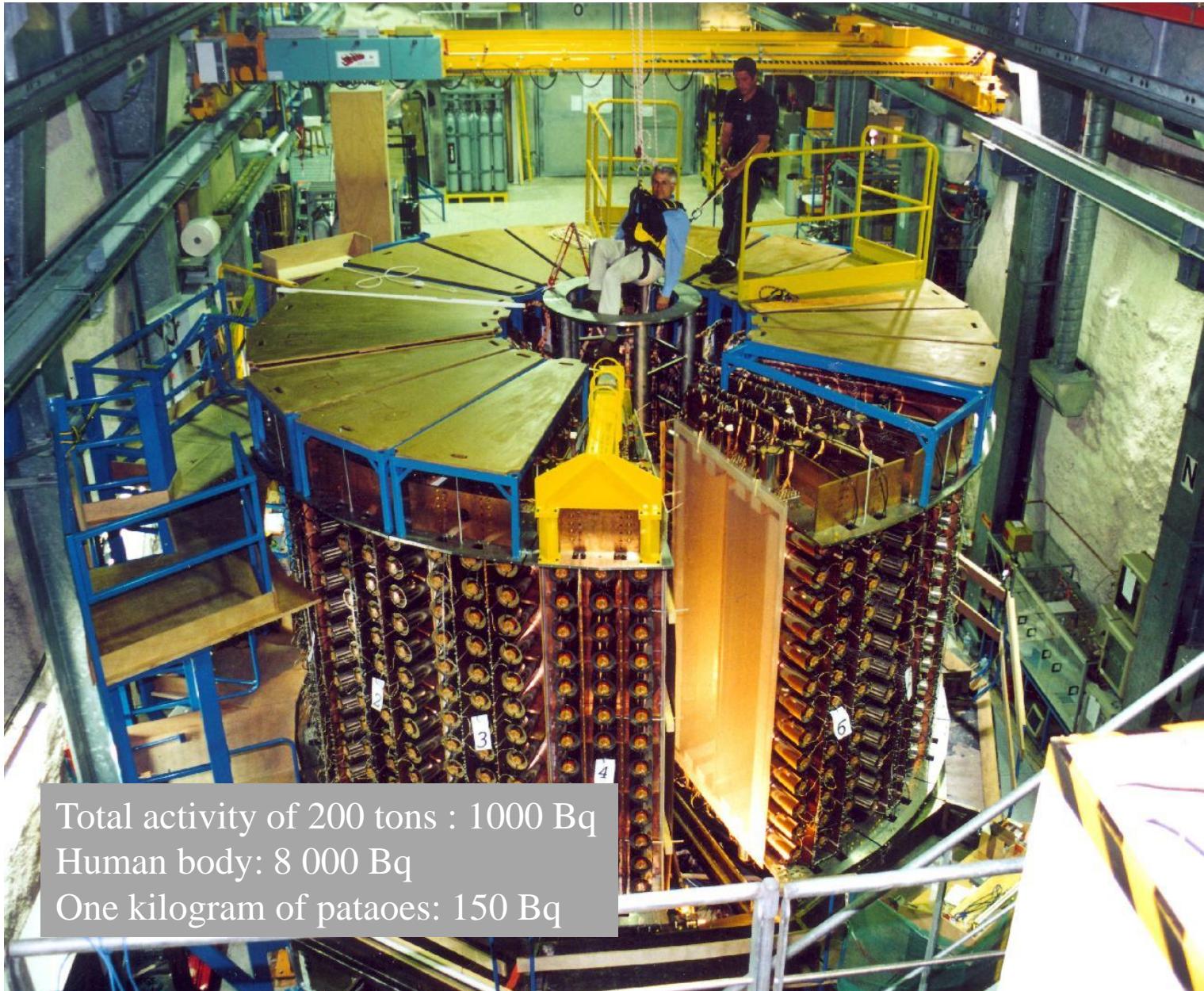


Principle of experiments with electron detection

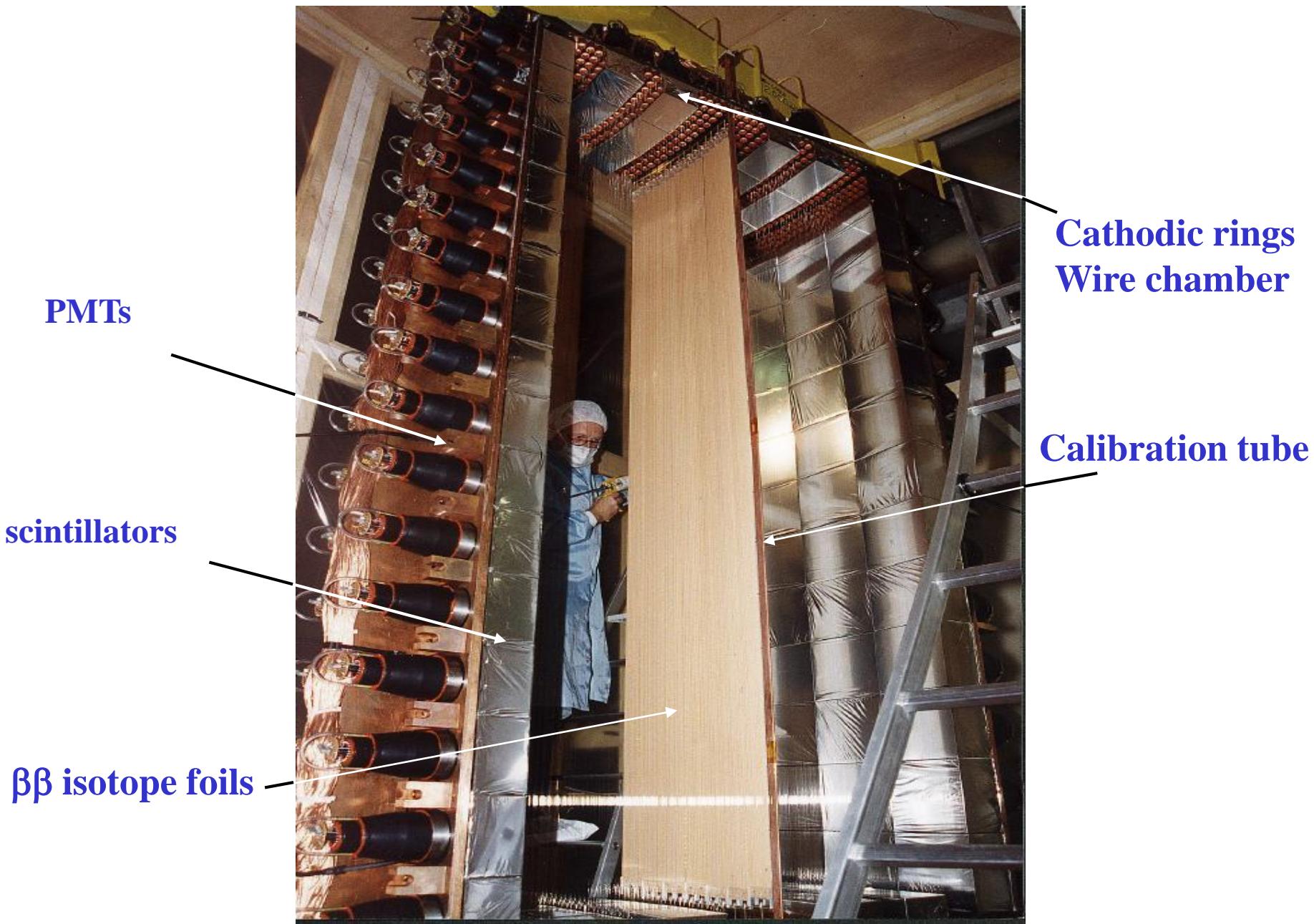


Multi-isotope detector
High rejection of background

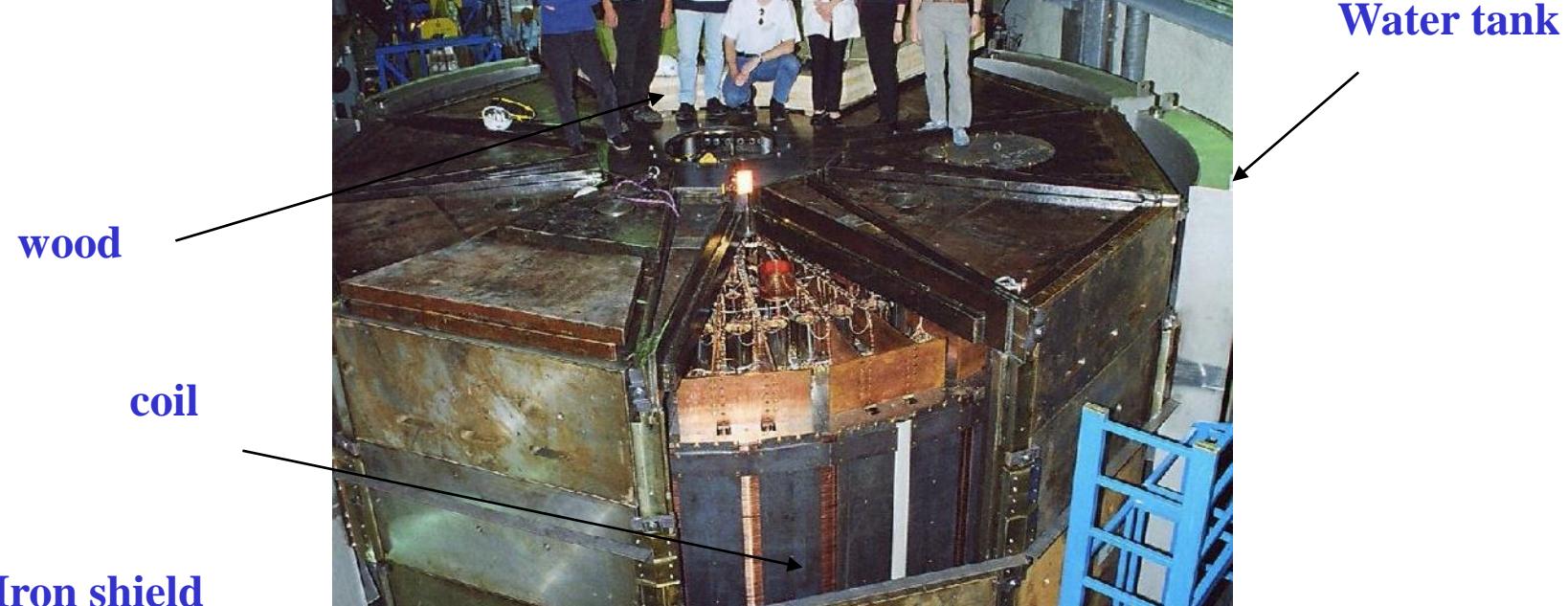
The NEMO3 detector



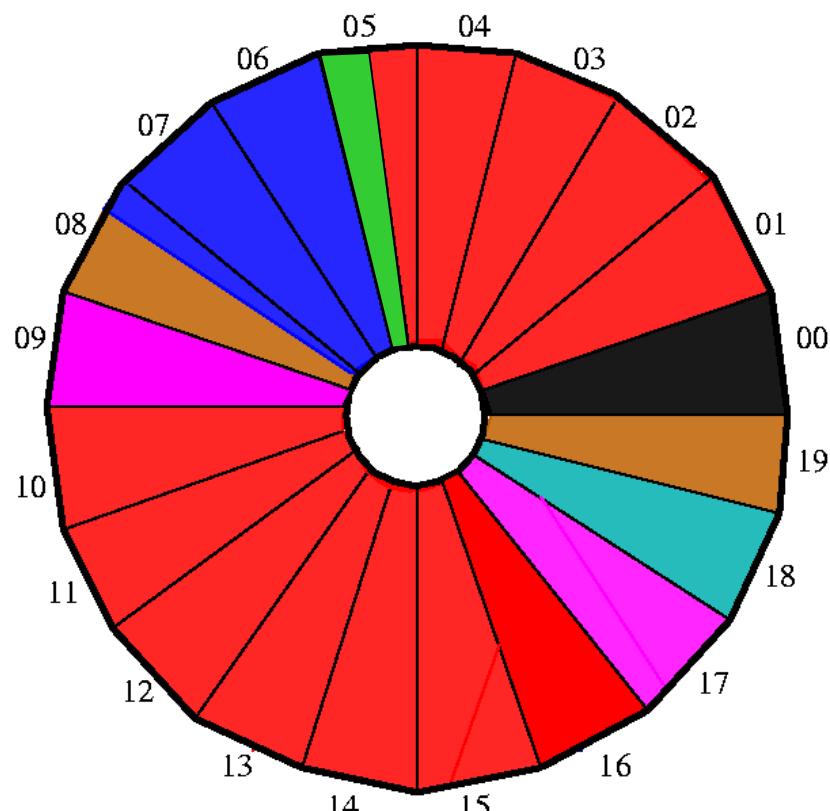
