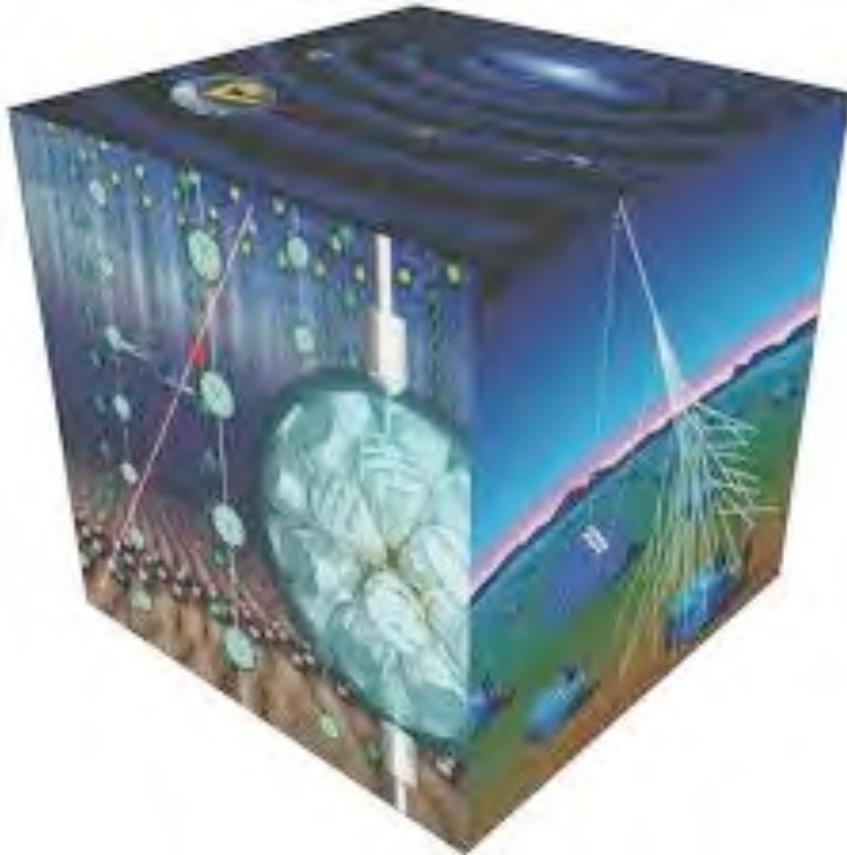


Astroparticle Physics



Cosmic rays

Gamma rays

Neutrinos

Gravitational waves

???

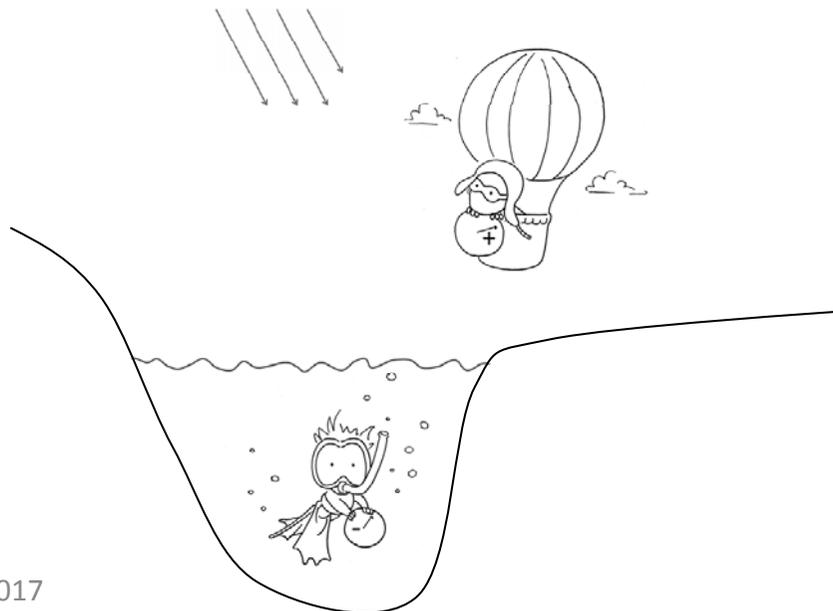
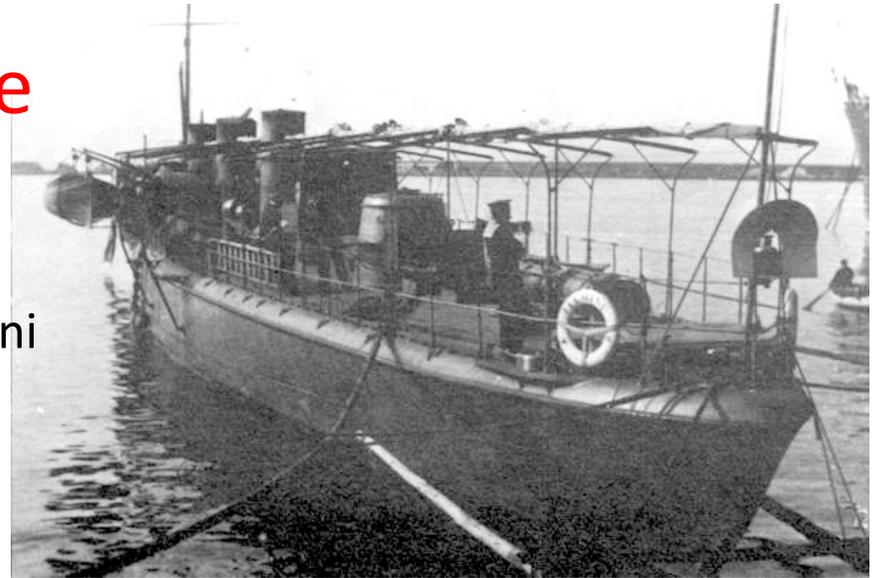
Alessandro De Angelis Mário Pimenta
Asiago, June 2017

I- Introduction

Messengers from the Universe

1911/12: Domenico Pacini and Victor Hess perform two complementary experiments: Pacini discovers that ionizing radiation decreases underwater, and Hess that it increases at high altitudes

- 20% of the natural radiation at ground is due to cosmic radiation!!! Can we use these “**cosmic rays**” for science?



YES (the birth of Particle Physics)

Positron (Anderson 1932)

Antimatter! (Dirac)

$\gamma \rightarrow e^+e^-$ (Einstein)

μ (Anderson 1937)

Rossi, 1940:

Muon life time.

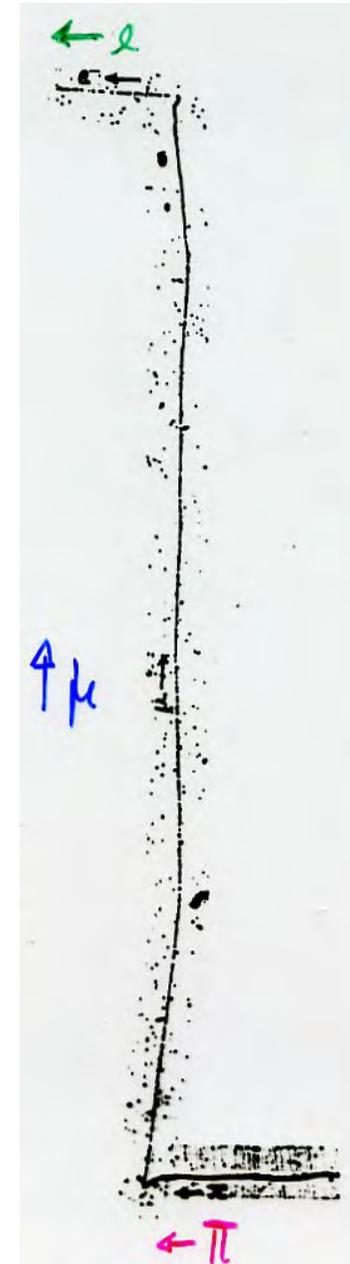
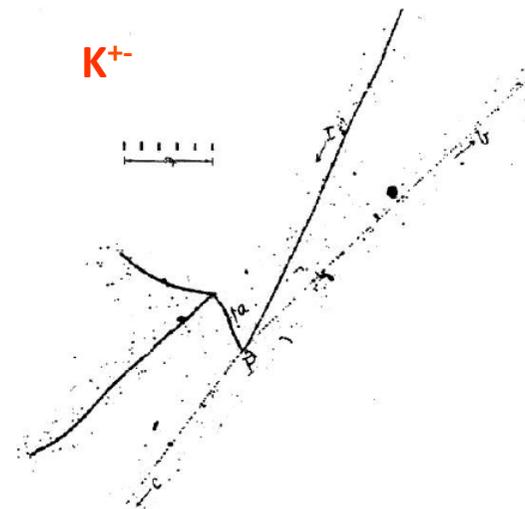
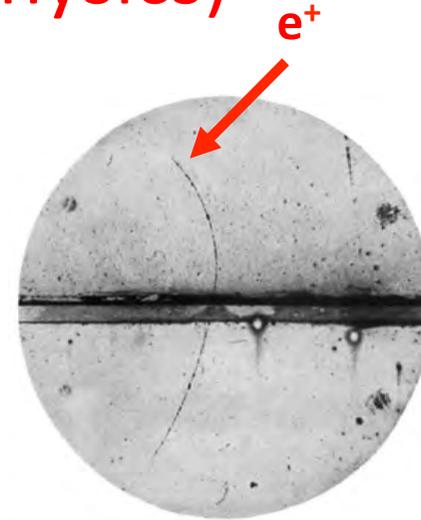
Time dilation!

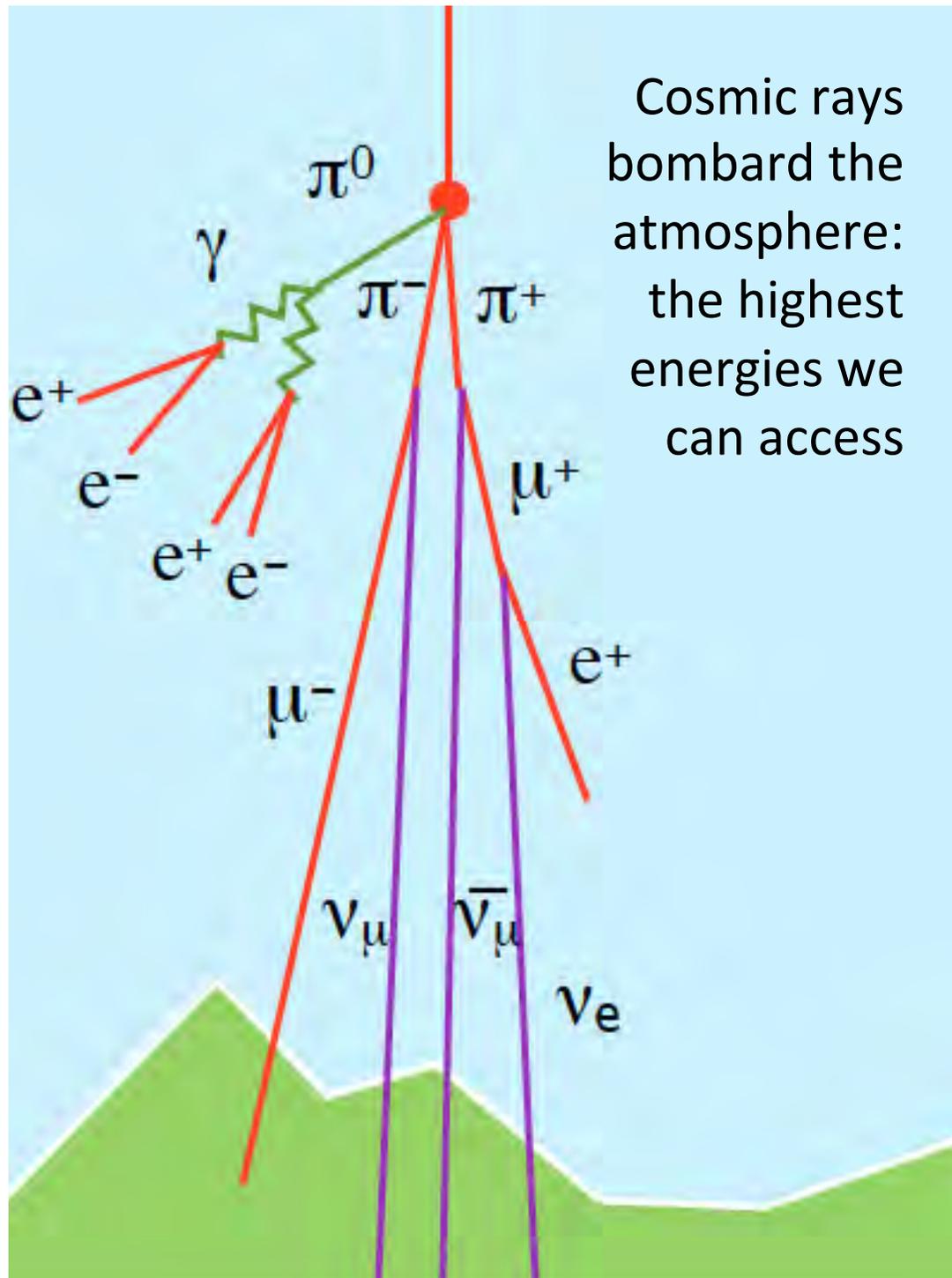
π (Lattes, Powell 1947)

Strong interactions (Yukawa)

K, Λ , ... (Leprince Ringuet 1944, Rochester, Butter 1947, ...)

Strangeness





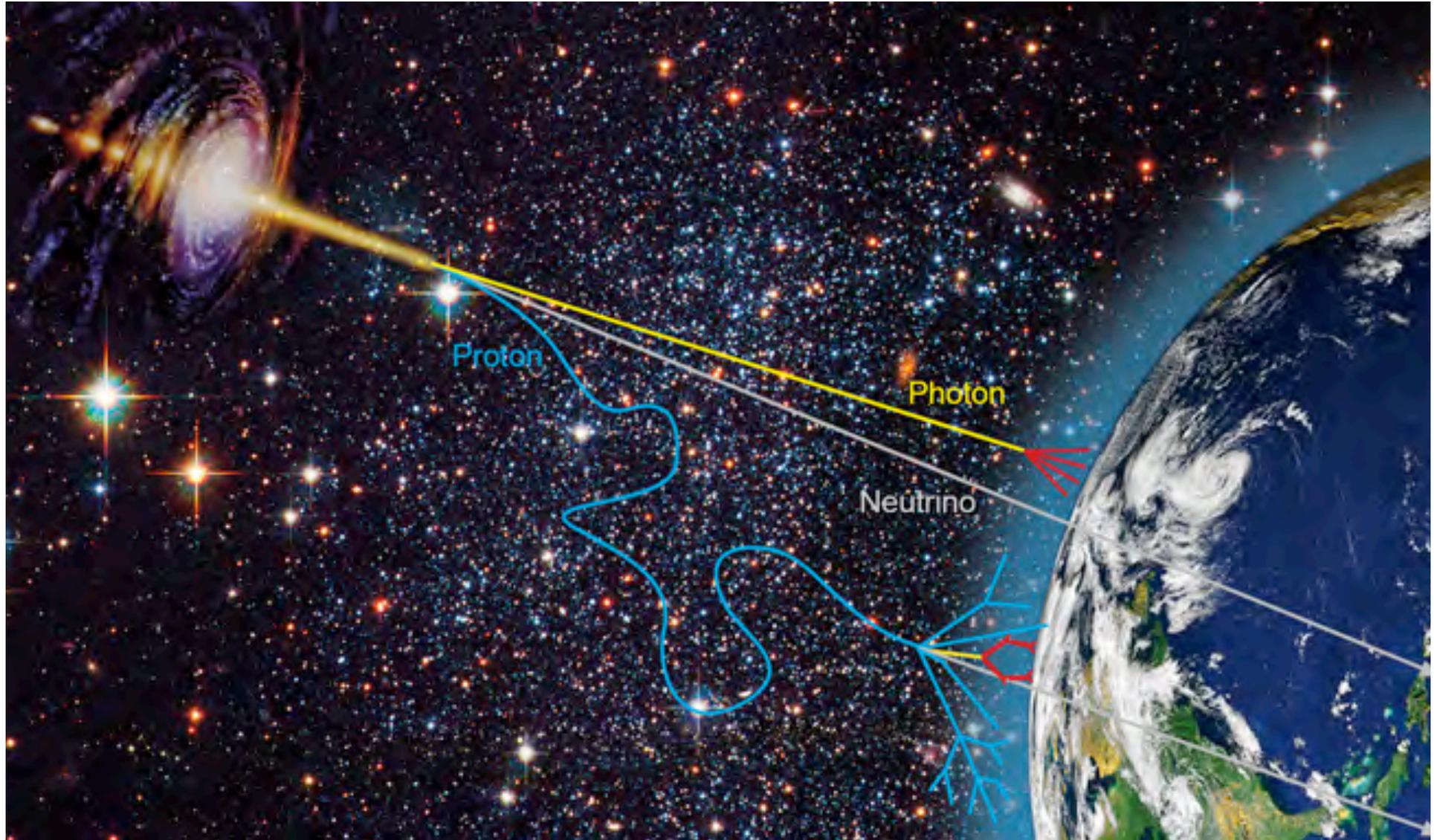
YES, and it allows accessing the highest energies

