Tracking detectors

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Course on Physics at the LHC LIP, 16th March 2015

Simplified overview of the LHC detectors concept

Inner tracking

- minimal interference with the event
- identify and measure charged particles

Calorimetry

- absorb electromagnetic and hadronic E
- avoid leakages \rightarrow hermetic

Outer tracking

Weakly interacting charged particles: muons

• Magnetic field

- → Field integral: B.r
- Crucial for particle separation and p measurement





Particles and their decays



Particles and their decays



Tracking: why?

- Identify the hard interaction vertex
 - Reconstruct secondary vertices from long lived particles
 - Measure particle trajectories
 - Momentum (p)
 - Energy loss (dE/dx)
 - Link to calorimeters (identify electrons, conversions)
 - Link to muon chambers : inner leg for muon reconstruction

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CMS Preliminary

16

12

10

\s=8 TeV. L=18.8 fb

Data (\s=8 TeV) MC: Q=3 400 GeV/a

Excluded

[HEP 07 (2013) 122

MC: Q=1 400 GeV/c²

MC: Q=2/3 400 GeV/c²

10⁴

 10^{3}

 10^{2}

10

Usage of Si-based trackers for HEP

- Kemmer, 1979 transferred Si-technology for electrons to detector NIM 169(1980)499
- NAII/32 spectrometer at CERN ►
 - 6 planes Si-Strip, <2k channels
 - Resolution ~4.5µm
- SLD vertex detector at SLAC ►
 - 120-307 M pixels: 0.4%X0
 - → Resolution <4µm, d₂~11-9µm
- ALEPH detector at LEP ►
 - Enable precise measurements for B-physics (lifetime, b-tagging)

	N	
nnels	(103)	Si are
95		0
405		

10 cm

10 CM

Experiment	Detectors	Channels (10 ³)	Si area [m ²]
Aleph (LEP)	144	95	0.49
CDF II (TEV)	720	405	1.9
D0 II (TEV)	768	793	4.7
AMS IÌ	2300	196	6.5
ATLAS (LHC)	4088	6300	61
CMS (LHC)	15148	10000	200

Tracking at the LHC - I

- Resolve 25 ns bunch crossings, keep low occupancy in high pileup regime
- Radiation hard, low material budget in front of calorimeters
- Good momentum resolution, and high efficiency
- Identify b-jets and hadronically decaying tau leptons (T)



Tracking at the LHC - II

















Tracking: what?

- While transversing a medium a charged particle leaves an ionization trace
 - create a depletion zone in between electrodes: gaseous, liquid or solid-state (semi-conductor)
 - ionization charges drift towards electrodes
 - amplify electric charge signal and deduce position from signals collected in individual strips



Tracking: how?

Solid state detectors

- Ge, Si, Diamond,...
- Pixels for vertexing, strips for tracking



- drift tubes, resistive plate chambers, gas electron multipliers, ...
- usually for outer tracking









Gaseous versus solid state

		Gas	Solid	state
Density (g/cm³)	Low	C₂H₂F₄	High	Si
Atomic number (Z)	Low	(~95% for CMS RPC)	Moderate	
lonization energy (ε_{l})	Moderate	30eV	Low	3.6eV
Signal speed	Moderate	10ns-10µs	Fast	<20ns

- In solid state detectors ionization energy converts in e-h pairs
 - 10 times smaller with respect to gaseous-based ionization
 - Charge is increased \rightarrow improved E resolution

$$n = \frac{E_{\text{loss}}}{E_{\text{eh}}} \to \frac{\sigma_{\text{E}}}{\text{E}} \propto \frac{1}{\sqrt{n}} \propto \sqrt{E_{\text{eh}}}$$

- Higher density materials used in solid state detectors
 - Charge collected is proportional to the thickness
 - Most probable value:

$$\frac{\Delta_p}{x} \sim 0.74 \cdot 3.876 \,\mathrm{MeV} \,/\,\mathrm{cm} \rightarrow N_{eh} \sim \frac{23 \cdot 10^3}{300 \mu m}$$

Excellent spatial resolution: short range for secondary electrons

Ionization energy loss in the Si



Most probable value of the Landau distribution for energy loss defines the minimum ionizing particle

Si properties



BAND GAP ENERGY (eV)

Low ionization energy

- → Band gap is 1.12 eV
- Takes 3.6 eV to ionize atom → remaining yields phonon excitations
- Long free mean path \rightarrow good charge collection efficiency
- High mobility \rightarrow fast charge collection
- Low Z → reduced multiple scattering
- Good electrical properties (SiO₂)