The NEMO3 detector



The NEMO3 detector



NEMO3 isotopes



^{100}Mo 6.914 kg
 $Q_{\beta\beta} = 3034 \text{ keV}$

^{82}Se 0.932 kg
 $Q_{\beta\beta} = 2995 \text{ keV}$

$\beta\beta0\nu$ search

$\beta\beta2\nu$ measurement

^{116}Cd 405 g

$Q_{\beta\beta} = 2805 \text{ keV}$

^{96}Zr 9.4 g

$Q_{\beta\beta} = 3350 \text{ keV}$

^{150}Nd 37.0 g

$Q_{\beta\beta} = 3367 \text{ keV}$

^{48}Ca 7.0 g

$Q_{\beta\beta} = 4272 \text{ keV}$

^{130}Te 454 g

$Q_{\beta\beta} = 2529 \text{ keV}$

$^{\text{nat}}\text{Te}$ 491 g

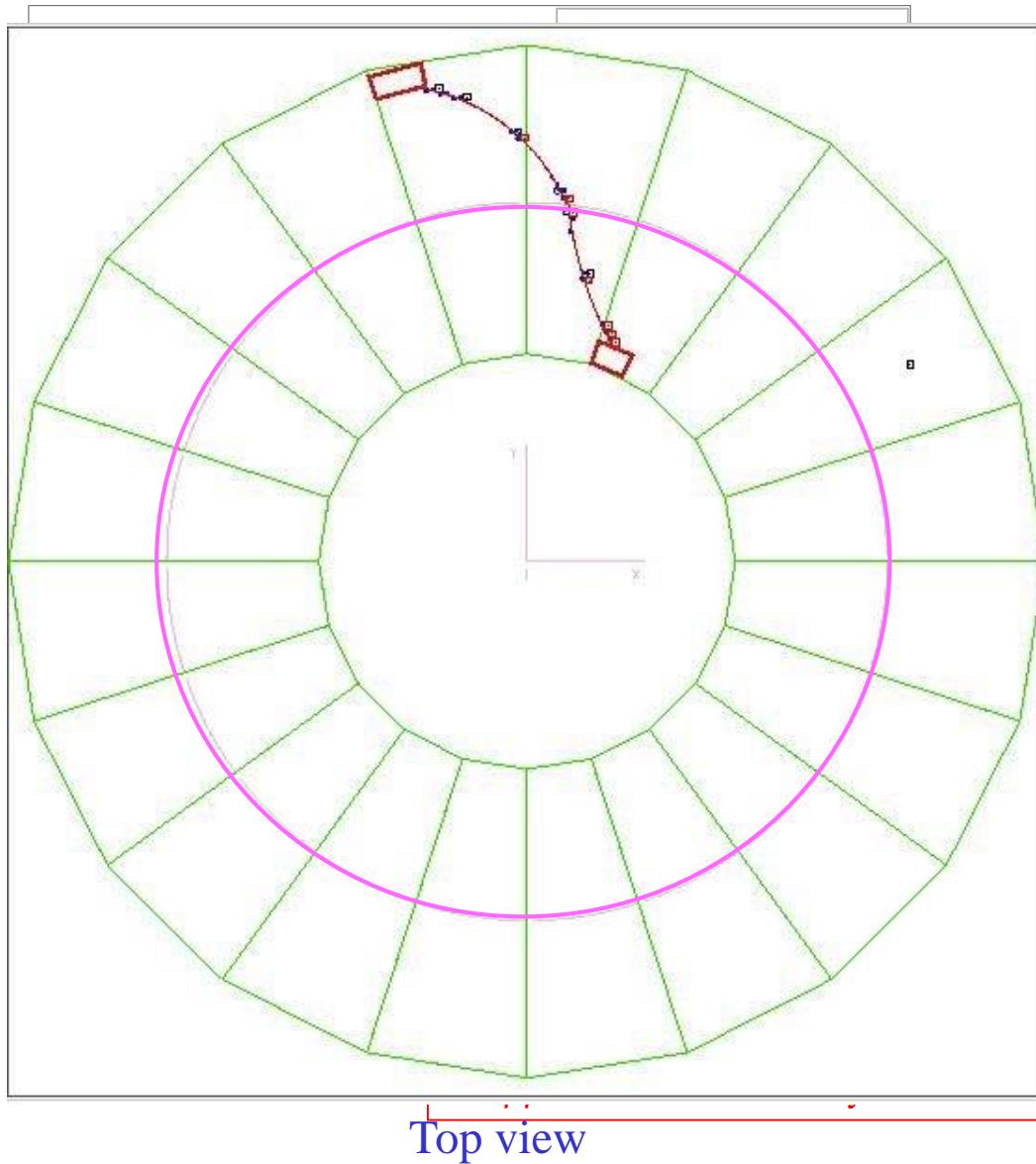
Cu 621 g

**External bkg
measurement**