Detected protons 10^8 times more energetic than LHC

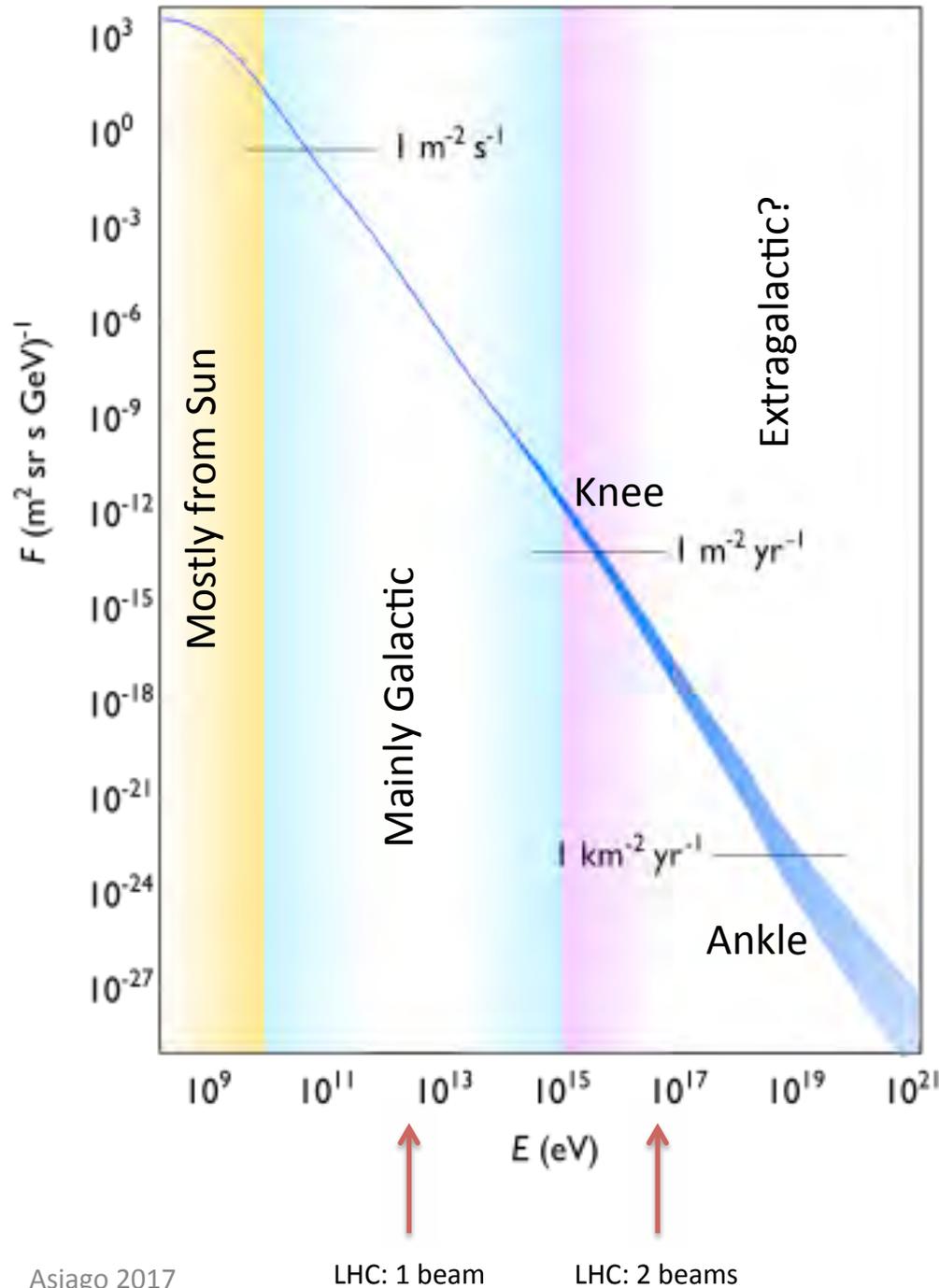
Detected gamma-rays 10000 times more energetic than human-made

Detected neutrinos 10^5 times more energetic than human-made

YES, and it allows understanding high-energy astrophysics (physics under extreme conditions)



Cosmic Rays ("astroparticles")

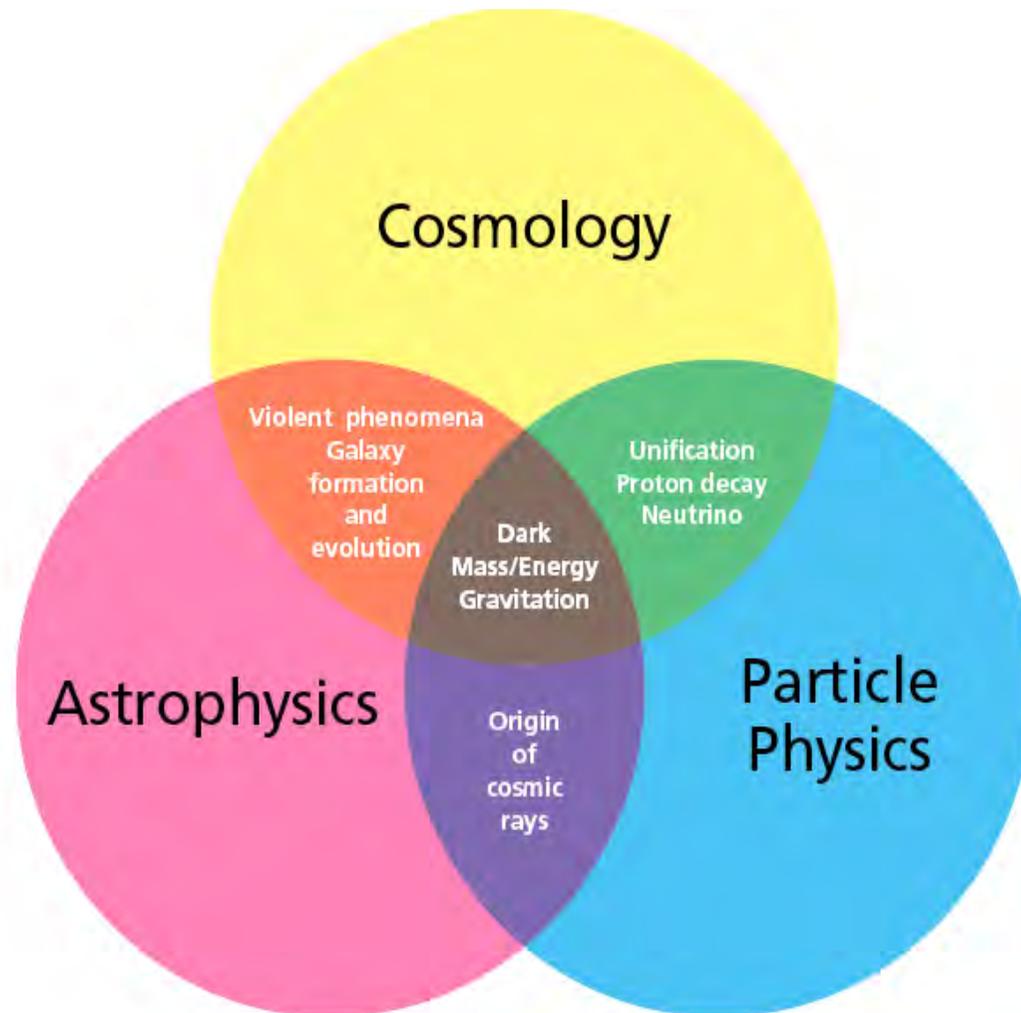


- Once per second per cm² a high-energy particle from the sky hits the Earth
 - Mostly (~89%) protons
 - He (~9%) nuclei and heavier (~1%);
 - Electrons are ~1%
 - 0.01% - 1% are gamma rays

$$\frac{dN}{dE} \approx 1.8 \times 10^4 \left(\frac{E}{\text{GeV}} \right)^{-2.7} \frac{\text{particles}}{\text{m}^2 \text{ s sr GeV}}$$

- The flux falls as $\sim E^{-2.7}$ as energy increases
 - 10²¹ eV once per second on Earth
 - The highest energies

Astroparticle physics



A multimessenger science

1. *HE gammas*
2. *HE neutrinos*
3. *HE protons/nuclei*
4. *Gravitational waves*

Several possible fundamental physics objectives

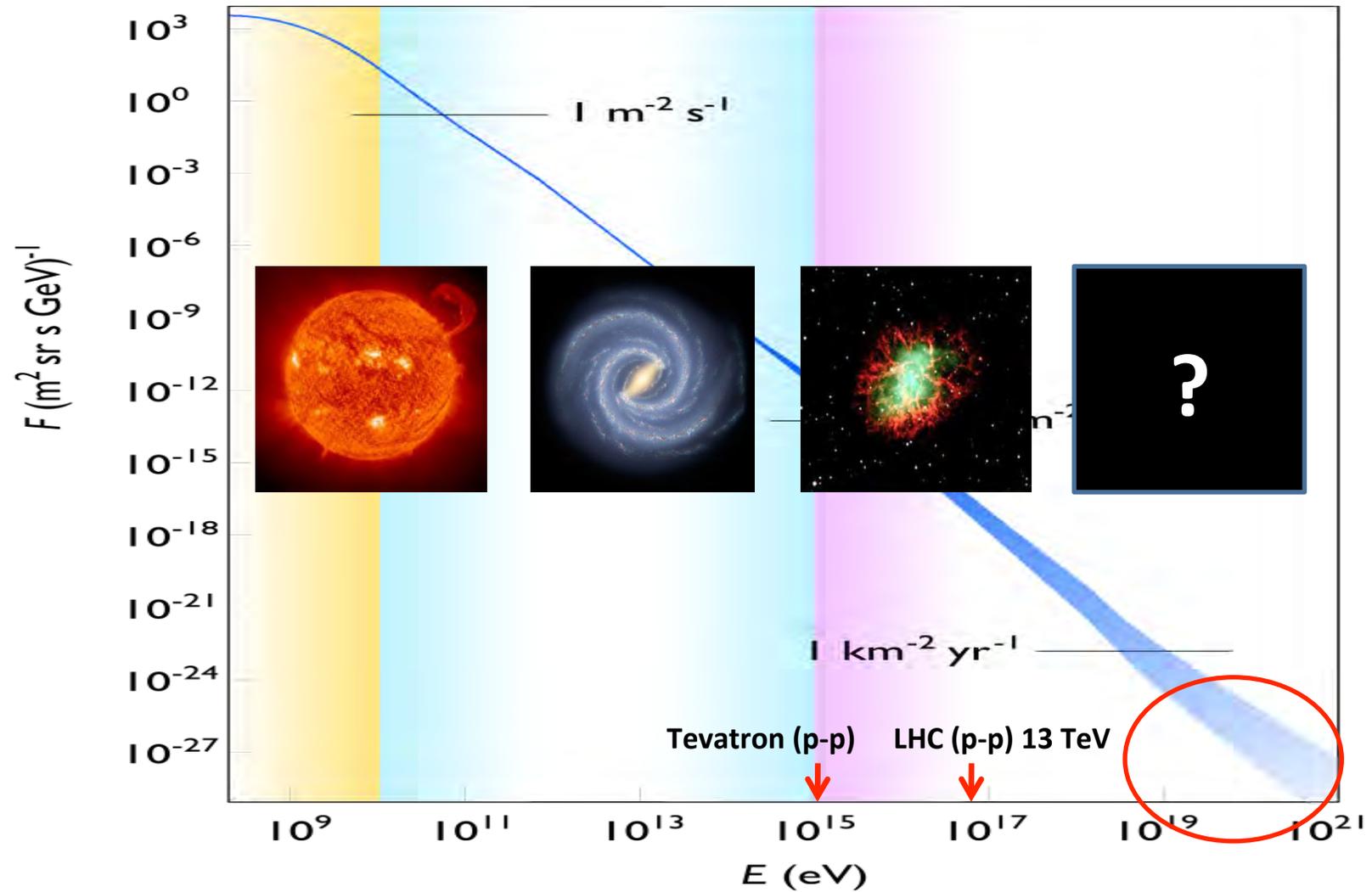
1. *Extremely high energy collisions*
2. *Dark matter/energy*
3. *Axions, ALPs*
4. *Neutrino mass*
5. *Neutrino mixing*
6. *CMB*

And of course, astrophysics

1. *Behavior of physics near (SM)BHs*
2. *Acceleration mechanisms*

II- Production

Origin ! ?



Possible UHECR Sources: **2 scenarios**

Bottom-Up Acceleration

(Astrophysical Acceleration Mechanisms)

UHECR's are accelerated in extended objects or catastrophic events (supernova remnants, rotating neutron stars, AGNs, radio galaxies)

Experimental evidence:

- ✓ anisotropy in arrival directions
- ✓ Photons $< \approx 1\%$

Top-Down Decay

(Physics Beyond the Standard Model)

Decay of topological defects
Monopoles Relics
Supersymmetric particles
Strongly interacting neutrinos
Decay of massive new long lived particles
Etc.

Experimental evidence:

- ✓ isotropy in arrival directions
- ✓ Photons $> \approx 10\%$

Ila- Charged particle acceleration

Origin ($E \sim <10^{15}$ eV)?

Energy density (cosmic rays)

$$\rho_E \sim \int E \frac{dN}{dE} dE \sim 10^{-12} \text{ erg/cm}^3$$
$$\sim 1 \text{ eV/cm}^3$$

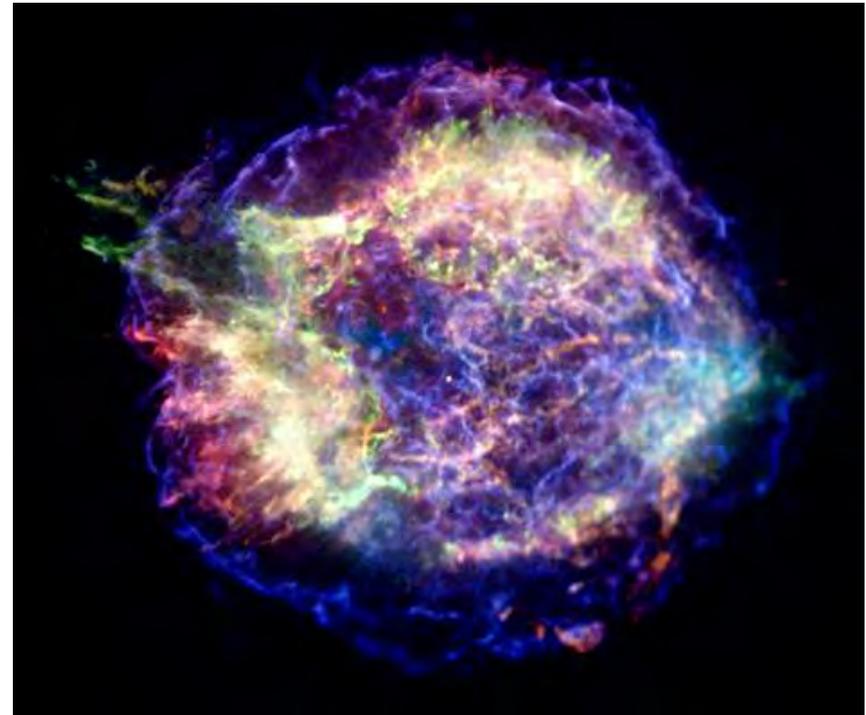
$$P \sim \frac{\rho_E V_{\text{galaxy}}}{\tau_{\text{esc}}} \sim 5 \cdot 10^{40} \text{ erg/s}$$

For example, power dissipated by a Supernova (the remnant of a collapsed star) of $10 M_{\text{sun}}$.

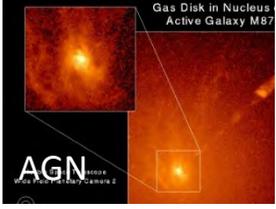
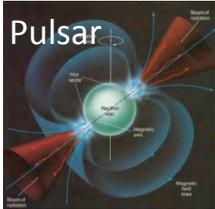
$$E \sim 10^{53} \text{ erg}$$

Supernovae in our Galaxy

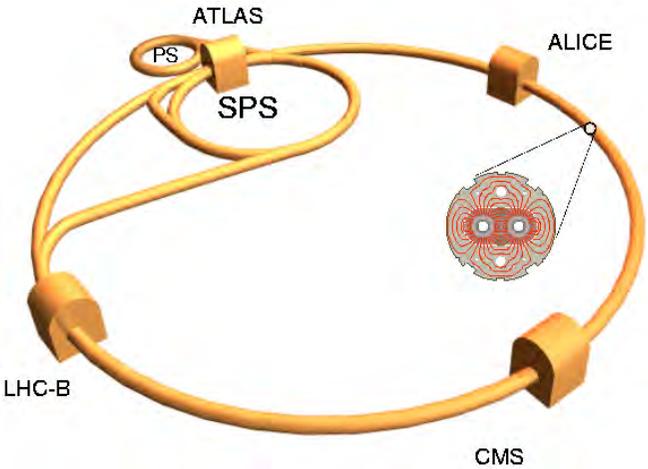
$$1 \text{ SN} \sim 30 \text{ Years} \sim 10^{-9} \text{ s}^{-1}$$



Where can be these accelerators in the Universe?



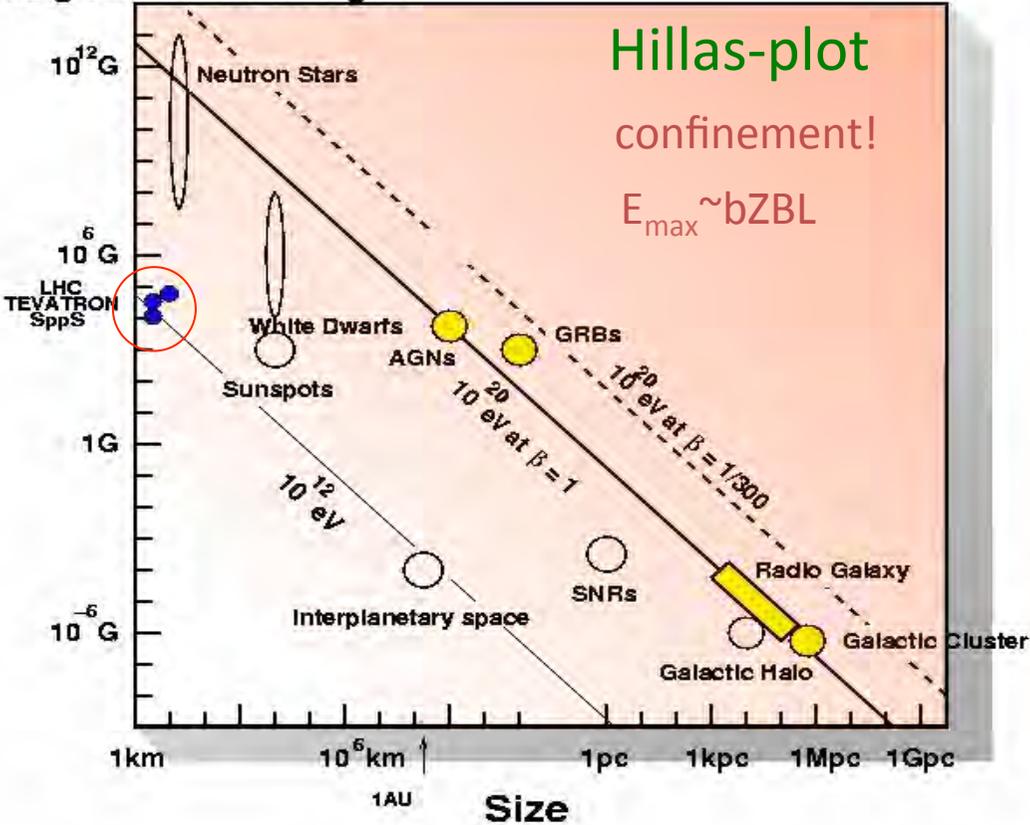
Large Hadron Collider



$E \propto BR$

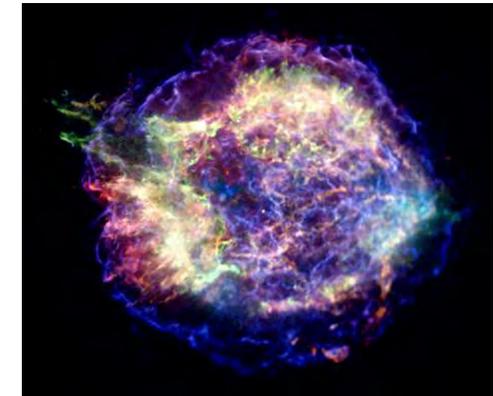
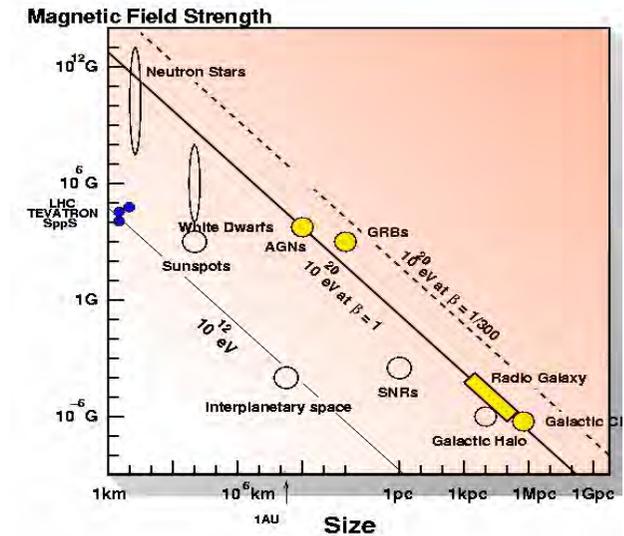
$R \sim 10 \text{ km}, B \sim 10 \text{ T}$
 $E \sim 10 \text{ TeV}$