Good mechanical properties

- Easily patterned to small dimensions
- Can be operated at room temperature
- Crystalline → resilient against radiation

Widely used in industry

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ENERGY (eV)

IONIZATION

RADIATION

Tracking detectors

Excellent material for HEP detectors

Bond model of semi-conductors

• Covalent bonds formed after sharing electrons in the outermost shell

Thermal vibrations

- break bonds and yield electron conduction (free e⁻)
- remaining open bonds attract free e- \rightarrow holes change position \rightarrow hole conduction







- Valence electron
- ··· Conduction electron

Energy bands structure compared

In solids, the quantized energy levels merge

- <u>Metals</u>: conduction and valence band overlap
- Insulators and semi-conductors: conduction and valence band separated by energy (band) gap
- If µ (band gap) sufficiently low : electrons fill conduction band according to Fermi-Dirac statistics



Intrinsic carrier concentration

- The probability that an energy state is occupied by an e⁻ is given by Fermi statistics ▼
- At room temperature
 - excited electrons occupy conduction band
 - electrons tend to recombine with holes
- Excitation and recombination in thermal equilibrium
 - Intrinsic carrier concentration given by

 $n_{
m e} = n_{
m h} = n_{
m i} = A \cdot T^{3/2} \cdot e^{-Eg/k_{
m B}T}$

with A=3.1x10¹⁶ K^{-3/2}cm⁻³ and $E_g/2k_B = 7x10^3$ K

 \rightarrow n_i~1.45x10¹⁰ cm⁻³ \rightarrow 1/10¹² Si atoms is ionized



In semi-conductors signal-to-noise (S/N) is compromised by the band gap

- Keep low ionization energy \rightarrow small band gap
- Keep low intrinsic charge carriers \rightarrow large band gap
- → Optimal E_{g} ~6 eV → diamond ►



S/N in intrinsic Si detector

Example: Si detector with thickness d=300µm



- Minimum ionizing particle (MIP) creates:
- Intrinsic charge carriers (per cm²):

 $\frac{1}{E_{\rm eh}} \frac{dE}{dx} \cdot d = \frac{3.87 \cdot 10^6 {\rm eV/cm}}{3.63 {\rm eV}} \cdot 0.03 {\rm cm} = 3.2 \cdot 10^4 {\rm eh \ pairs}$

 $n_i \cdot d = 1.45 \cdot 10^{10} cm^{-3} \cdot 0.03 cm = 4.35 \cdot 10^8 eh pairs$

• Number of thermally-created e-h pairs exceeds mip signal by factor 10!

Si doping: n-dope bond model

- Doping with a group 5 atom (e.g. P,As, Sb)
 - atom is an electron donor/donator
 - Weakly bound 5th valence electron
 - Positive ion is left after conduction electron is released



Si doping: n-dope bond model II

- Energy level of donor is below edge of conduction band
 - Most electrons enter conduction band at room temperature
 - Fermi level moves up with respect to pure Si



Si doping: p-dope bond model

- Doping with a group 3 atom (e.g. B, Al, Ga, In)
 - atom is an electron acceptor
 - open bond attracts electrons from neighboring atoms
 - acceptor atom in the lattice becomes negatively charged



Si doping: p-dope bond model - II

- Energy level of acceptor is above edge of conduction band
 - Most levels are occupied by electrons \rightarrow holes in the valence band
 - Fermi level moves down with respect to pure Si



p-n junctions

- Difference in Fermi levels at the interface of n-type or p-type
 - diffusion of excess of charge carriers until thermal equilibrium (or equal Fermi level)
 - remaining ions create a **depletion zone**: electric field prevents further the diffusion



p-n junctions

pn junction scheme



acceptor and donator concentration









Biasing p-n junctions

p-n junction with forward bias





Forward-biased junction

- Anode to p, cathode to n
- Depletion zone becomes narrower
- Smaller potential barrier facilitates diffusion
- Current across the junction tends to increase



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Depletion zone width and capacitance

- Characterize depletion zone from Poisson equation with charge conservation:
- Typically: $N_a = 10^{15}$ cm⁻³ (p+ region) >> $N_d = 10^{12}$ cm⁻³ (n bulk)
- Width of depletion zone (n bulk): $W \approx \sqrt{\frac{2\epsilon V_{\text{bias}}}{q}} \cdot \frac{1}{N_d}$