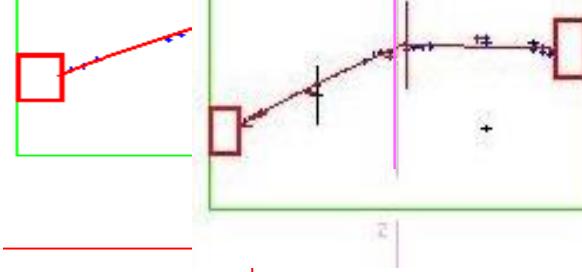
(All enriched isotopes produced in Russia)

$\beta\beta$ events selection in NEMO-3

Typical $\beta\beta 2\nu$ event observed from ^{100}Mo



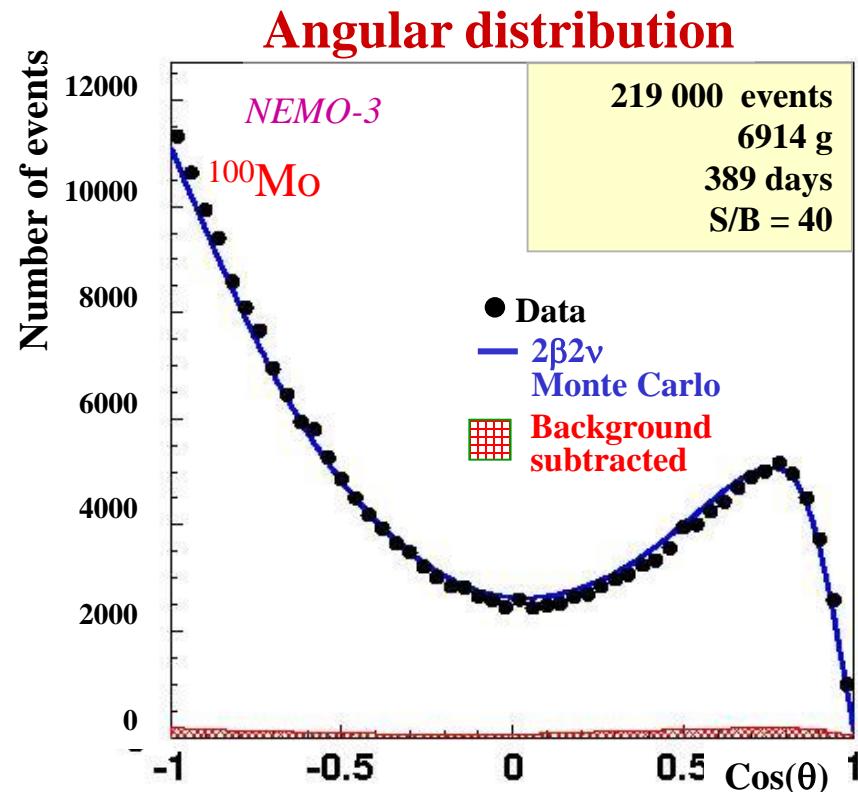
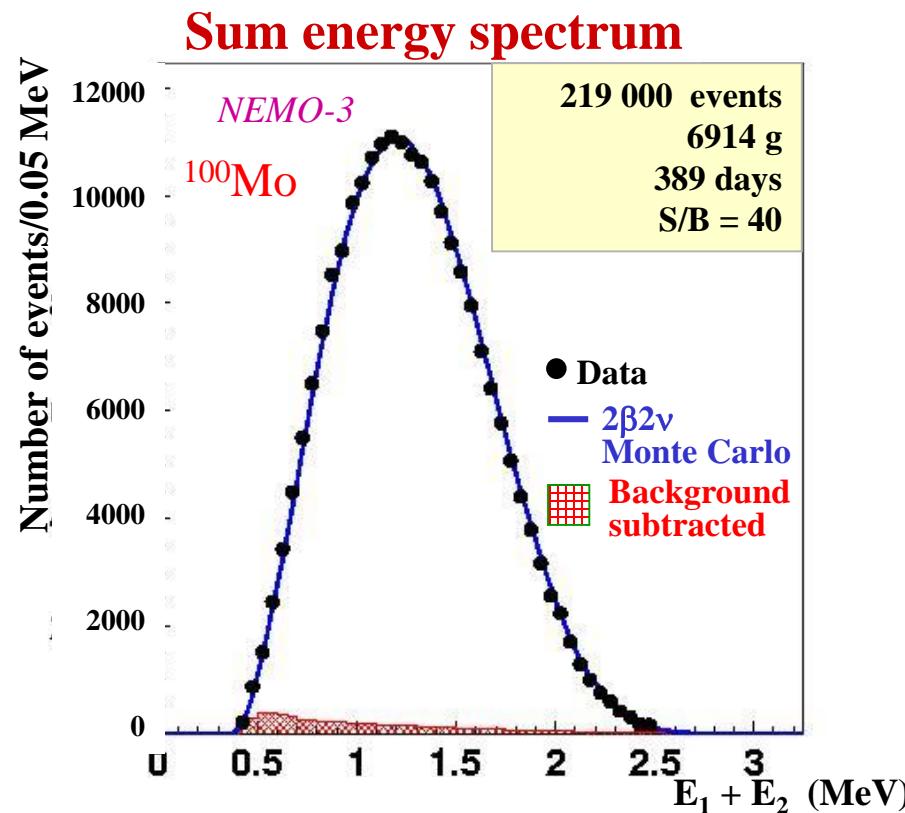
Longitude
view