Magnetic Field Strength

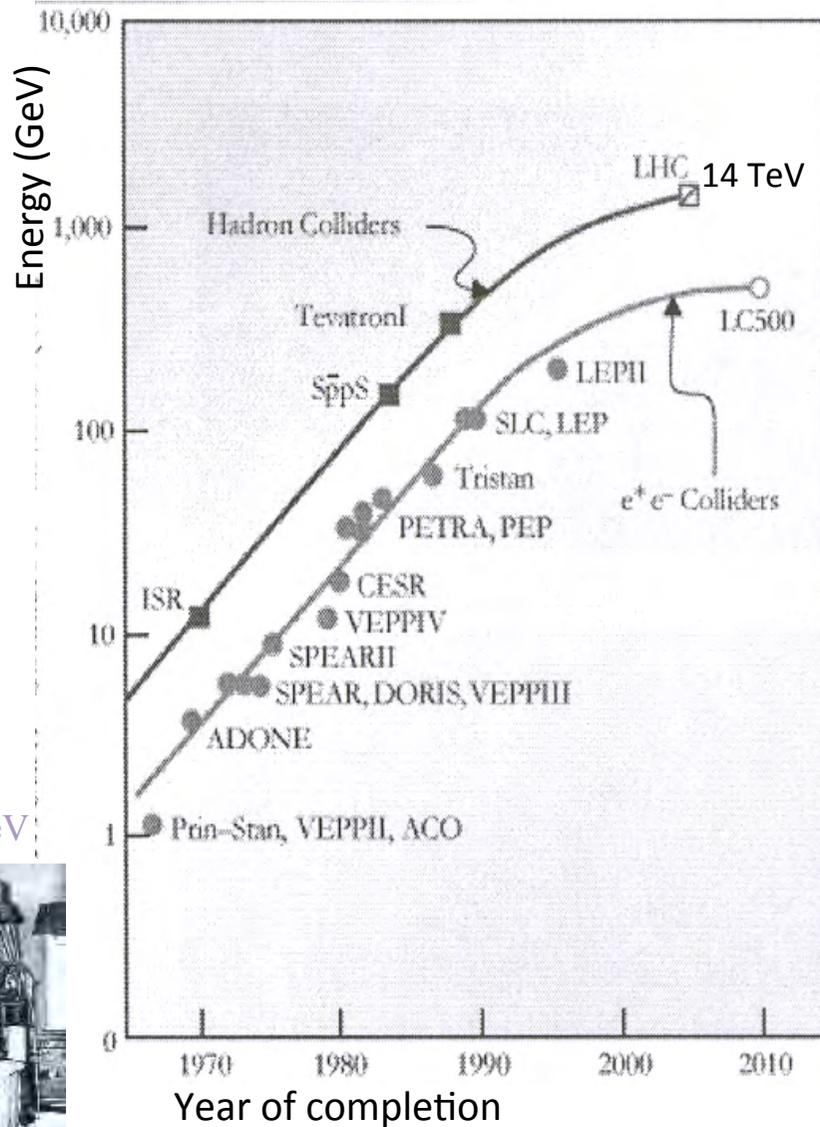


A few new terms

- Stellar end-products. A star heavier than the Sun collapses at the end of its life into a neutron star ($R \sim$ few km, which can be pulsating – a **pulsar**) or into a BH, and ejects material in an explosion (**SuperNova Remnant**).
 - Very large B fields are in the pulsar; magnetic fields also in the SNR
- The centres of galaxies host black holes, often supermassive (millions or even billion solar masses). They might accrete at the expense of the surrounding matter, and accelerate particles in the process. When they are active, they are called **Active Galactic Nuclei**.



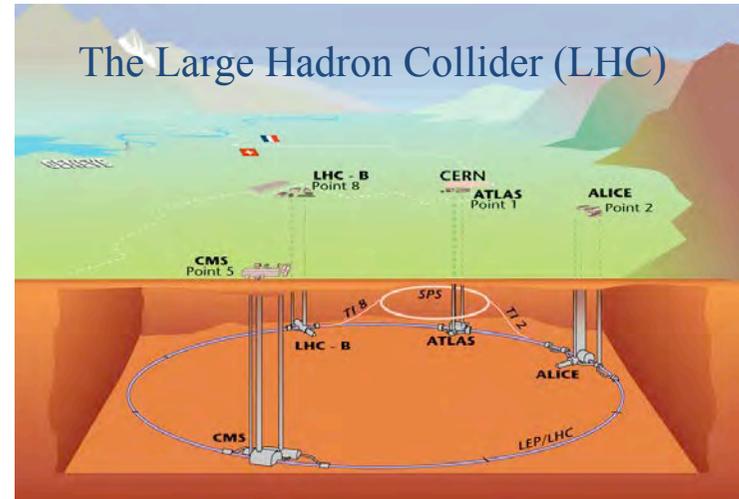
They surpass human-made accelerators



~ 10 MeV

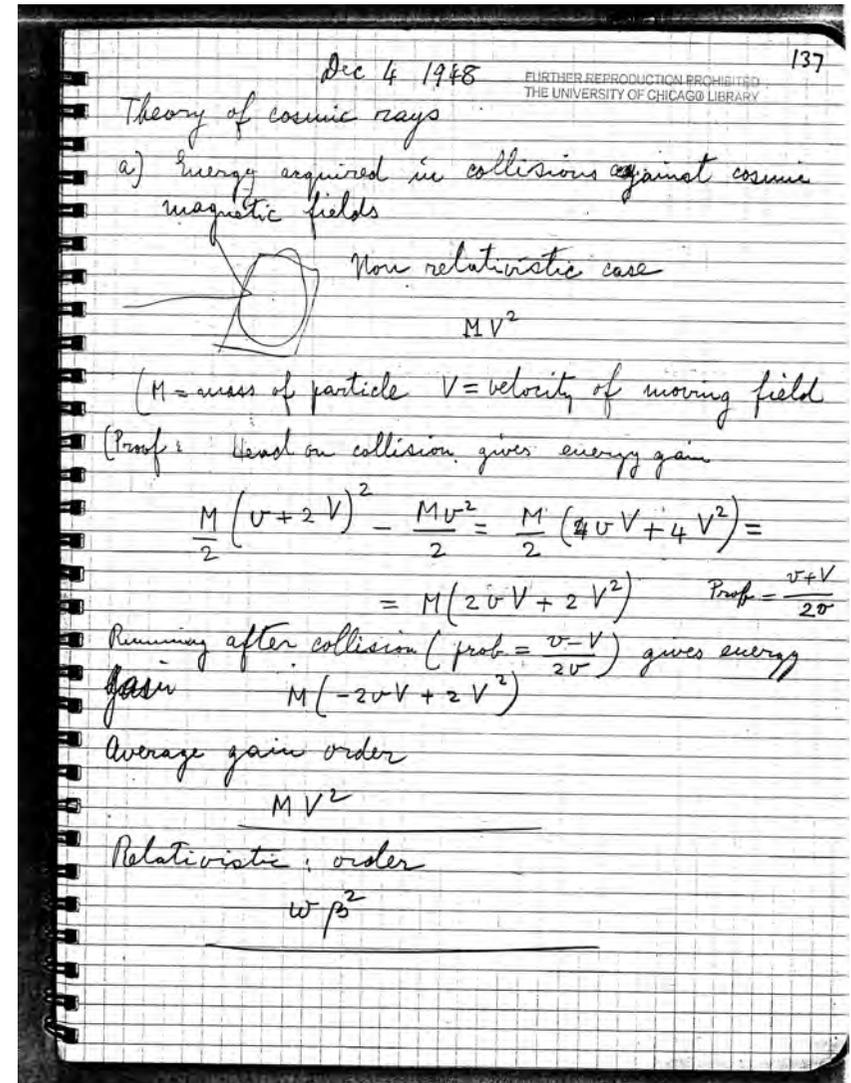


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High Luminosity
 Sophisticated detectors
 Central region
 Energy limited

How to generate bottom-up energies much higher than thermal?



Acceleration mechanism

Fermi 2nd order (1949)

particles accelerated in stochastic collisions with massive interstellar clouds (collisions to a moving diffusive wall!)

In the cloud reference frame

$$E_1^* = \gamma E_1 (1 - \beta \cos \theta_1)$$

$$E_2^* = E_1^*$$

Back to the Lab reference frame

$$E_2 = \gamma E_2^* (1 + \beta \cos \theta_2^*)$$

Then:

$$\frac{\Delta E}{E} = \frac{1 - \beta \cos \theta_1 + \beta \cos \theta_2^* - \beta^2 \cos \theta_1 \cos \theta_2^*}{1 - \beta^2} - 1$$

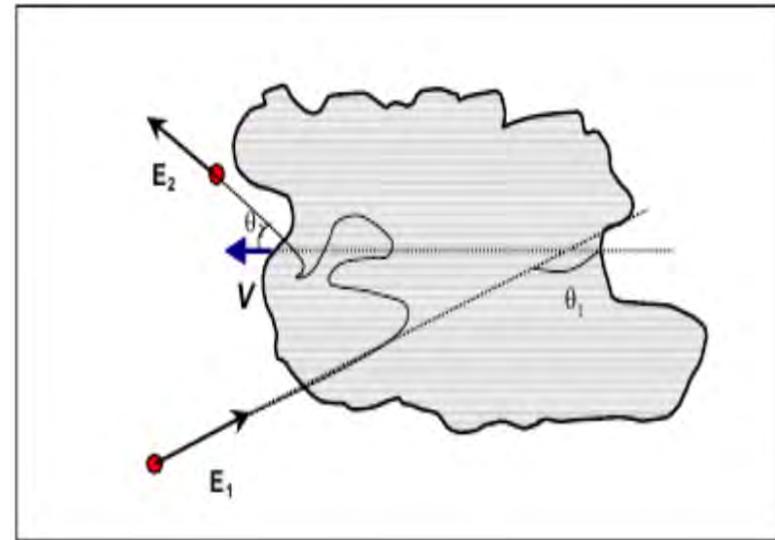
But:

$$\langle \cos \theta_2^* \rangle = 0$$

$$\langle \cos \theta_1 \rangle = \frac{\int_{-1}^1 \cos \theta_1 \overbrace{(1 - \beta \cos \theta_1)}^{\text{Probability}} d\cos \theta_1}{\int_{-1}^1 (1 - \beta \cos \theta_1) d\cos \theta_1} = -\frac{\beta}{3}$$

$$\left\langle \frac{\Delta E}{E} \right\rangle \approx \frac{4}{3} \beta^2$$

$$\beta \sim 10^{-4} !!!$$



Acceleration mechanism

Fermi 1st order

Shock formation :

- Sudden release of Energy (CMEs, SNRs, GRBs,...)
- Supersonic flow hits an obstacle (AGNs jets, pulsar winds, ...)

Particles gain energy by consecutive crossings of the shock front!

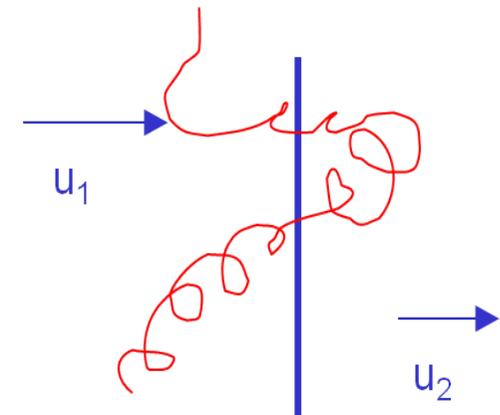
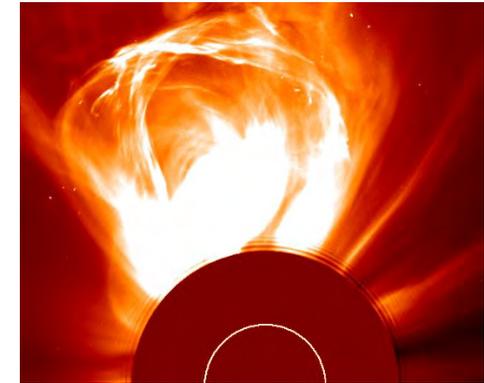
$$\frac{\Delta E}{E} = \frac{1 - \beta \cos \theta_1 + \beta \cos \theta_2^* - \beta^2 \cos \theta_1 \cos \theta_2^*}{1 - \beta^2} - 1$$

Now (plane shock front):

$$\langle \cos \theta_1 \rangle = \frac{\int_{-1}^0 \cos^2 \theta_1 d\cos \theta_1}{\int_{-1}^0 \cos \theta_1 d\cos \theta_1} = -\frac{2}{3}$$

$$\langle \cos \theta_2^* \rangle = \frac{\int_0^1 \cos^2 \theta_2^* d\cos \theta_2^*}{\int_0^1 \cos \theta_2^* d\cos \theta_2^*} = \frac{2}{3}$$

Solar coronal mass ejection 9 Mar 2000



Crossing probability $\propto \cos(\theta)$

$$\left\langle \frac{\Delta E}{E} \right\rangle \approx \frac{4}{3} \beta$$

The power law

In each cycle the particle gains a small fraction of energy ϵ . After n cycles:

$$E_n = E_0 (1 + \epsilon)^n$$

Or the number of cycles to attain an energy E is:

$$n = \ln(E/E_0)/\ln(1+\epsilon)$$

The particle may escape from the shock region with some probability P_i . Then the probability to escape with $E > E_n$ is:

$$P_{E_n} = P_i \sum_{j=n}^{\infty} (1 - P_i)^j = (1 - P_i)^n$$

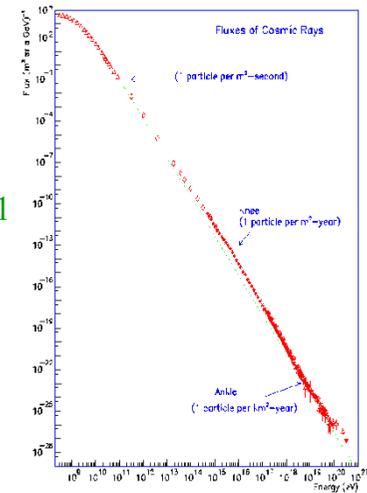
and

$$\frac{N}{N_0} = P_{E_n} = \left(\frac{E}{E_0}\right)^{-\alpha}$$

$$\alpha = -\frac{\ln(1 - P_i)}{\ln(1 + \epsilon)} \cong \frac{P_i}{\epsilon}$$

$$\frac{dN}{dE} \propto E^{-\gamma}$$

$$(N > E) \propto E^{-\gamma+1}$$



$$\frac{dN}{dE} \propto \left(\frac{E}{E_0}\right)^{-\gamma} \quad \gamma = \alpha + 1$$

$$\left(\frac{dN}{dE}\right)_{Source} \approx E^{-2}$$

$$\left(\frac{dN}{dE}\right)_{Earth} \propto \left(\frac{dN}{dE}\right)_{Source} \cdot \tau_{esc}(E) \propto E^{-2.7}$$

Zwicky conjectures (1933)

1. Heavy enough stars collapse at the end of their lives into super-novae
2. Implosions produce explosions of cosmic rays
3. They leave behind neutron stars



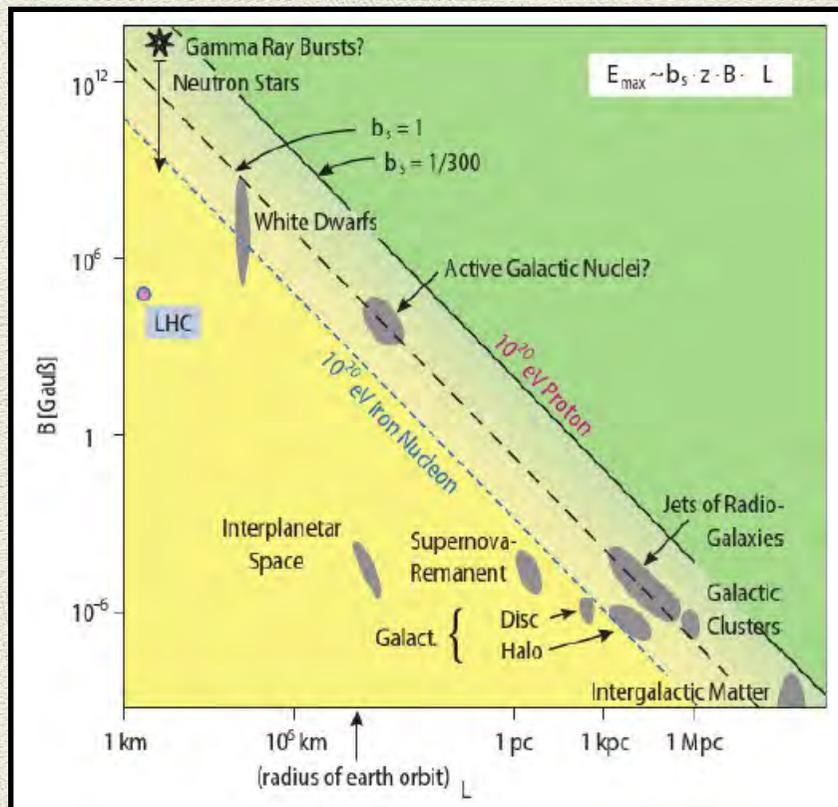
(Zwicky in 1930)

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Where do they come from?