Reverse bias voltage (V)	W_ρ (μm)	W _n (μm)
0	0.02	23
100	0.4	363

Device is similar to a parallel-plate capacitor

 $C = \frac{q}{V} = \frac{\varepsilon A}{d} = A \sqrt{\frac{\varepsilon q N_d}{2V_{\text{Visc}}}}$

Depletion voltage saturates the capacitance

Typical curve obtained for CMS strip detector



 $\nabla^2 \phi = -\frac{\rho_f}{2}$

citance C [nF]

detector capa

Leakage current

- Thermal excitation generates eh pairs
- Reverse bias applied separates pairs
- eh pairs do not recombine and drift
 - → leads to **leakage current**

Leakage current at room temperature for the CMS strip detector $\mathbf{\nabla}$

300 250 leakage current Io [nA] 200 150 100 50 0 50 300 350 0 100 150 250 200 reverse bias voltage V [V]

- Depends on purity and defects in material
- Depends on the temperature:



- prefer low, stable temperatures
- CMS tracker operated at <-10°C



Charge collection



→ 400 V bias, at 20°C, all charge collected after 10ns

Position resolution (DC coupled)

- Segmentation of the implants
 - reconstruct position of the particle
- Standard configuration uses
 - ✤ p implants in strips
 - n-doped substract ~300µm (2-10kΩcm)
 - depletion voltage <200 V</p>
 - Backside P implant establishes ohmic contact and prevents early breakdown
 - Al metallization
- Field closest to the collecting electrodes where most of the signal is induced



Position resolution (AC coupled)

Amplifier generates leakage current

- Blocked with AC coupling
- Deposit SiO₂ between p⁺ and Al strip
 - Capacitance ~32 pF/cm
 - Shorts through pinholes may be reduced with a second layer of Si₃N₄
- Use large poly silicon resistor (R>IMΩ) connecting the bias voltages to the strips





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CMS module



Pixel sensors

- High track density better resolved with 2D position information
 - back-to-back strips for 2D position information \rightarrow yields "ghost" hits
- Hybrid pixel detectors with sensors and readout chips bump-bonded together in model
 - e.g. one sensor, 16 front-end chips and 1 master controller chip



Hybrid Pixel Module for CMS

Sensor:

- Pixel Size: 150mm x 100mm
 - Resolution $\sigma_{r-\phi} \sim 15 \mu m$
 - Resolution $\sigma_z \sim 20 \mu m$
- n+-pixel on n-silicon design
 - Moderated p-spray → HV robustness
- Readout Chip:
- Thinned to 175µm
- 250nm CMOS IBM Process
- 8" Wafer

Kapton signal cable 21 traces, 300µ pitch

Alu-power cable 6 x 250µ ribbon

High Density Print 3 Layers, 48µ thick

Silicon Sensor t=285µ > 100µ x 150µ pixels

>µ-bump bonding

16 x Readout Chips (CMOS) 175µ thick

SiN base strips 250m thick, screw holes

screw holes

R. Horisberger

Performance: S/N

• **Signal** depends on the thickness of the depletion zone and on dE/dx of the particle



Optimizing S/N

- \rightarrow N_{ADC}>thr, given high granularity most channels are empty
- decrease noise terms (see above)
- minimize diffusion of charge cloud after thermal motion
 - (typically $\sim 8\mu$ m for 300 μ m drift)
- radiation damage severely affects S/N (next slide)



Influence of radiation

- In operation at the LHC Si performance is affected by radiation e.g. from CMS
 - depletion voltage increases with fluence, kept within 500V design limit
 - mild S/N degradation
 - expected hit finding efficiency after 10 years of LHC operation: 95%



Position resolution



- Affected by different factors
 - transverse drift of electrons to track
 - strip pitch to diffusion width relationship
 - statistical fluctuations on energy deposition



• Single strip resolution tends to dominate



A. Peisert, *Silicon Microstrip Detectors*, DELPHI 92-143 MVX 2, CERN, 1992

Coordinates for tracking

- The LHC experiments use a uniform B field along the beam line (z-axis)
 - Trajectory of charged particles is an helix radius R
 - Use transverse (xy) and longitudinal (rz) projections
 - Pseudo-rapidity: $\eta = -\ln \tan \frac{\theta}{2}$ Transverse momentum: $p_T = p \sin \theta = p / \cosh \eta$
- Impact parameter is defined from dca to origin or PV:



Resolution for the impact parameter

• Depends on radii+space point precisions

• For two layers we expect

$$\sigma_{d_0}^2 = rac{r_2^2 \sigma_1^2 + r_1^2 \sigma_2^2}{(r_2 - r_1)^2}$$

- Improve with small r_1 , large r_2
- Improves with better σ_i
- Precision is degraded by **multiple scattering**
 - Gaussian approximation is valid, width given by

$$\theta_0 = \frac{13.6 \text{MeV}}{\beta c p} z \sqrt{x/X_0} [1 + 0.038 \ln(x/X_0)]$$

extra degradation term for d₀



Resolution for the impact parameter

- For a track with $\theta \neq 90^{\circ}$ we can write $r \rightarrow r/\sin\theta$ and $x \rightarrow x/\sin\theta$
- By substitution in the formulas of the previous slide we have:



• **Resolution estimated with early pp data**

- Observed
 - 100 μm @ I GeV
 - 20 µm @ 20 GeV
- Excellent agreement with simulation



Examples from data: jets

Number of tracks reconstructed in jets

- two samples compared: multijets and top-pairs
- track multiplicity is not well described by standard PYTHIA generator
- $t \rightarrow Wb$ naturally enriches the top-pair sample in b-jets
- \rightarrow B-hadrons are long-lived, b-jets often contain tracks with high d₀





Examples from data: IP of tracks in jets

- Overall better agreement for b-jets: real displaced tracks
- Uncertainty on IP (resolution on IP) depends on the number of hits in pixels
 - jets from top pairs are more central with respect to a multijets sample



Examples from data: b-tagging from IP

- Distribution of the **third track with highest d** $_0/\sigma_{d0}$
 - Simple b-tagging algorithm, with high purity track counting high purity (TCHP)
 - Good description of the b-jets
 - Light jets hard to model in simulation: multiple scattering, fake hits, missing hits, conversions, V_0 decays



How can we profit from precision in d_o?

- ...it's not only the b-tagging performance that benefits
- Can use measurement of the displaced vertices to measure fundamental properties
- Boost of B-hadrons: proportional to the mass of a top quark when $t \rightarrow Wb$
 - $= \frac{L_{xy} = \gamma_B \beta_B \tau_B \approx 0.4 \frac{m_i}{m_B} \beta_B \tau_B}{2}$
 - Average shift of 30µm per 1 GeV
 - Use observed media to measure m_r

 $m_t = 173.5 \pm 1.5_{\text{stat}} \pm 1.3_{\text{syst}} \pm 2.6_{\text{PT}(\text{top})} \text{GeV}$





How can we profit to search for exotic signatures?

trajectory



• Search for long-lived particles decaying to jets

many displaced tracks: secondary vertex yielding two jets X ightarrow qq'

→ e.g.
$$H \rightarrow 2X$$
, $\tilde{q} \rightarrow X^0 q \rightarrow 3q+\mu$



Momentum measurement

• Circular motion under uniform B-field

 $R[m] = 0.3 rac{B[T]}{p_{\mathrm{T}}[GeV]}$

- Measure sagitta, s, from track ark
 - yields R estimate:

 $R = \frac{L^2}{2s} + \frac{s}{2} \approx \frac{L^2}{2s}$

- relate to B and estimate p_T



Uncertainty improves with B, number of hits, longer path L



• Again, spoiled with multiple scattering:

$$\frac{\sigma_{p_{\mathrm{T}}}}{p_{\mathrm{T}}} \sim a p_{\mathrm{T}} \oplus \frac{b}{\sin^{1/2}\theta}$$

Momentum resolution



Performance: ATLAS vs CMS

	ATLAS	CMS
Reconstruction efficiency for muons with $p_T = 1 \text{ GeV}$	96.8%	97.0%
Reconstruction efficiency for pions with $p_T = 1 \text{ GeV}$	84.0%	80.0%
Reconstruction efficiency for electrons with $p_T = 5 \text{ GeV}$	90.0%	85.0%
Momentum resolution at $p_T = 1$ GeV and $\eta \approx 0$	1.3%	0.7%
Momentum resolution at $p_T = 1$ GeV and $\eta \approx 2.5$	2.0%	2.0%
Momentum resolution at $p_T = 100$ GeV and $\eta \approx 0$	3.8%	1.5%
Momentum resolution at $p_T = 100$ GeV and $\eta \approx 2.5$	11%	7%
Transverse i.p. resolution at $p_T = 1$ GeV and $\eta \approx 0$ (µm)	75	90
Transverse i.p. resolution at $p_T = 1$ GeV and $\eta \approx 2.5$ (µm)	200	220
Transverse i.p. resolution at $p_T = 1000$ GeV and $\eta \approx 0 (\mu m)$	11	9
Transverse i.p. resolution at $p_T = 1000$ GeV and $\eta \approx 2.5 (\mu m)$	11	11
Longitudinal i.p. resolution at $p_T = 1$ GeV and $\eta \approx 0$ (µm)	150	125
Longitudinal i.p. resolution at $p_T = 1$ GeV and $\eta \approx 2.5$ (µm)	900	1060