Side view

(nr layers + 1)

NEMO3 results



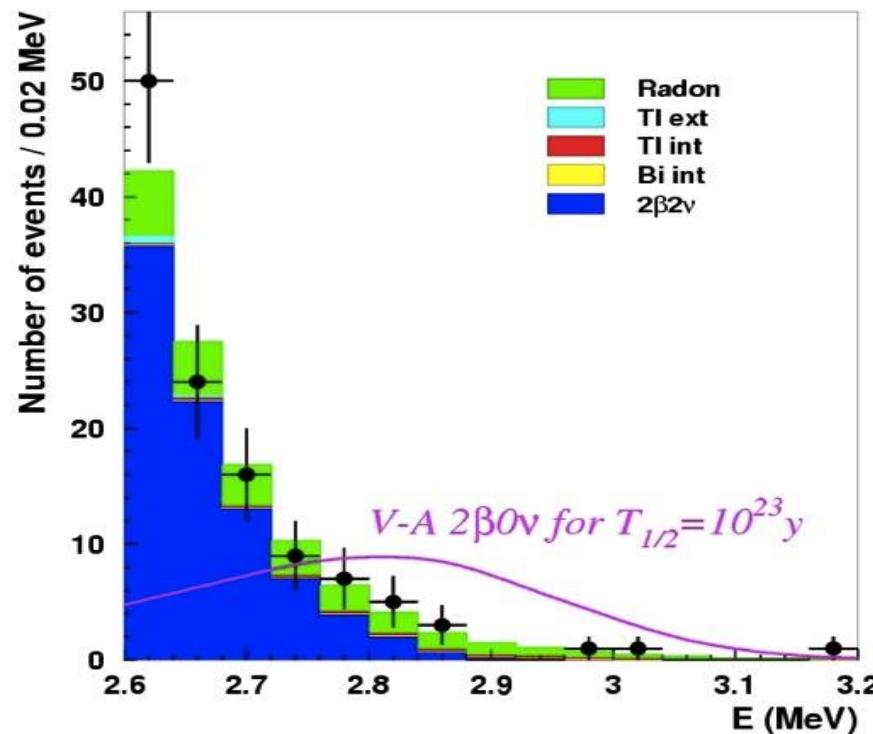
$T_{1/2}(\beta\beta 2\nu) = 7.11 \pm 0.02 \text{ (stat)} \pm 0.54 \text{ (syst)} \times 10^{18}$
years

Phys. Rev. Lett. 95 182302 (2005)