r_L must be smaller than the dimension of the source L to remain confined.



$$r_L = \frac{E_{15}}{Z B_{\mu G}} [\text{pc}]$$

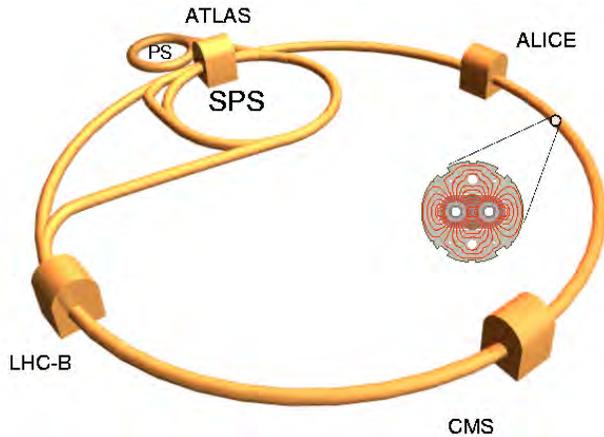
$$E_{max} \simeq ZeBL\beta$$

One should consider also energy losses at the source

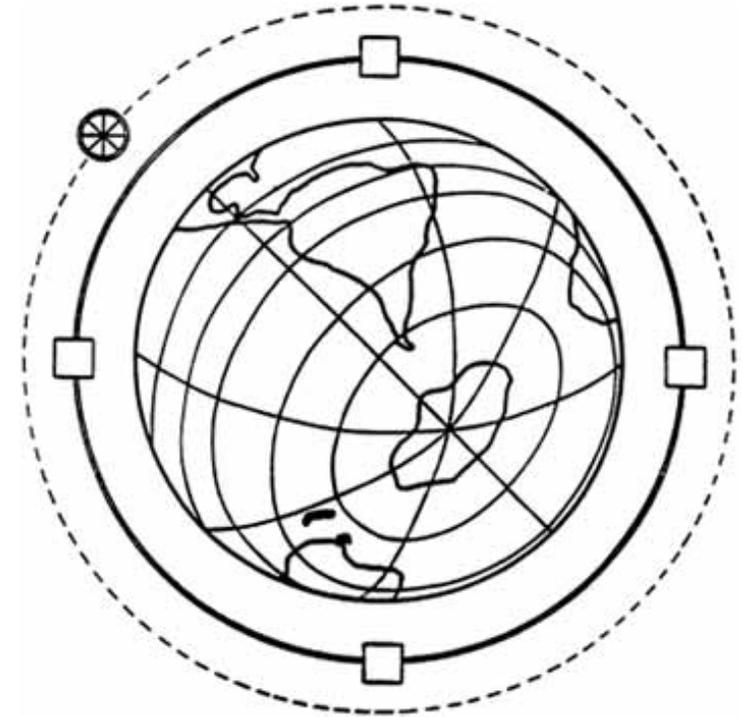
$$E = k B R$$

Whatever is the acceleration mechanism...

Large Hadron Collider

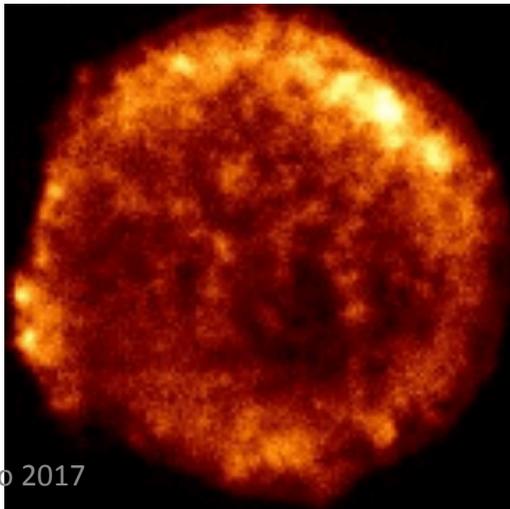


$R \sim 10 \text{ km}$, $B \sim 10 \text{ T}$
 $\Rightarrow E \sim 10 \text{ TeV}$



The maximum energy possible on Earth is $\sim 5000 \text{ TeV}$

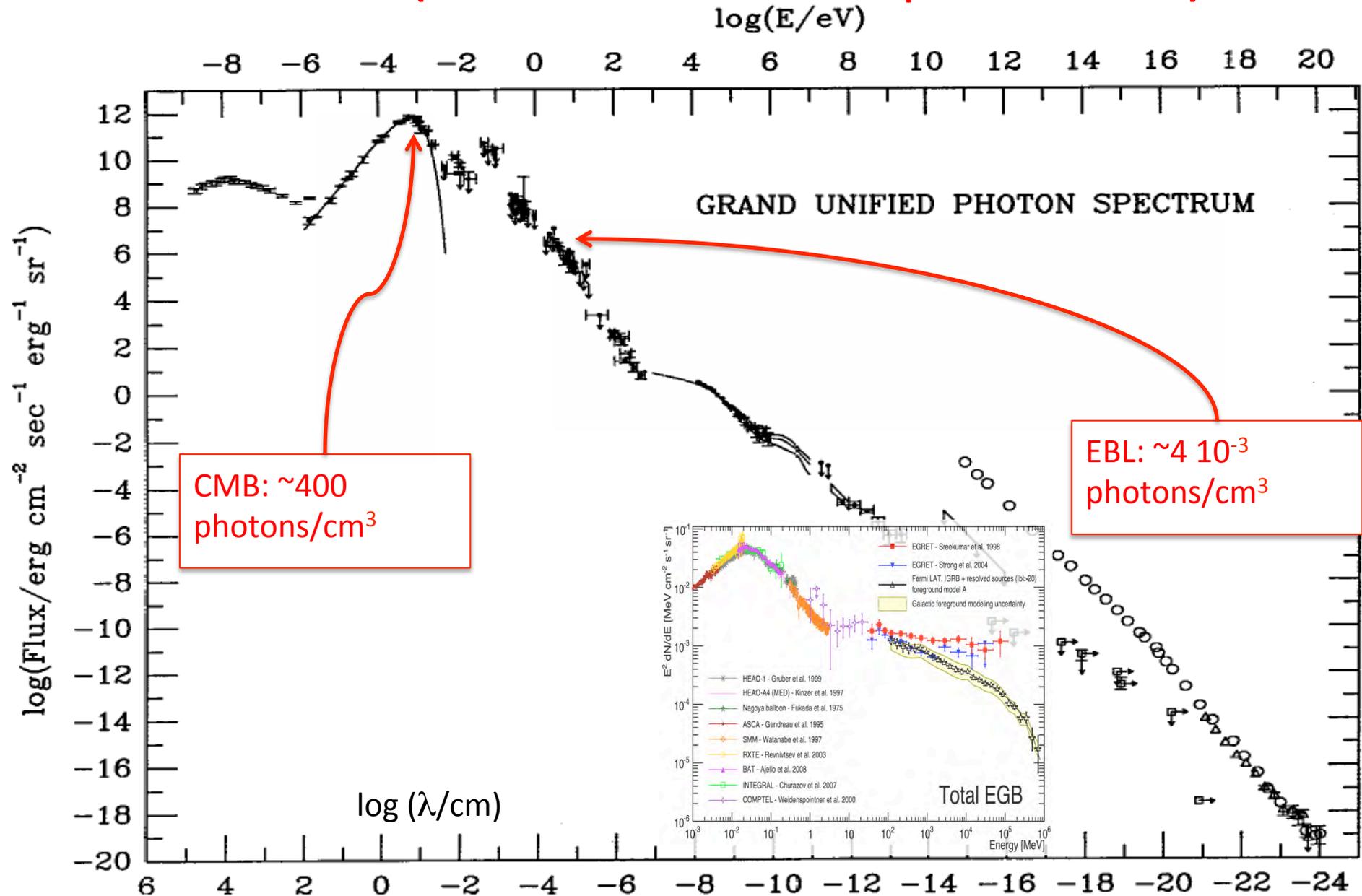
Tycho SuperNova Remnant



$R \sim 10^{15} \text{ km}$, $B \sim 10^{-10} \text{ T}$
 $\Rightarrow E \sim 1000 \text{ TeV}$

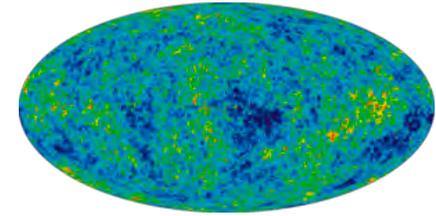
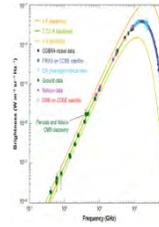
IIb- Production of high energy photons (and neutrinos)

The observed photon spectrum extends over 30 decades (measurements up to 1 TeV)



Thermal radiation: Blackbody Spectra

CMB:
2.7 K

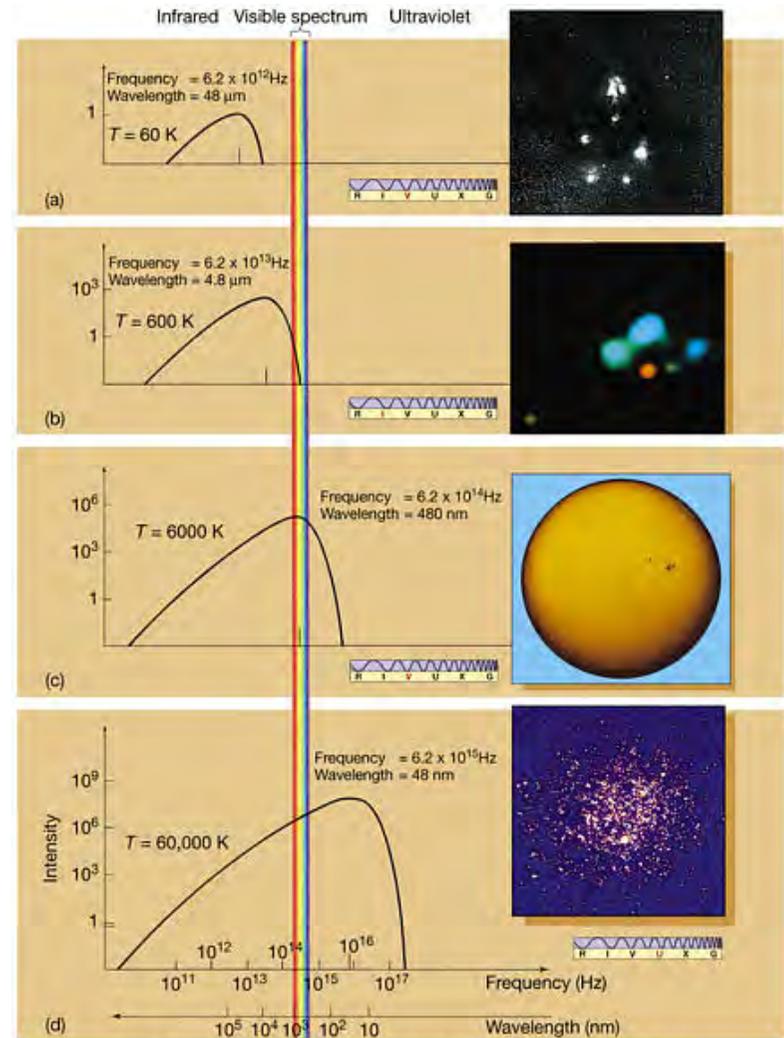


A Galactic gas cloud
60 K

Dim star in the Orion Nebula:
600 K

The Sun:
6000 K

Cluster of very bright stars,
Omega Centauri:
60 000 K



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γ rays: non-thermal Universe

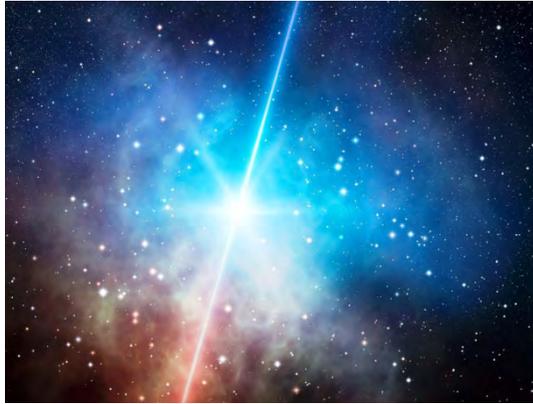
- Particles accelerated in extreme environments interact with medium
 - Gas and dust; Radiation fields – Radio, IR, Optical, ...;
 - Intergalactic Magnetic Fields, ...
- Gamma rays traveling to us!

- No deflection from magnetic fields, gammas point \sim to the sources
 - Magnetic field in the galaxy: $\sim 3\mu\text{G}$
 - Gamma rays can trace cosmic rays at energies $\sim 10x$
- Large mean free path
 - Regions otherwise opaque can be transparent to X/γ

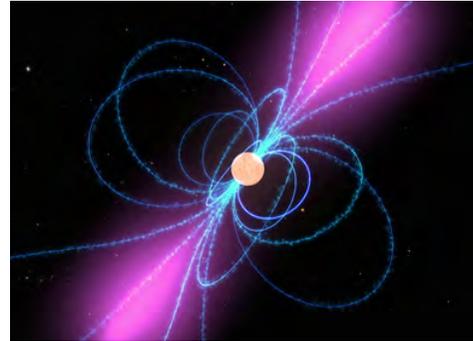
Studying Gamma Rays allows us to see different aspects of the Universe

Examples of known extreme environments

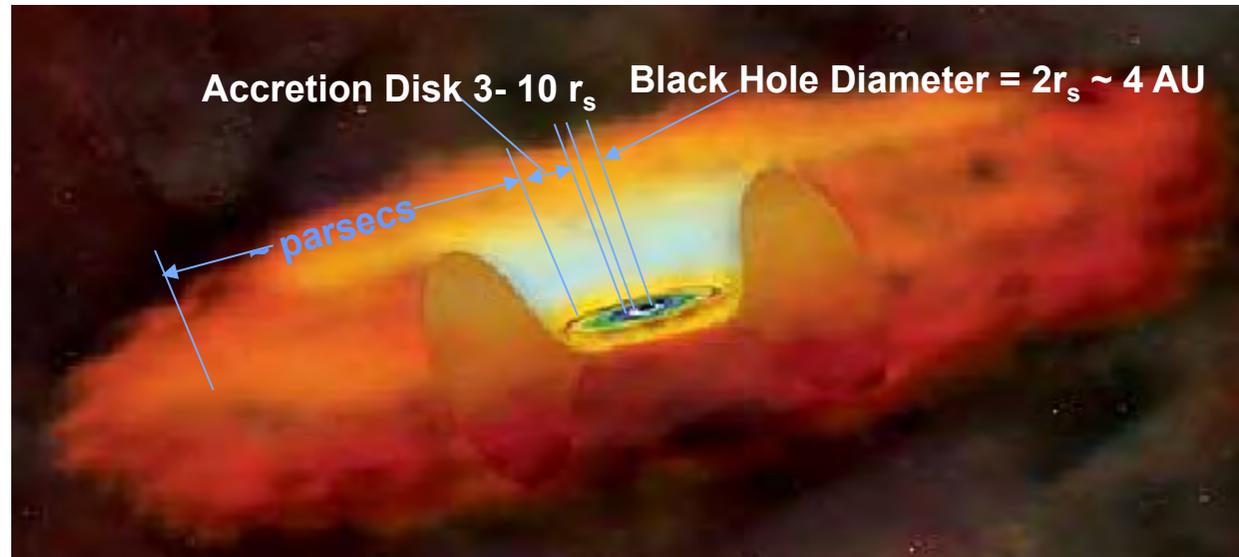
GRB



SuperNova Remnants
Pulsars



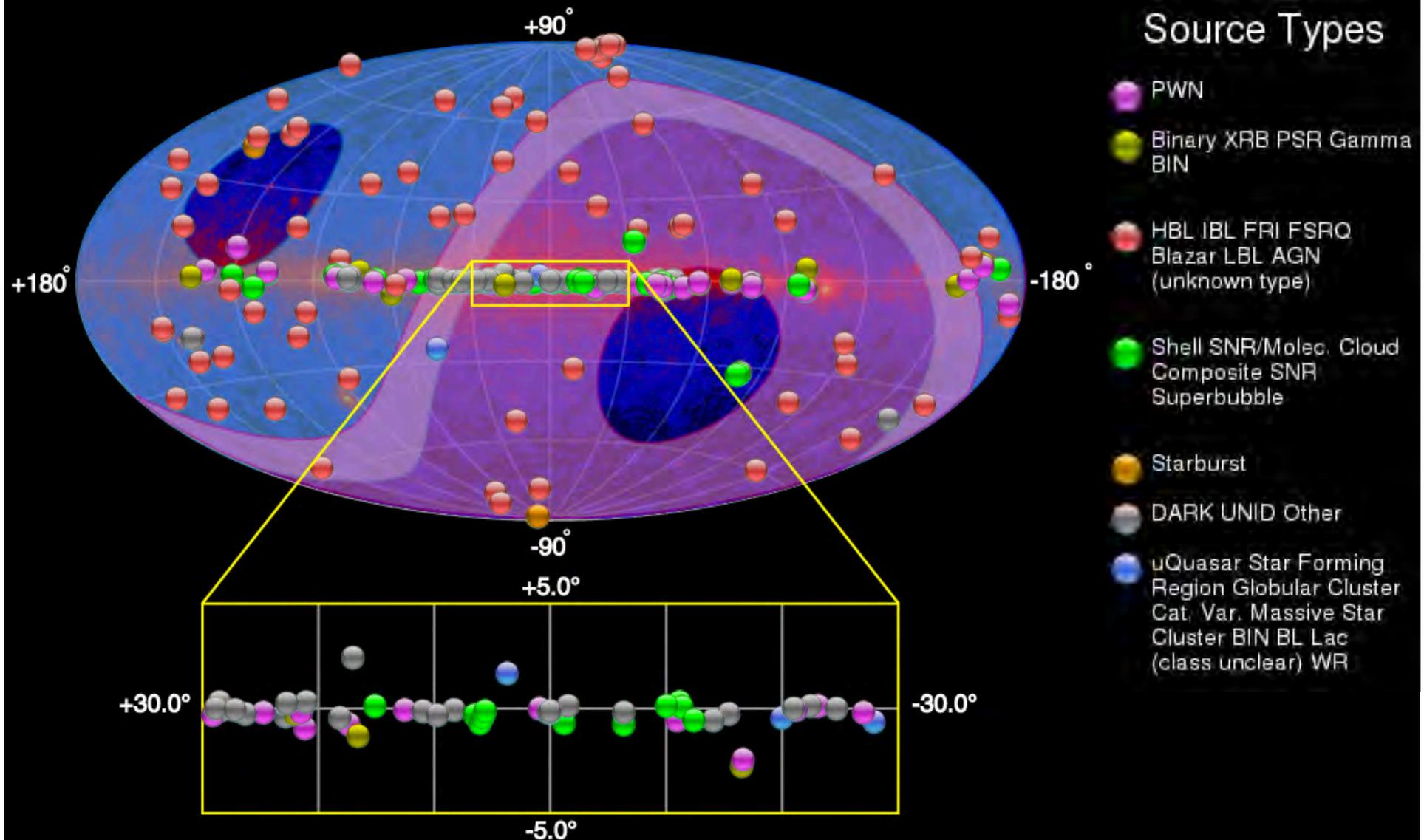
Active Galactic
Nuclei



Energies above the thermal regions

- (LE) or MeV : 0.1 (0.03) -100 (30) MeV
 - HE or GeV : 0.1 (0.03) -100 (30) GeV
 - VHE or TeV : 0.1 (0.03) - 100 (30) TeV
 - UHE or PeV : 0.1 (0.03) -100 (30) PeV
-
- LE,HE domain of space-based astronomy
 - VHE+ domain of ground-based astronomy
-
- When no ambiguity, we call “HE” all the HE and VHE+