- CMS tracker outperforms ATLAS: better momentum resolution, similar vertexing
- However it comes with a cost (next slide)

CMS tracker



- Pixel detector: ~ I m² area
 - I.4k modules
 - ✤ 66M pixels
- Strips: ~200m² area
 - 24k single sensors, I5k modules
 - 9.6M strips = electronics channels
 - 75k readout chips



CMS tracker budget

- In some regions can attain $I.8X_0 \rightarrow$ photons convert, electrons radiate often
- Use for alignment and material budget estimation
 - Simulation crucial for $H \to \gamma \gamma, H \to Z Z \to 2e2\mu, 4e$





X-ray of the CMS tracker

- Conversions: $\gamma \rightarrow e^+e^$
 - two op. Charged tracks consistent from the same point
 - consistent with fit to a common vertex with M=0 GeV
 - Note: 54% of the H \rightarrow yy events have are expected to have at least one conversion



Alignment check

• Use reconstructed long-lived neutral hadrons to compare simulation, PDG and data

	Mass (MeV/ c^2)			
V^0	Data	PDG	Simulation	Generated
K_{S}^{0}	497.68 ± 0.06	497.61 ± 0.02	498.11 ± 0.01	497.670
V_0	1115.97 ± 0.06	1115.683 ± 0.006	1115.93 ± 0.02	1115.680

Parameter	K ⁰ _S Data	K _S ⁰ Simulation	Λ^0 Data	Λ^0 Simulation
$\sigma_1(\text{MeV}/c^2)$	4.53 ± 0.12	4.47 ± 0.04	1.00 ± 0.26	1.71 ± 0.05
$\sigma_2(\text{MeV}/c^2)$	11.09 ± 0.41	10.49 ± 0.11	3.25 ± 0.14	3.71 ± 0.09
σ_1 fraction	0.58 ± 0.03	0.58 ± 0.01	0.15 ± 0.05	0.44 ± 0.03
$\overline{\sigma}(\text{MeV}/c^2)$	$\textbf{7.99} \pm \textbf{0.14}$	7.63 ± 0.03	3.01 ± 0.08	2.99 ± 0.03

$$\tau_{\rm K_c^0} = 90.0 \pm 2.1\,{\rm ps}$$

 $au_{\Lambda^0} = 271 \pm 20\,\mathrm{ps}$, both consistent with world average



Outer tracking



Find muons with the tracking system

- Standard-approach: outside-in
 - Standalone muon
 - Combine with tracker track
 - Fit a Global Muon track
- Complementary approach: inside-out
 - Extrapolate every track outward
 - Find compatible deposits in calorimeters
 - Define muon compatibility

Recovers inefficiencies

- Boundaries of muon chambers, low p_{T}





Performance: ATLAS vs CMS II

ATLAS

- → B=0.7 T (toroidal)
- → L~5m
- N=3 stations x 8 points



- s=750 µm for I TeV track
- 10% $\rightarrow \sigma$ =75 µm

Δp/p~**6**%

CMS

- B~2T (in return yoke)
- → L~3.5m
- N=4 stations x 8 points in rφ



- s=900 µm for I TeV track
- $10\% \rightarrow s=90\mu m$

Δp/p~I2%

Spoiled by multiple scattering in Fe

Combined muon performance in CMS

Combine with tracker: Δp/p~2%



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CMS dimuon performance



- Tracking system is crucial for reconstruction
- Detector design must be physics-driven: optimal reconstruction+performance
- Combine powerful tracker with field integral: base for particle-flow

- Particle data group, "2013 Review of Particle Physics", PRD 86 010001 (2012)
- CMS Collaboration, "The CMS experiment at the CERN LHC", JINST 3 (2008) S08004
- D. Bortoletto, "Detectors for particle physics semiconductors", Purdue
- A. David, "Tracking and trigger", LIP
- M. Kranmer, "Silicon detectors", HEPHY