« $\beta\beta$ factory» → tool for precision test

100Mo

Phase I + II
693 days

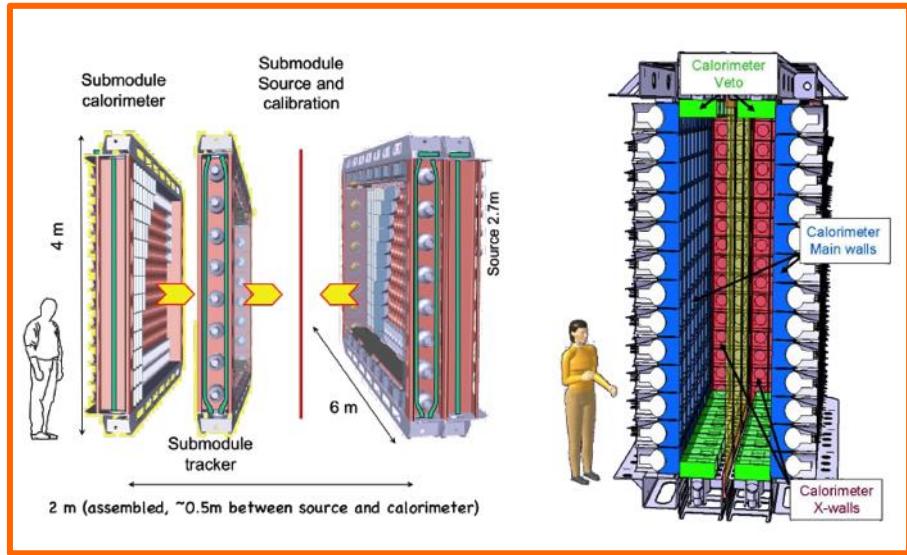


$$T_{1/2} > 1.0 \cdot 10^{24} \text{ yr}$$

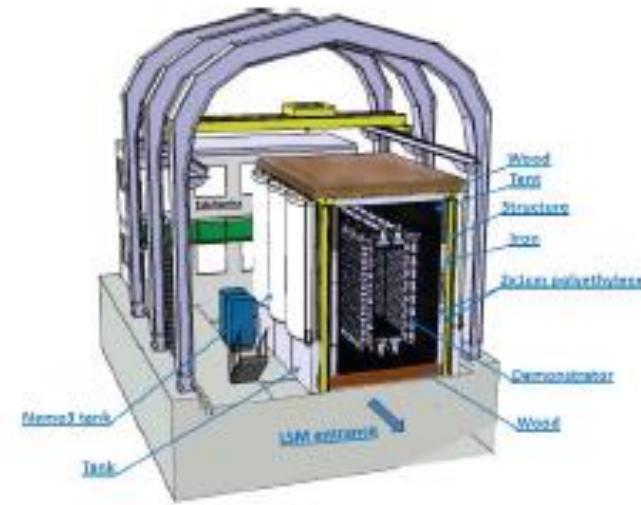
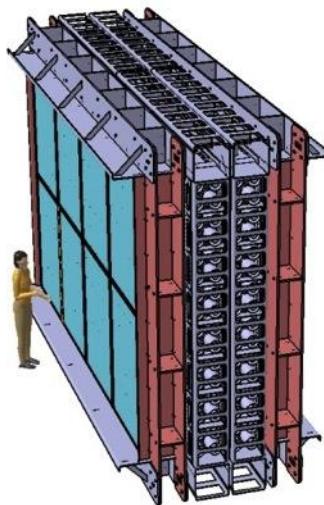
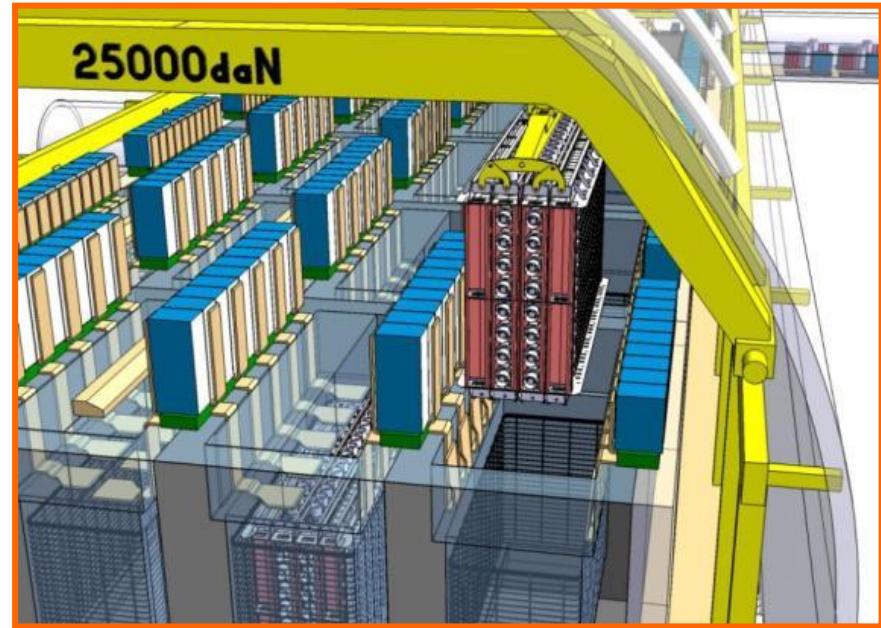
$$\langle m_\nu \rangle < 0.3 - 0.7 \text{ eV}$$

SuperNEMO project

A module



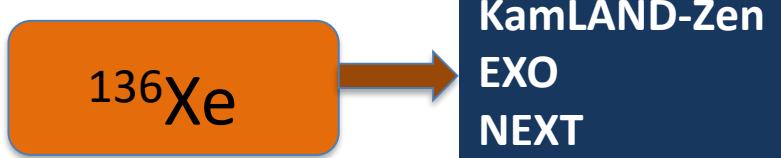
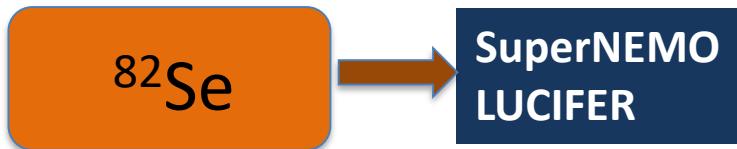
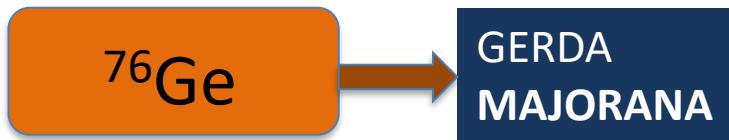
20 modules