>3k HE and >200 VHE photon emitters



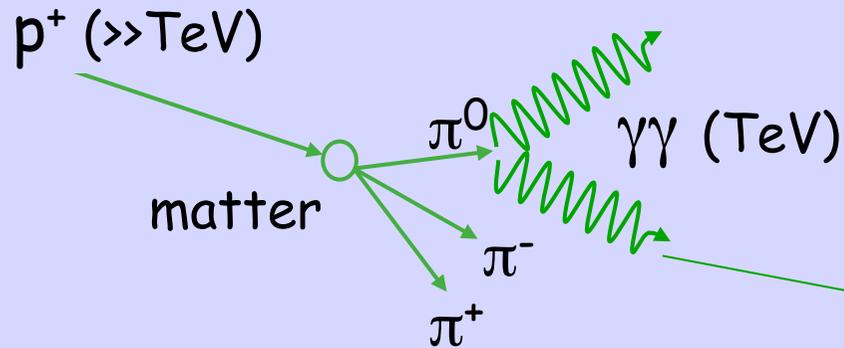
(1) Bottom-up: Interaction of accelerated particles with radiation and matter fields

- Gamma-ray production and absorption processes: several but well studied
- These phenomena generally proceed under extreme physical conditions in environments characterized by
 - huge gravitational, magnetic and electric fields,
 - very dense background radiation,
 - relativistic bulk motions (black-hole jets and pulsar winds)
 - shock waves, highly excited (turbulent) media, etc.
- They are related to, and their understanding requires knowledge of,
 - nuclear and particle physics,
 - quantum and classical electrodynamics,
 - special and general relativity,
 - plasma physics, (magneto) hydrodynamics, etc.
 - astronomy & astrophysics

Leptonic and hadronic production of gamma rays

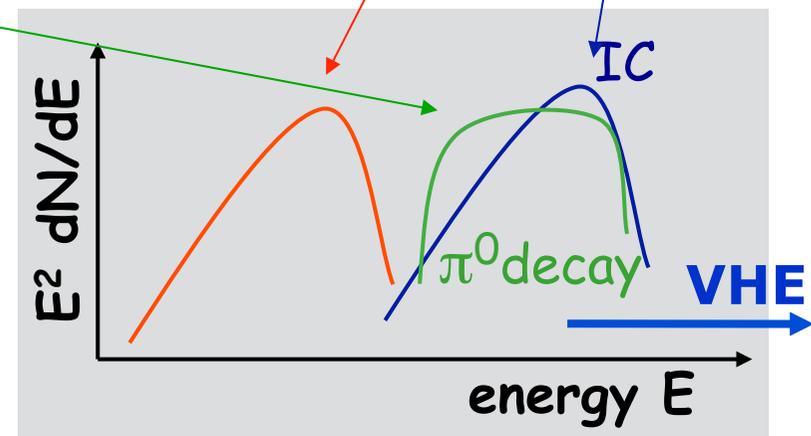
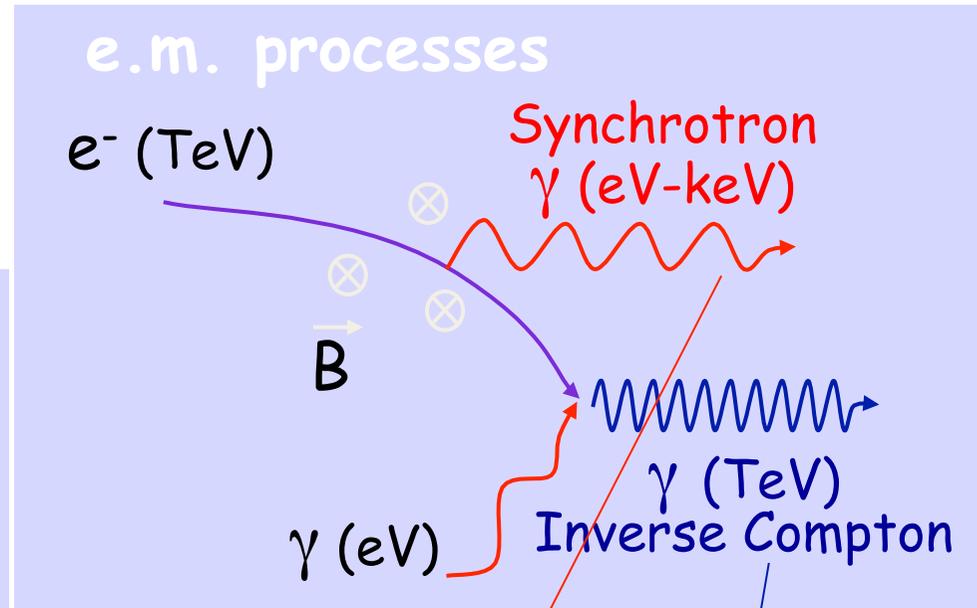
50 TeV gamma-rays hadronically produced track a population of protons of energy ~ 1 PeV

hadronic cascades

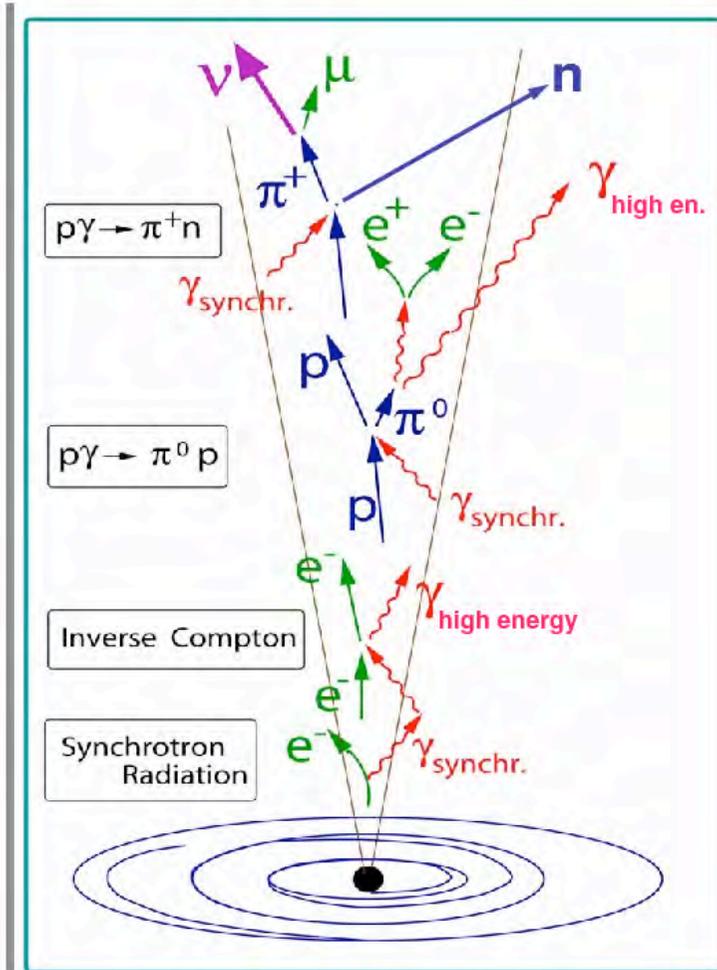


In the VHE region,
 $dN/dE \sim E^{-\Gamma}$ (Γ : spectral index)

To distinguish between hadron/leptonic origin study Spectral Energy Distribution (SED):
 (differential flux) $\cdot E^2$



The hadronic mechanism is at work also for neutrinos...



In a hadronic process (isospin symmetry)

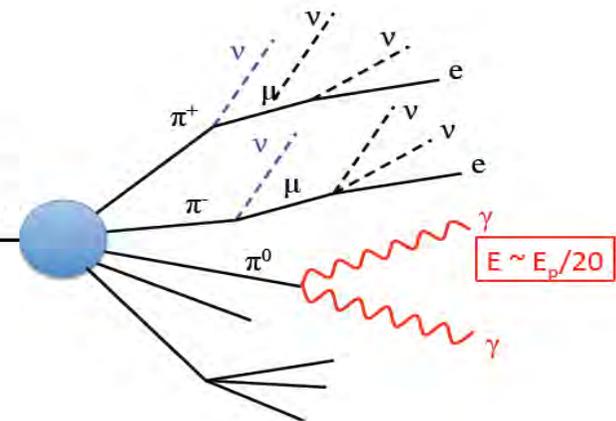
- $N(\pi^+) \sim N(\pi^-) \sim N(\pi^0)$ Same energies!

$$\pi^+ \rightarrow \mu^+ \nu$$

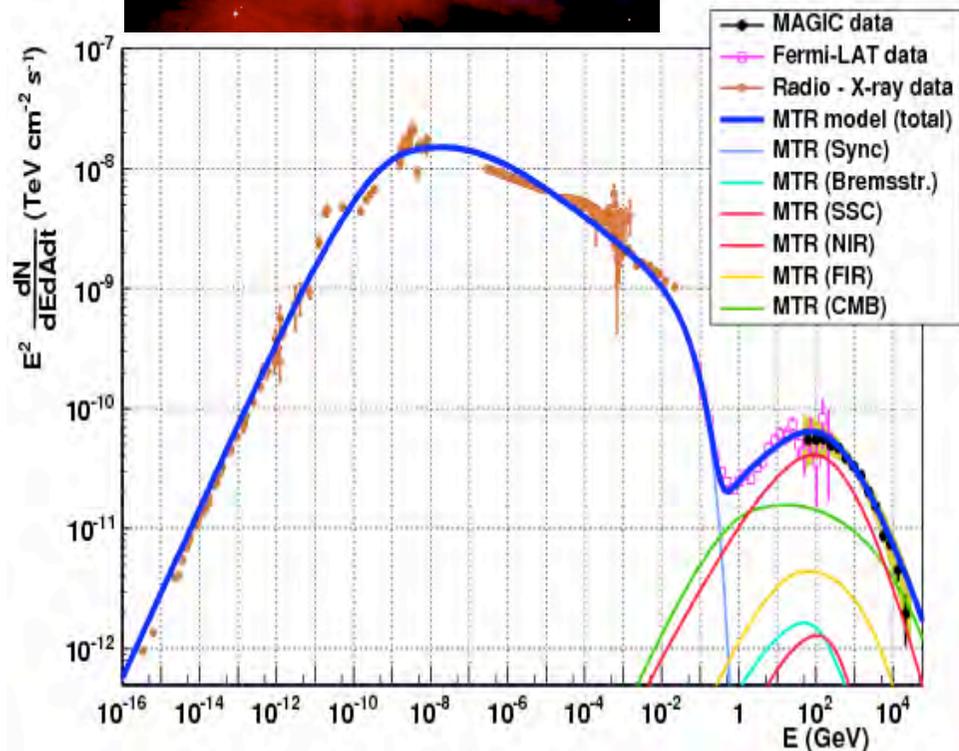
$$\pi^- \rightarrow \mu^- \nu$$

$$\pi^0 \rightarrow \gamma\gamma$$

Proton colliding with nucleus in molecular cloud or photon in field



A “typical” (V)HE γ source: Crab Nebula

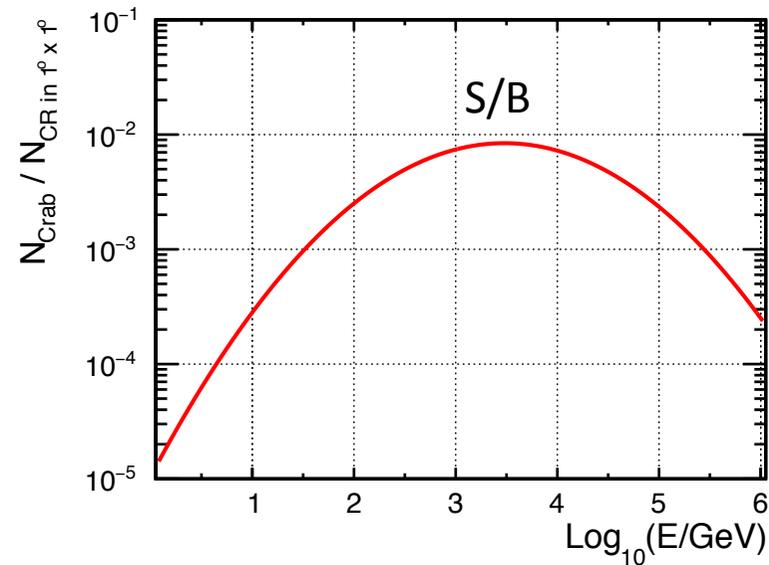
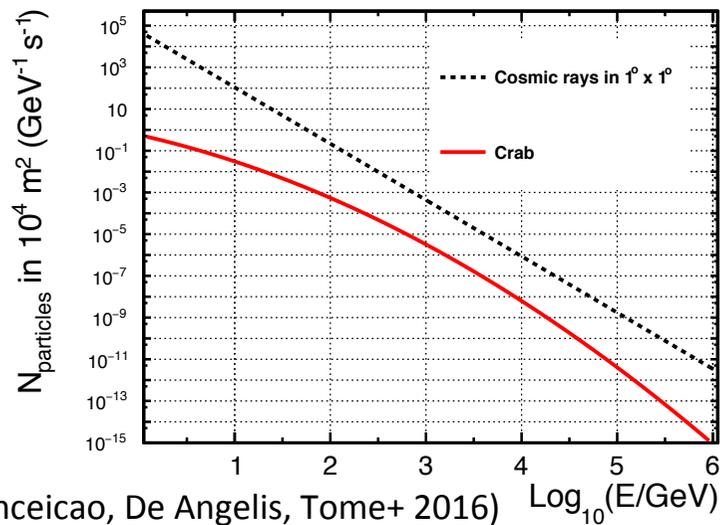


- The Crab Nebula is a nearby (~ 2 kpc away) PWN and the first source detected in VHE gamma-rays [Weekes 1989].
- It is the brightest steady VHE gamma-ray source, therefore it has become the so-called “standard candle” in VHE astronomy.
 - Recent observation of flares in the GeV range have however shown that occasionally the Crab flux can vary.

$$\frac{dN_\gamma}{dE} \simeq 3.23 \times 10^{-11} \left(\frac{E}{\text{TeV}} \right)^{-2.47-0.24\left(\frac{E}{\text{TeV}}\right)} \text{TeV}^{-1} \text{s}^{-1} \text{m}^{-2}$$

γ -ray detection: signal vs. background

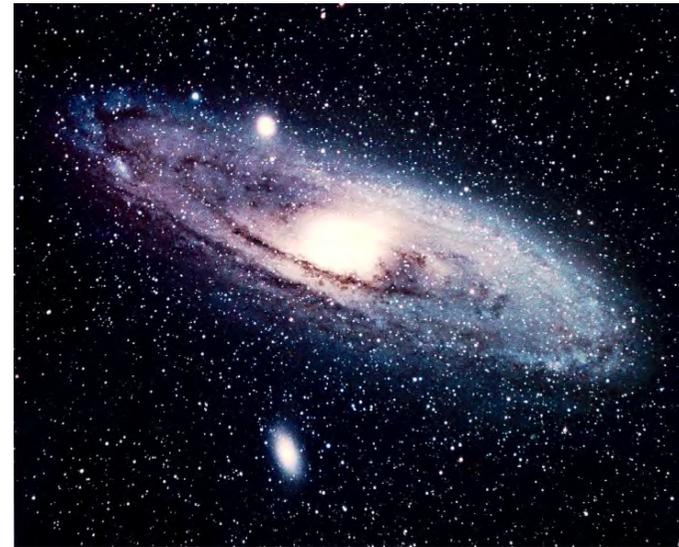
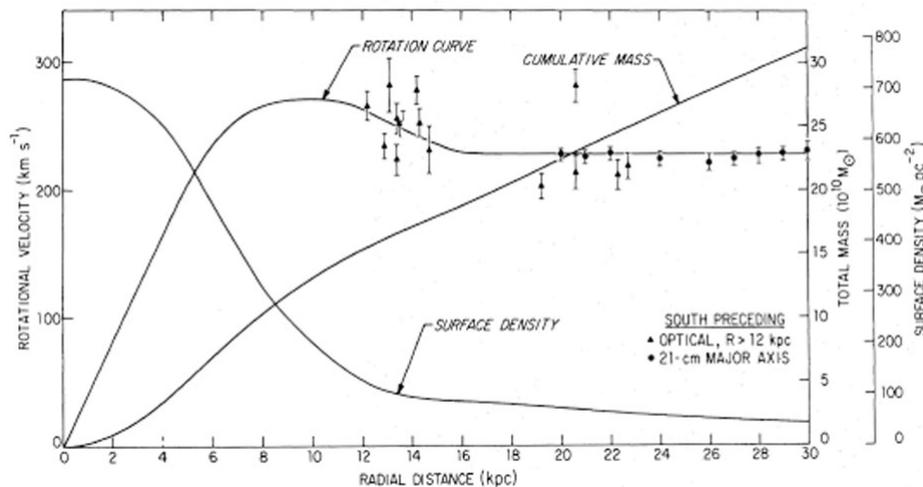
- Is Crab Nebula easy to detect?
- Suppose to have a $100 \times 100 \text{ m}^2$ detector with a resolution of 1 square degree:



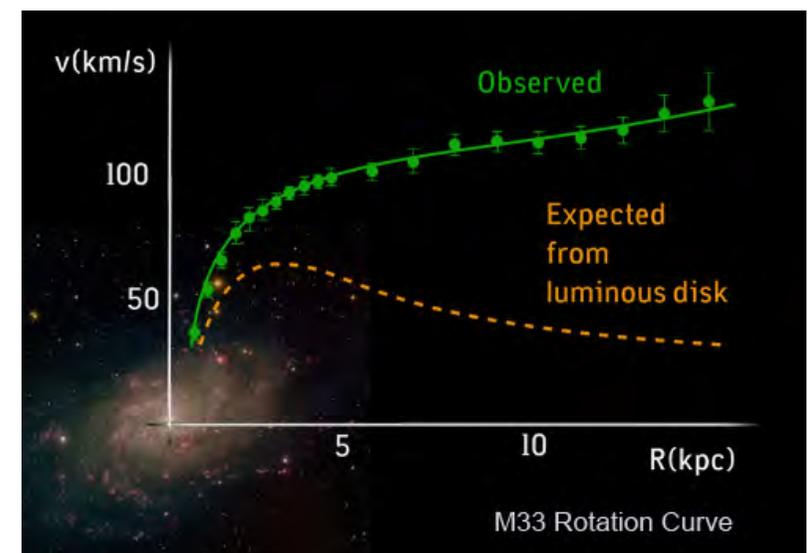
Conclusion: you need large effective area, good angular resolution, proton rejection

(2) Top-down: are there new (heavy) particles which can produce HE photons?