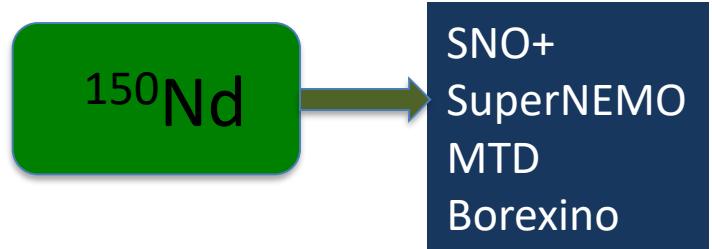
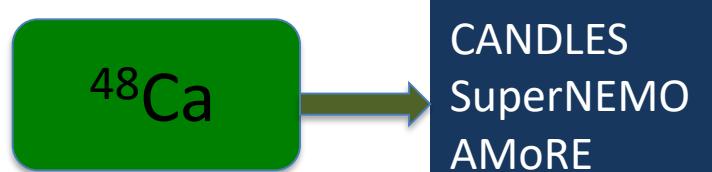
Latest results

Experiment	isotope	Mass (kg)	Half-life limit in years	Neutrino mass limit in eV
H.M.	^{76}Ge	14	$1.9 \cdot 10^{25}$	0.21 - 0.53
GERDA	^{76}Ge	14	$1.9 \cdot 10^{25}$	0.20 - 0.40
Cuoricino	^{130}Te	12	$2.8 \cdot 10^{24}$	0.27 – 0.57
NEMO3	^{100}Mo	7	$1.0 \cdot 10^{24}$	0.31 – 0.79
EXO-200	^{136}Xe	200	$1.6 \cdot 10^{25}$	0.14 – 0.38
Kamland-Zen	^{136}Xe	400	$6.2 \cdot 10^{24}$	0.26 – 0.54

Present experiments or projects



A dream ?

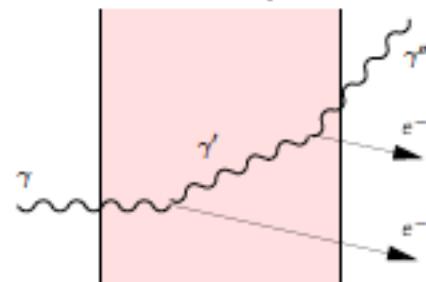


Summary

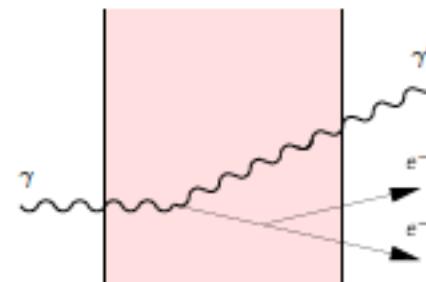
- ◆ The search of neutrinoless double beta decay is one of most important question in particle physics:
 - Neutrino nature
 - Neutrino mass
- ◆ The experimental search is a real challenge to reduce background
- ◆ Present sensitivity on neutrino mass $< 0.2 - 0.4 \text{ eV}$ with 10 kg (or 400 kg of ^{136}Xe)
- ◆ Next generation 100 kg should allow to reach $\langle m_\nu \rangle < 0.05 \text{ eV}$
- ◆ New ideas required for higher mass (1 ton)

Background from natural radioactivity

External (γ flux):



double
Compton

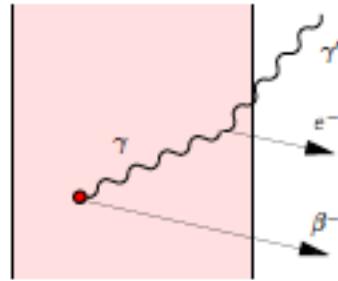


Compton+
Möller

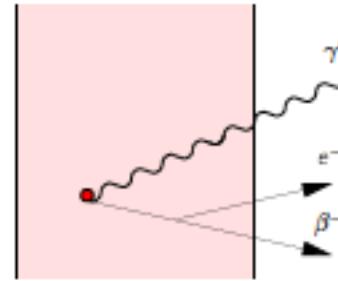


pair
production

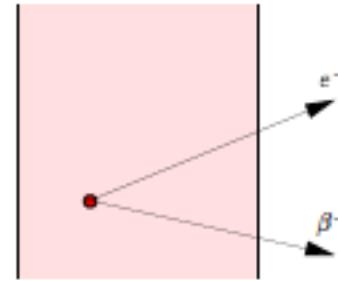
Internal (source foil contaminants):



$\beta^- +$
Compton



$\beta^- +$
Möller



$\beta^- +$
IC

Piège à neutrino

← 30 000 000 000 000 km de plomb →



Quelles interactions peut avoir le neutrino ?



Pour détecter des neutrinos: beaucoup de neutrinos et beaucoup de matière (noyau) !