- Rotation curves of spiral galaxies



- flat at large radii: if light traced mass we would expect them to be Keplerian at large radii, $v \propto r^{-1/2}$, because the light is concentrated in the central bulge
 - and disc light falls off exponentially
 - Zwicky had already noted in 1933 that the velocities of galaxies in the Coma cluster were too high to be consistent with a bound system
 - Observed for many galaxies, including the Milky Way



The currently favored solution

To assume that in and around the Galaxies there is

Dark Matter

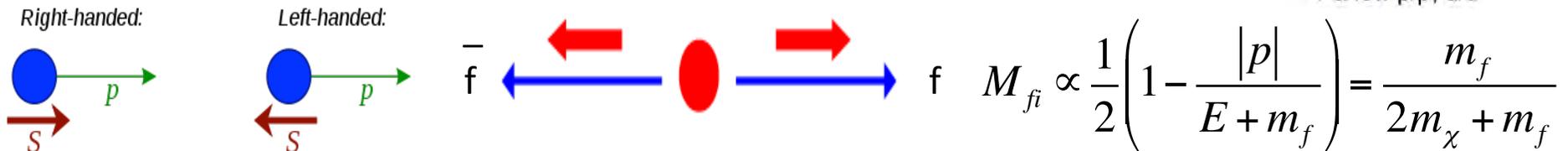
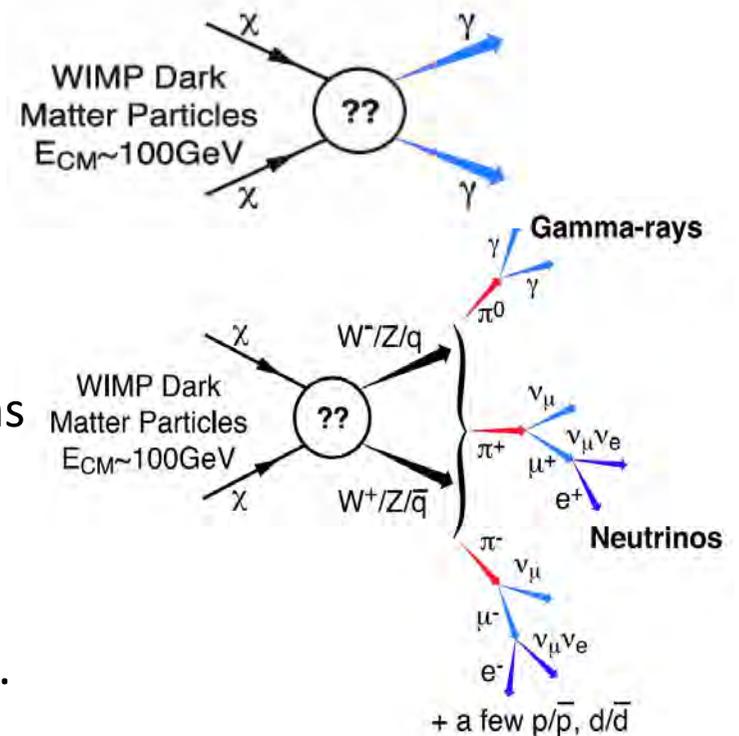
subject to gravitational interaction but no electromagnetic interaction

$$M(r) \propto r \Rightarrow v_{rot} = \sqrt{\frac{GM(r)}{r}} = const.$$

- Must be “cold”, i.e., non-relativistic (it is trapped by the gravitational field), and “weakly” interacting: **WIMP**
- The hypothesis is not odd: remember that the existence of Neptune was suggested on the basis of the irregular motions of Uranus
- **How much DM do we need? results to be 5 times more than luminous matter (astrophysics, evolution of the Universe)**

How do WIMPs produce photons?

- The energy “blob” from $\chi\chi$ annihilation might decay:
 - Directly into 2γ , or into $Z\gamma$ if kinematically allowed. Clear experimental signature (photon line), but not very likely (requires one loop). In SUSY, the BR depends on what is the lightest neutralino composition.
 - Into a generic $f\text{-}\bar{f}$ pair, then generating a hadronic cascade with π^0 decaying into photons in the final state. Remind that flavors are left-handed and anti-flavors are right-handed with amplitude $[1+|p|/(E+m_f)]/2 \sim v/c$, and in this case for an s-wave you need to “force” one of the decay products to have the “wrong” elicity.



=> The $\chi\chi$ pair will prefer to decay into the heaviest available pair – i.e., if $20 \text{ GeV} < m_\chi < 80 \text{ GeV}$, into $b\text{-}\bar{b}$

III- Propagation

Propagation of charged CR in the Universe

- Gyroradius

B in the Galaxy: a few μG ; outside the Galaxy: $1\text{nG} > B > 1\text{fG}$

- If you want to look at the GC ($d \sim 8\text{ kpc}$) you need $E > 2 \cdot 10^{19}\text{ eV}$

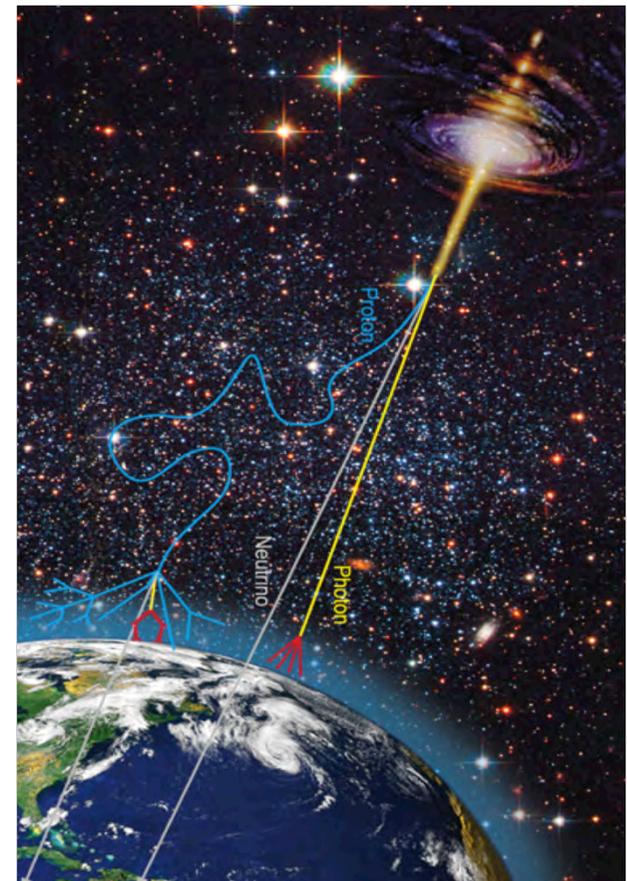
- But only 1 particle / km^2 / year
- *And no galactic emitters expected at this energy*

- But in principle one could look outside the galaxy, were B is smaller and there are SMBHs...

- *No: the resonant interaction with the CMB (GZK effect) provides a cutoff at $E \sim 10^{19}\text{ eV}$*

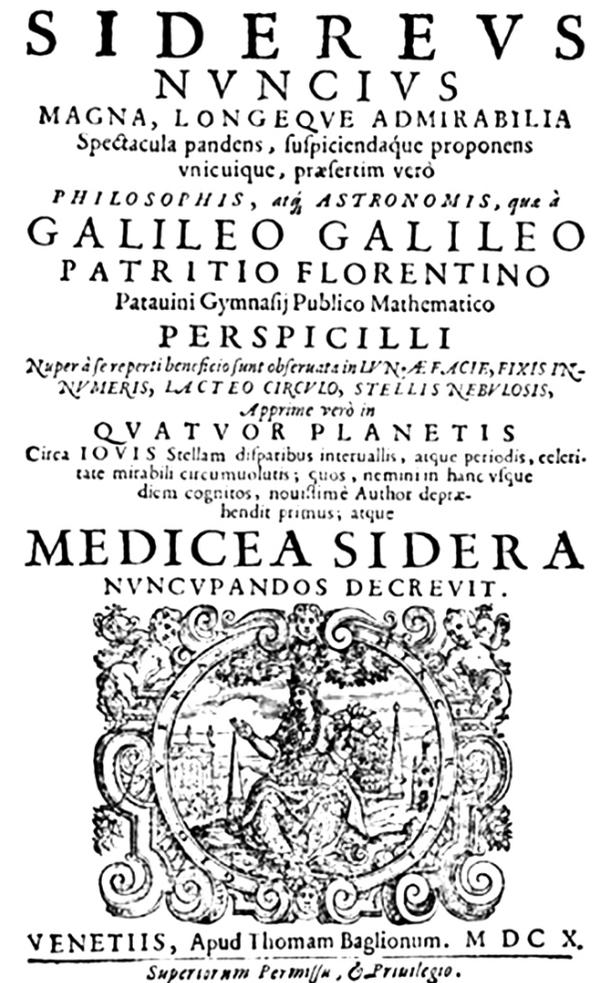
- **Conclusion: extremely difficult to use charged CR for astrophysics**

$$\frac{r}{1\text{ pc}} \approx \frac{E}{1\text{ PeV}} \frac{1\text{ }\mu\text{G}}{B}$$



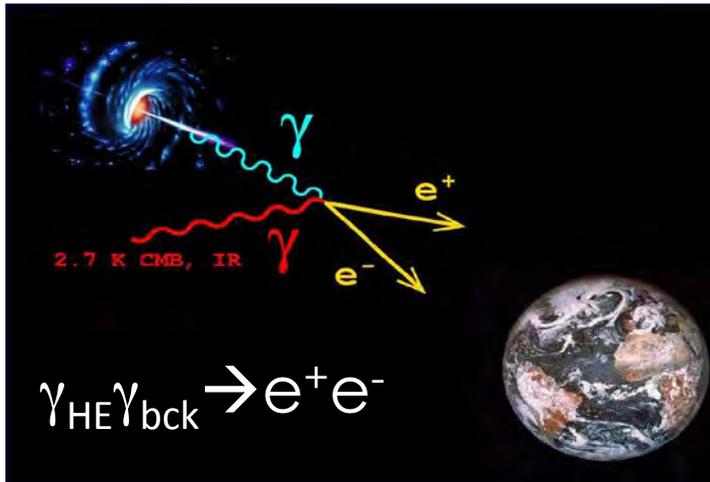
Neutral messengers must be used for astronomy & astrophysics

- Neutrinos: very difficult to detect due to the small interaction cross section (despite a km^3 detector in Antarctica, the only cosmic sources localized up to now are SN1987A, the Sun, and the Earth)
 - <10 neutrinos per year from astrophysical sources identified by IceCube (1km^3)!
- Gravitational waves: just started
- Photons: they have a long tradition in astronomy since millennia... And they are the “starry messengers” by default since 1610 at latest...



IIIa- Propagation of photons

Attenuation of γ -rays



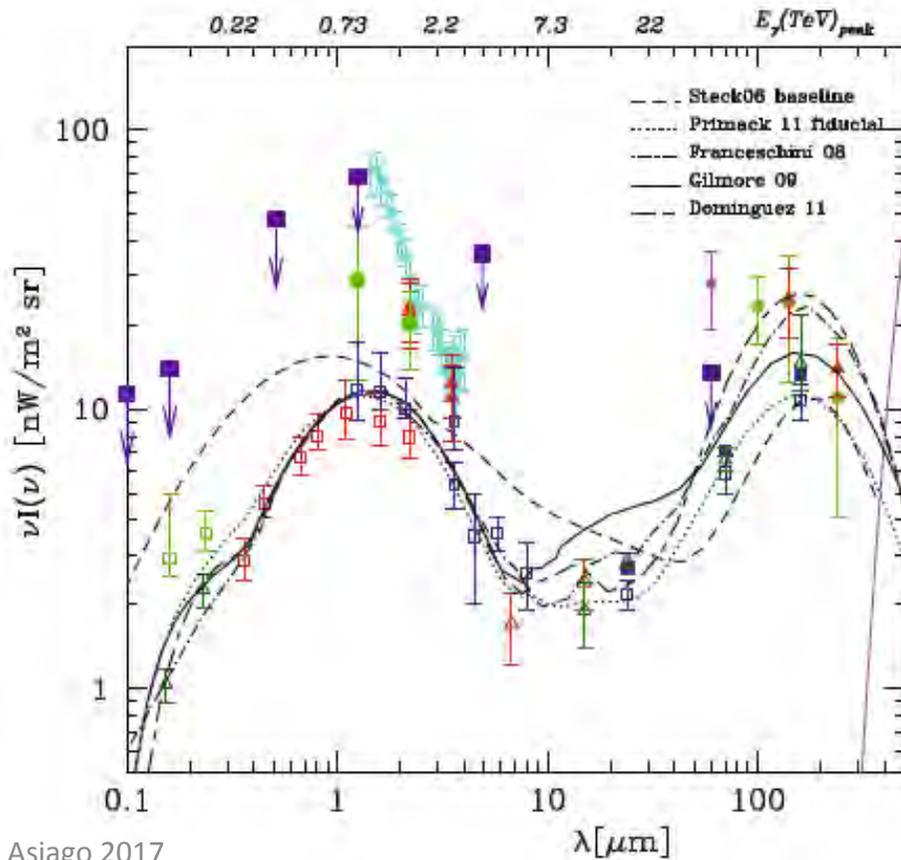
- γ -rays are effectively produced in EM and hadronic interactions
 - Energy spectrum at sources E^{-2}
- are effectively detected by space- and ground-based instruments
- effectively interact with matter, radiation ($\gamma\gamma \rightarrow e^+e^-$) and B-fields
- The interaction with background photons in the Universe attenuates the flux of gamma rays
- The “enemies” of VHE photons are photons near the optical region (Extragalactic Background Light, EBL)

$$\gamma_{\text{VHE}} \gamma_{\text{bck}} \rightarrow e^+ e^-$$

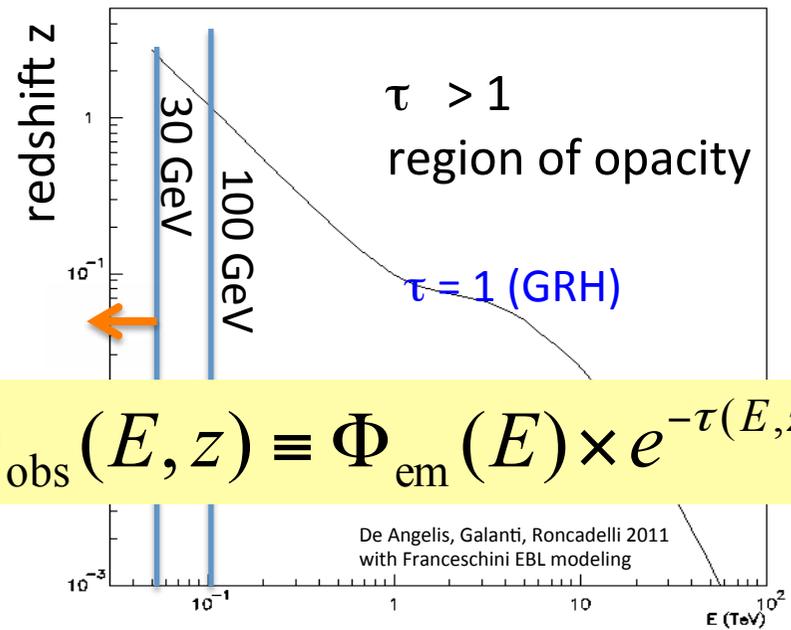
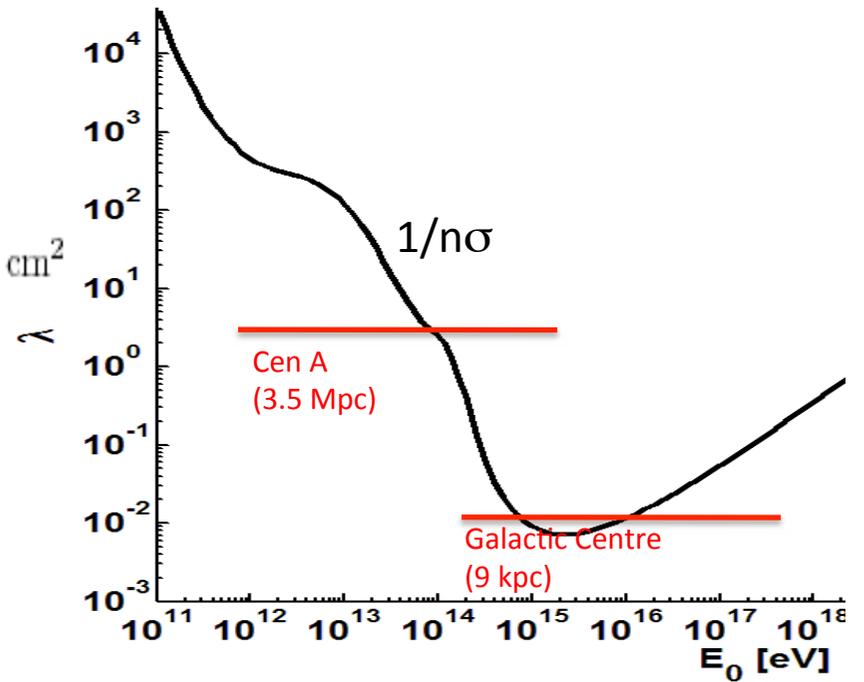
$$\sigma(\beta) \sim 1.25 \cdot 10^{-25} (1 - \beta^2) \cdot \left[2\beta(\beta^2 - 2) + (3 - \beta^4) \ln \left(\frac{1 + \beta}{1 - \beta} \right) \right] \text{cm}^2$$

Max for:

$$\epsilon \simeq \frac{2m_e^2 c^4}{E} \simeq \left(\frac{500 \text{ GeV}}{E} \right) \text{eV}$$



Asiago 2017

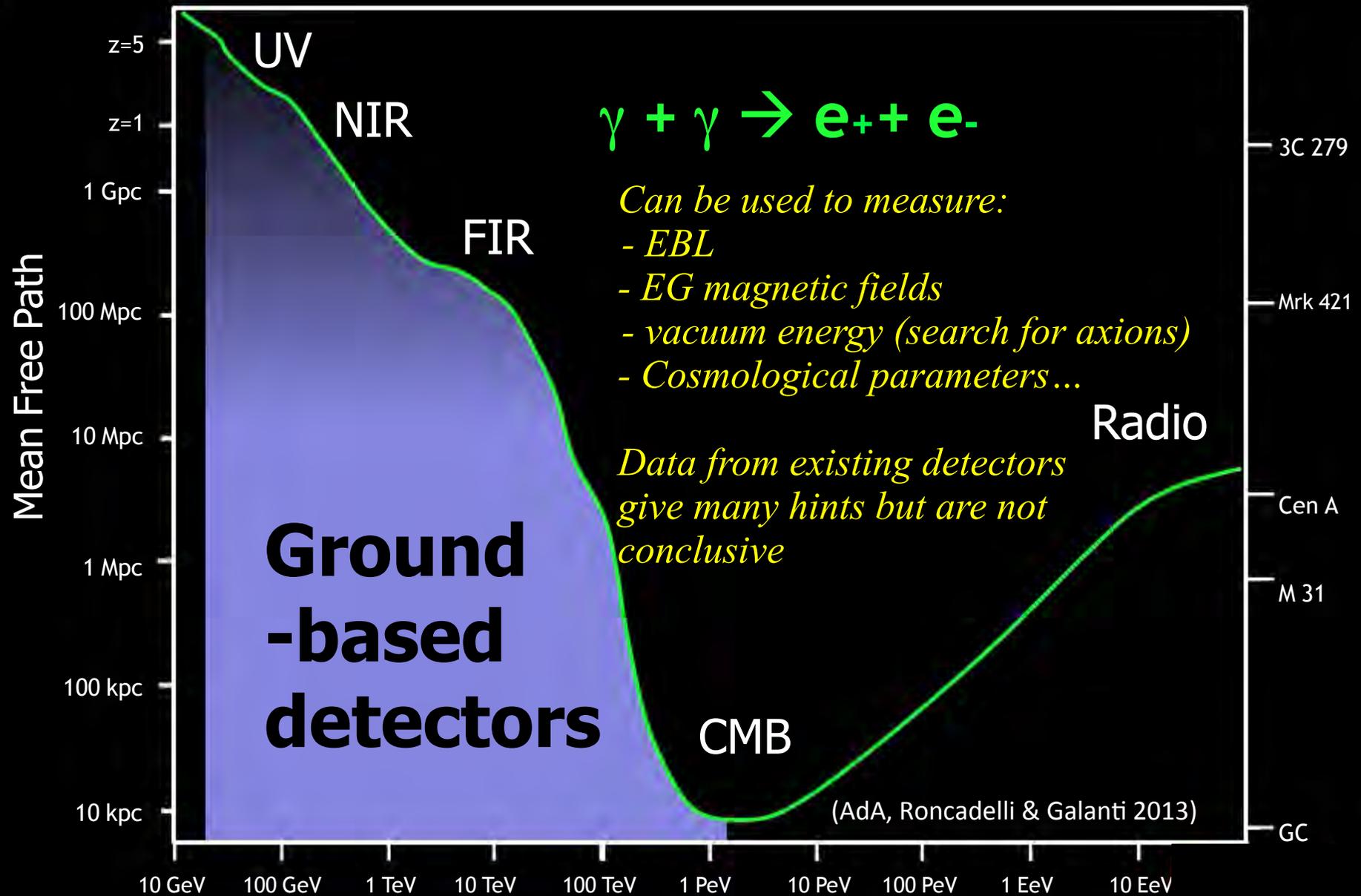


$$\Phi_{\text{obs}}(E, z) \equiv \Phi_{\text{em}}(E) \times e^{-\tau(E, z)}$$

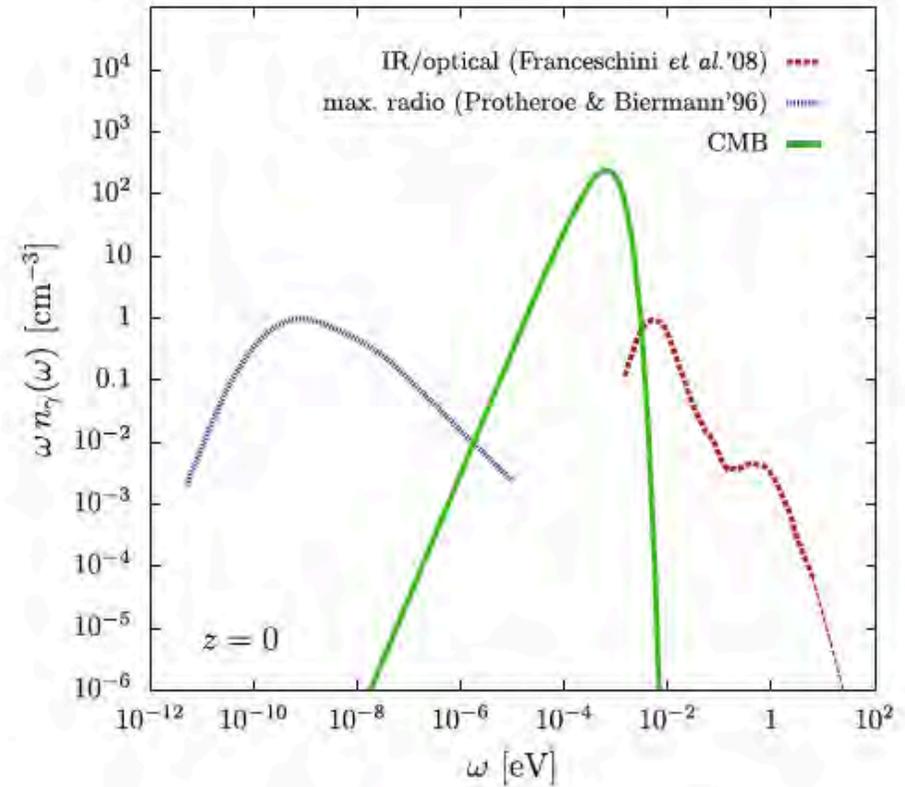
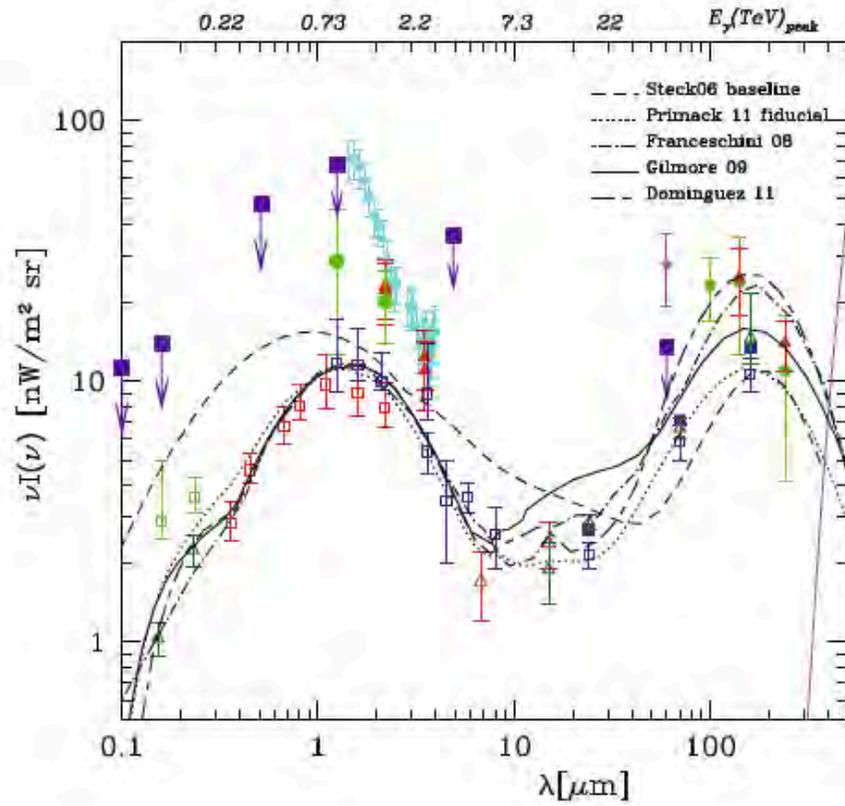
γ ray energy (TeV)

- The diffuse extragalactic background light (EBL) is all the accumulated radiation in the Universe due essentially to star formation processes
- This radiation covers a wavelength range between ~ 0.1 and $600 \mu\text{m}$ (consider the redshift and the reprocessing)
- After the CMB, the EBL is the second-most energetic diffuse background
- The understanding of the EBL is fundamental
 - To know the history of star formation
 - To model VHE photon propagation for extragalactic VHE astronomy. VHE photons coming from cosmological distances are attenuated by pair production with EBL photons. This interaction is dependent on the SED of the EBL.
- Therefore, it is necessary to know the SED of the EBL in order to study intrinsic properties of the emission in the VHE sources.

The γ horizon: nuisance and resource

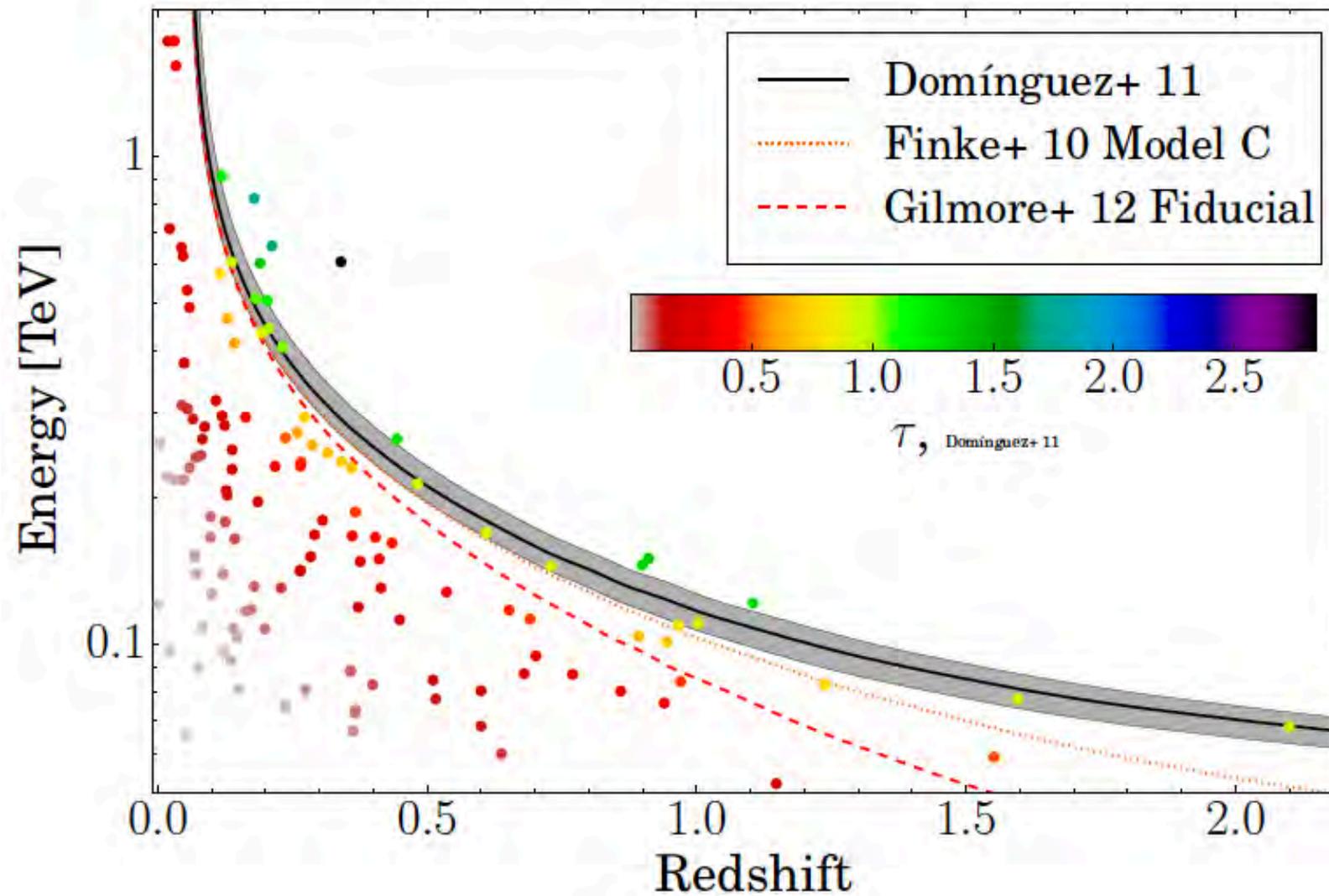


EBL

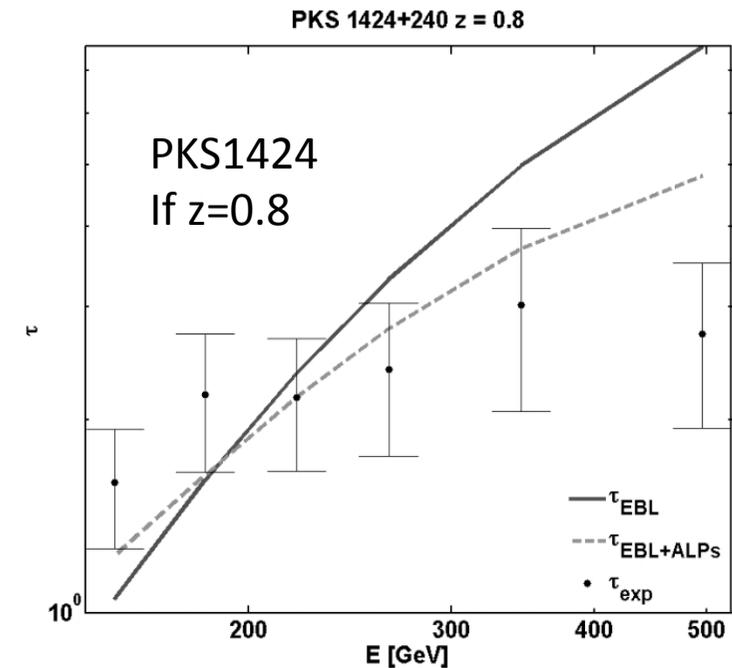
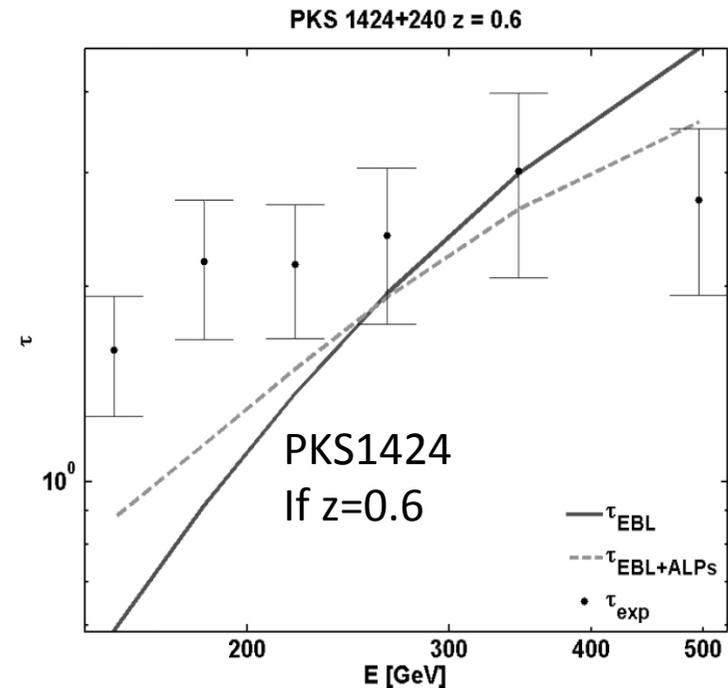
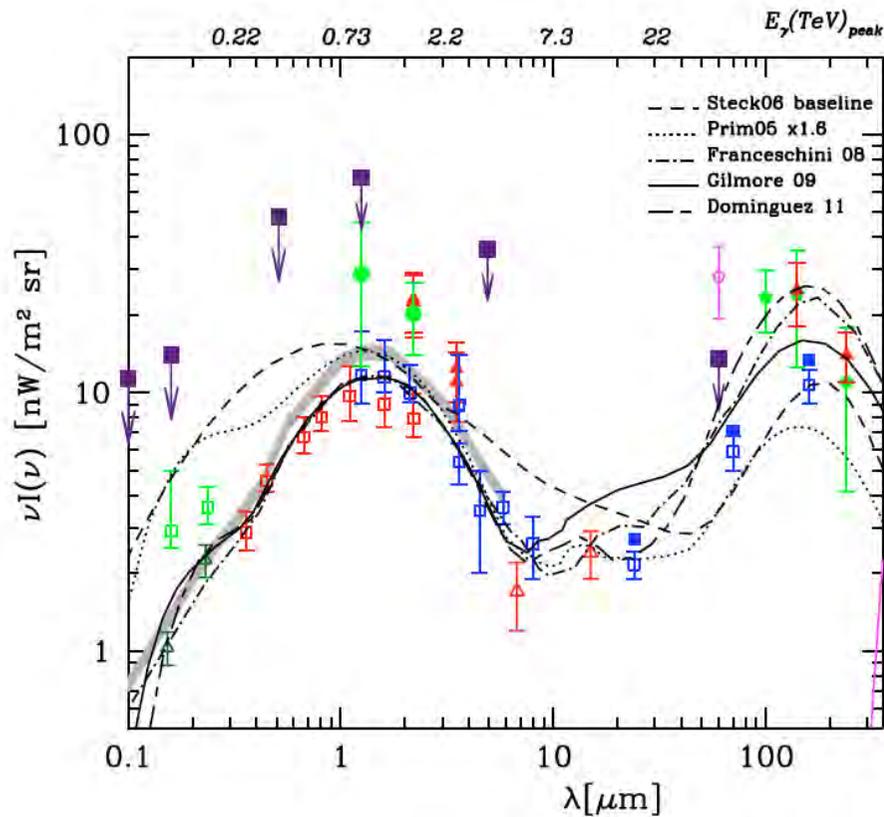