Neutrinoless double beta decay

$$\left(T_{1/2}^{0n}\right)^{-1} = G^{0n} \left|M^{0n}\right|^2 \frac{\alpha}{\beta} \frac{\langle m_n \rangle \bar{0}^2}{m_e \emptyset}$$

High $Q_{\beta\beta}$ and high Z

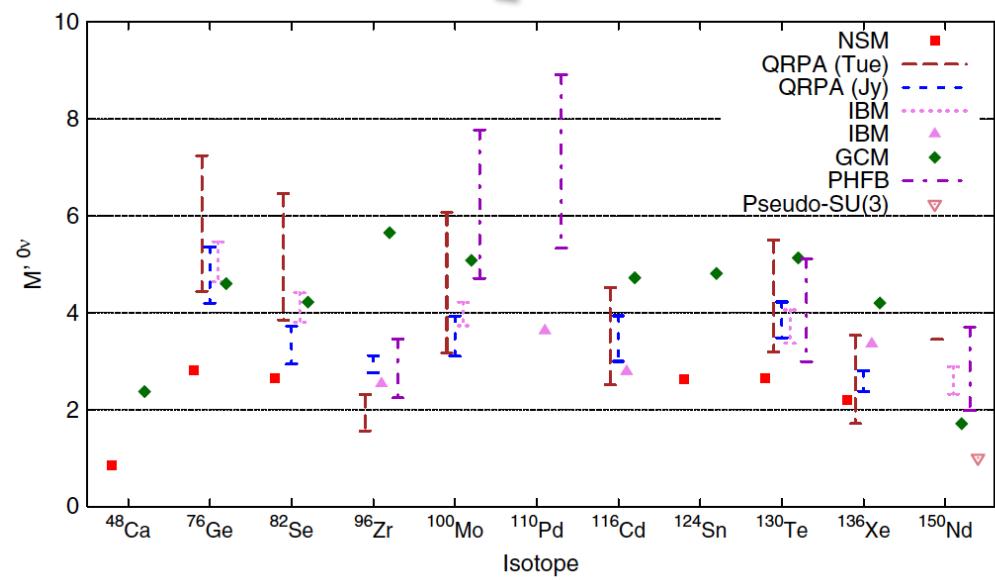
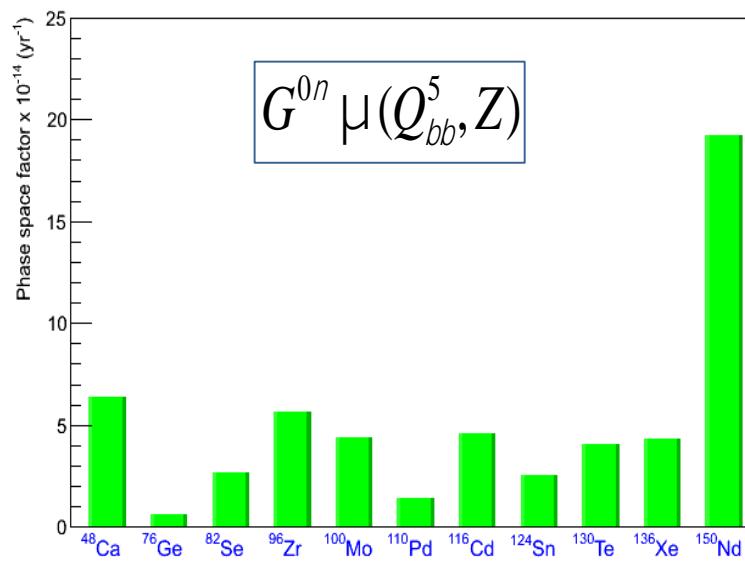
Possibility of enrichment
Expected half-life 10^{25} y

High isotopic abundance

	$Q_{\beta\beta}$ (MeV)	Isotopic Abundance
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	4.271	0.187
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	2.040	7.8
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	2.995	9.2
$^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$	3.350	2.8
$^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$	3.034	9.6
$^{110}\text{Pd} \rightarrow ^{110}\text{Cd}$	2.013	11.8
$^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$	2.802	7.5
$^{124}\text{Sn} \rightarrow ^{124}\text{Te}$	2.228	5.64
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	2.533	34.5
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	2.479	8.9
$^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$	3.367	5.6

Isotope choice

$$\left(T_{1/2}^{0n}\right)^{-1} = G^{0n} |M^{0n}|^2 \frac{\alpha \langle m_n \rangle \ddot{\theta}^2}{\zeta \frac{e}{m_e} \emptyset}$$



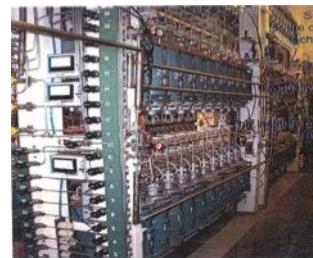
Isotopic enrichment

Nucleus	Existing method	R&D
^{48}Ca		Laser separation, gazeous diffusion
^{76}Ge	Centrifugation	
^{82}Se	Centrifugation	
^{96}Zr		Laser separation
^{100}Mo	Centrifugation	
^{116}Cd	Centrifugation	
^{130}Te	Centrifugation	
^{136}Xe	Centrifugation	
^{150}Nd		Centrifugation, Laser

R&D in KAERI (Korea) for
 ^{48}Ca enrichment by laser



R&D in Russia for
 ^{150}Nd enrichment
by centrifugation



R&D in France for
 ^{150}Nd enrichment
by laser