The EBL affects in particular the signal from extragalactic sources

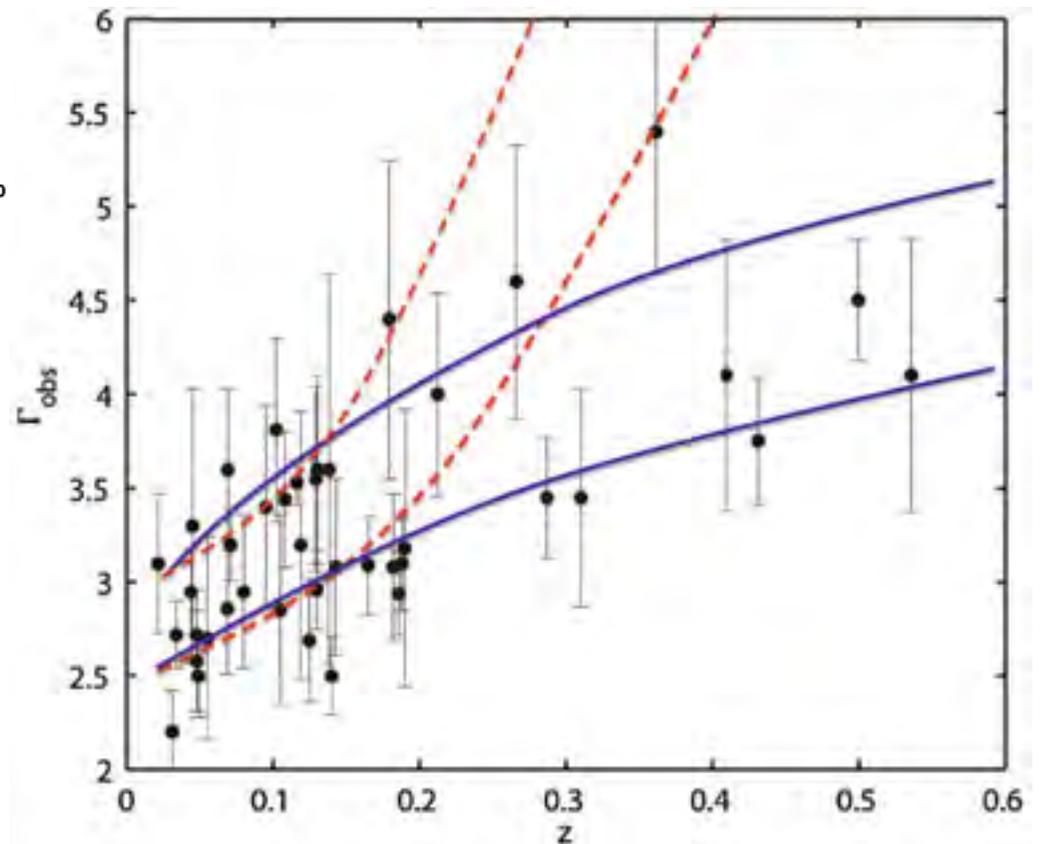
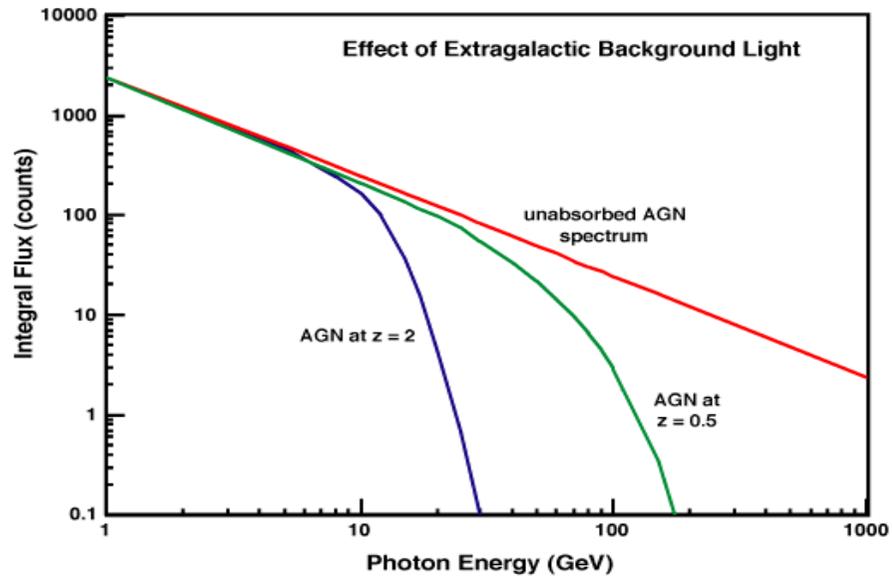
Fermi 2FHL and gamma horizon



A reminder: EBL rather well constrained, and SED extrapolation from Fermi is possible

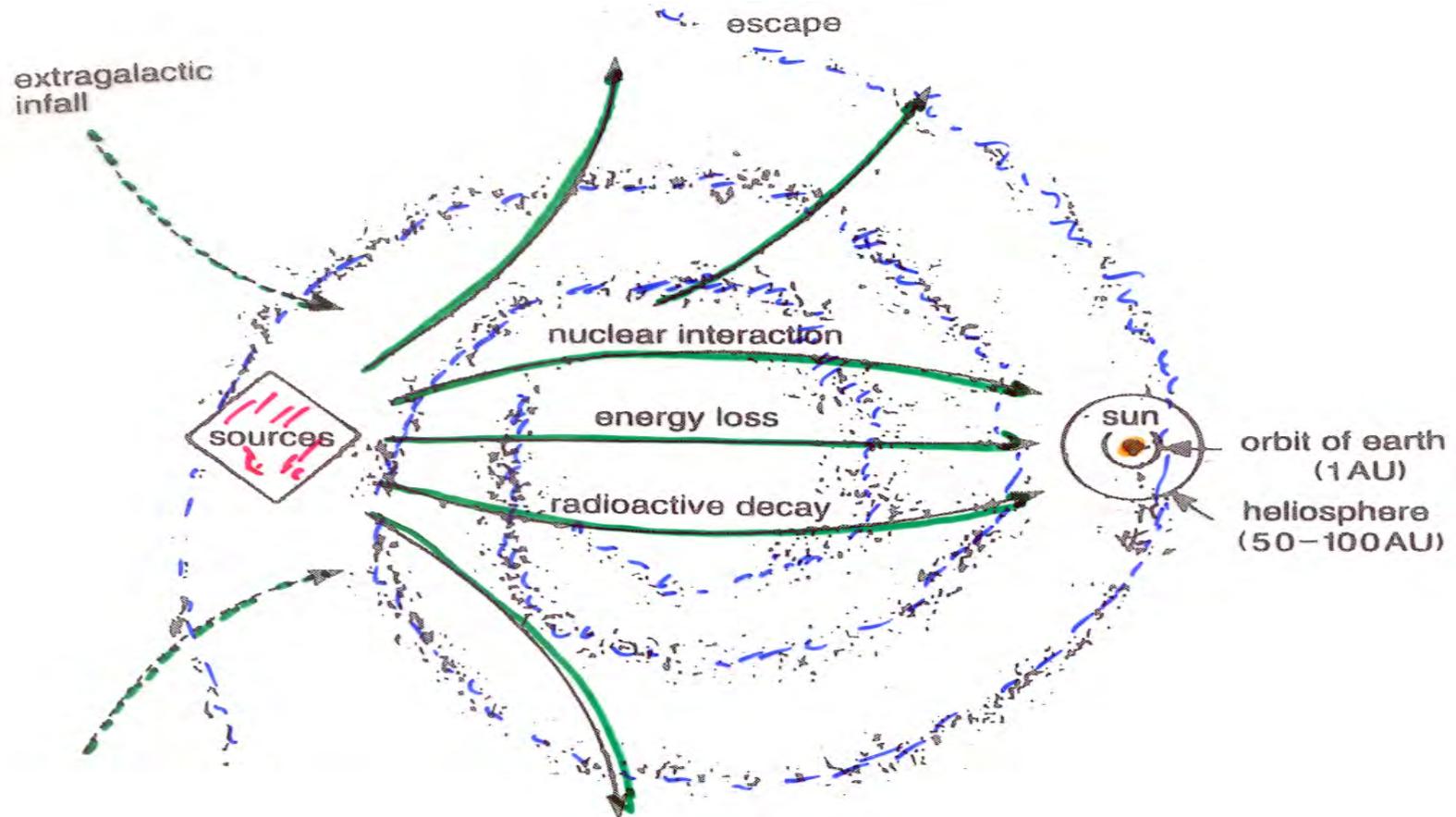


Spectral index of AGN



IIIb- Propagation of charged particles

The propagation in our galactic

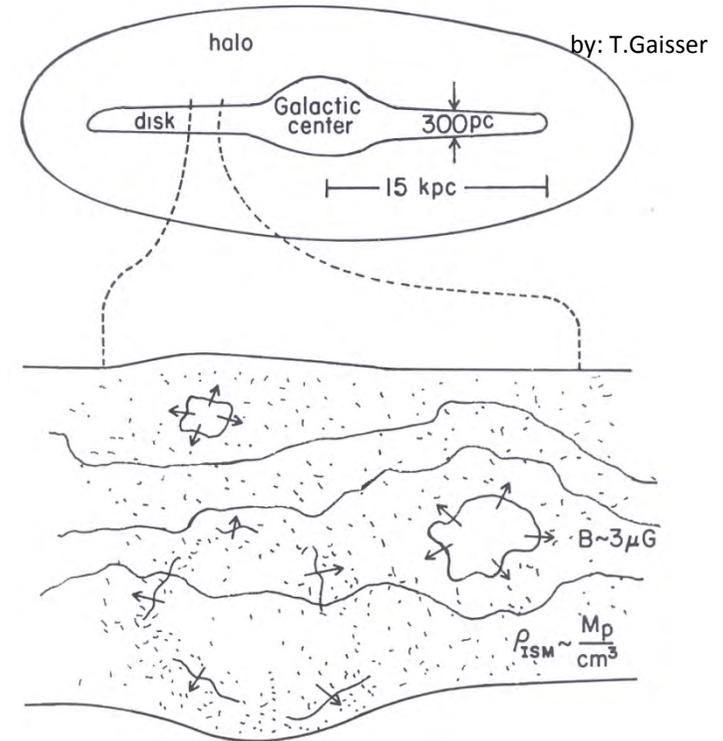
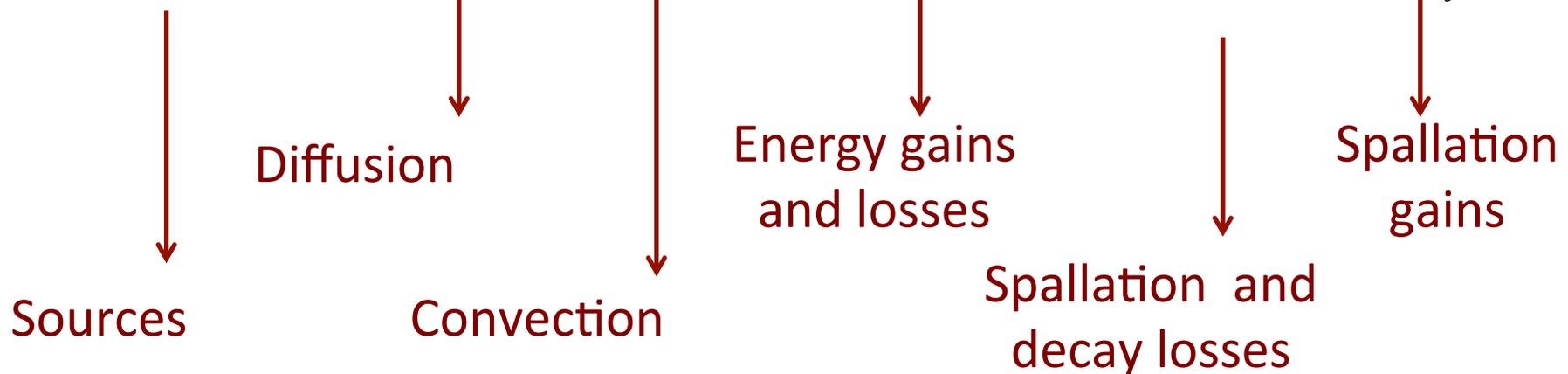


Propagation

Charged cosmic rays diffuse and interact in the Galactic randomly magnetized ISM . Confinement times are quite long ($\tau \sim 10^7$ years) and directions become basically isotropic.

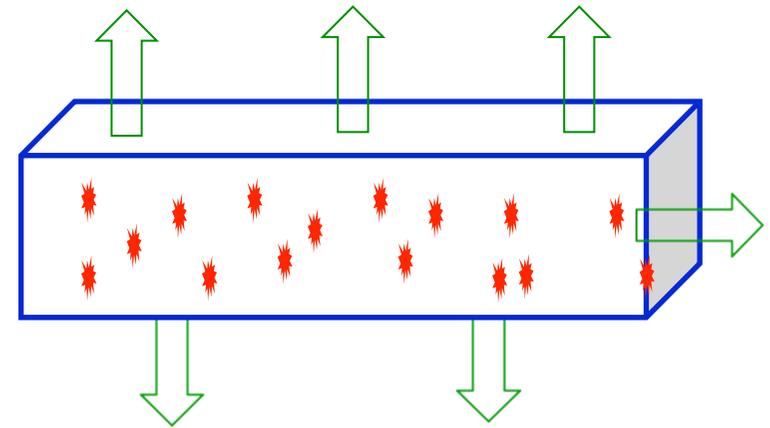
Transport equation :

$$\frac{\partial N_i}{\partial t} = Q_i + \vec{\nabla} \cdot (D \vec{\nabla} N_i - \vec{V} N_i) + \frac{\partial}{\partial E} (b(E) N_i) - \frac{N_i}{\tau_i} + \sum_{j>i} \frac{P_{ji} N_j}{\tau_j}$$



Leaky-Box

A box where charged cosmic rays freely propagates having however some probability to escape by the walls. The sources are uniformly distributed.



Simplified stationary equation :

$$0 = Q_i + \sum_{j>i} N_j \left\{ \rho\beta c \sigma_{ji}^{spall} + \frac{1}{\gamma\tau_{ji}^{decay}} \right\} - N_i \left\{ \rho\beta c \sigma_i^{spall} + \frac{1}{\gamma\tau_i^{decay}} + \frac{1}{\tau_i^{esc}} \right\}$$

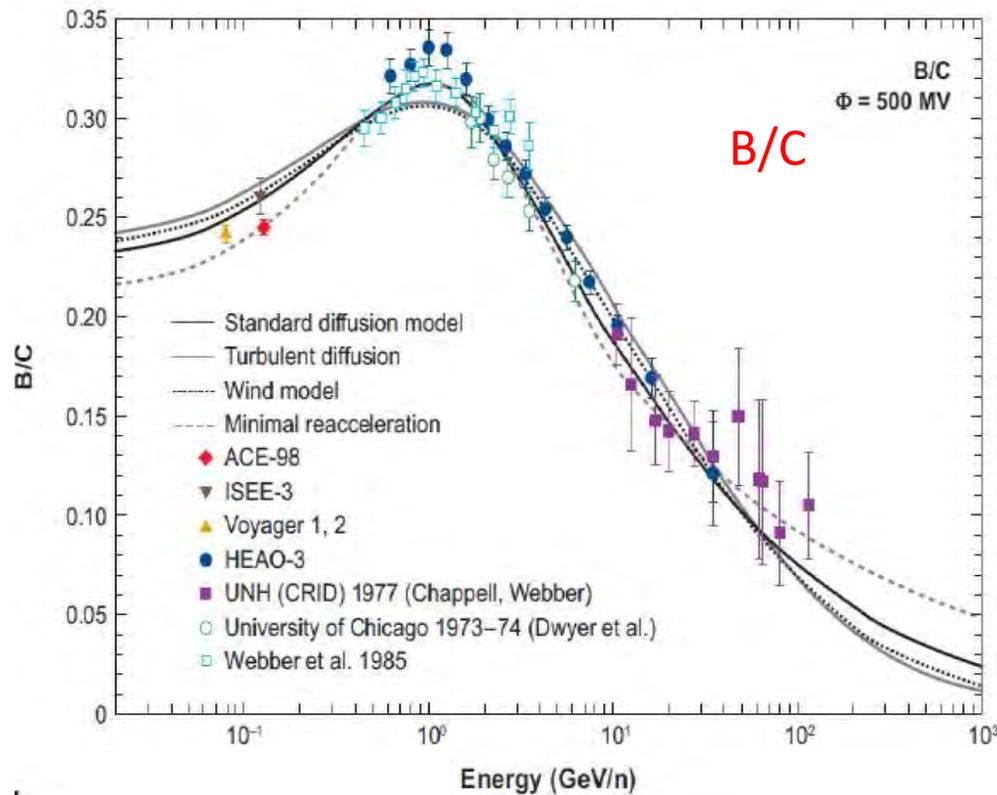
Sources

Spallation and
decays gains

Spallation, decays
and escape losses

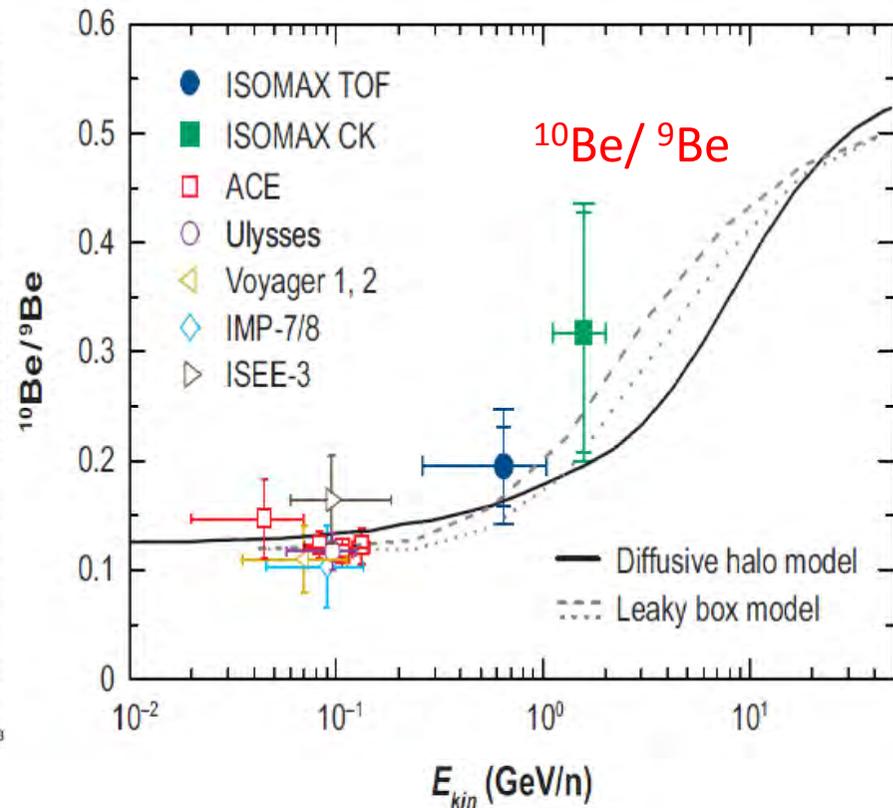
Constraining propagation models

Secondary/primary ratios



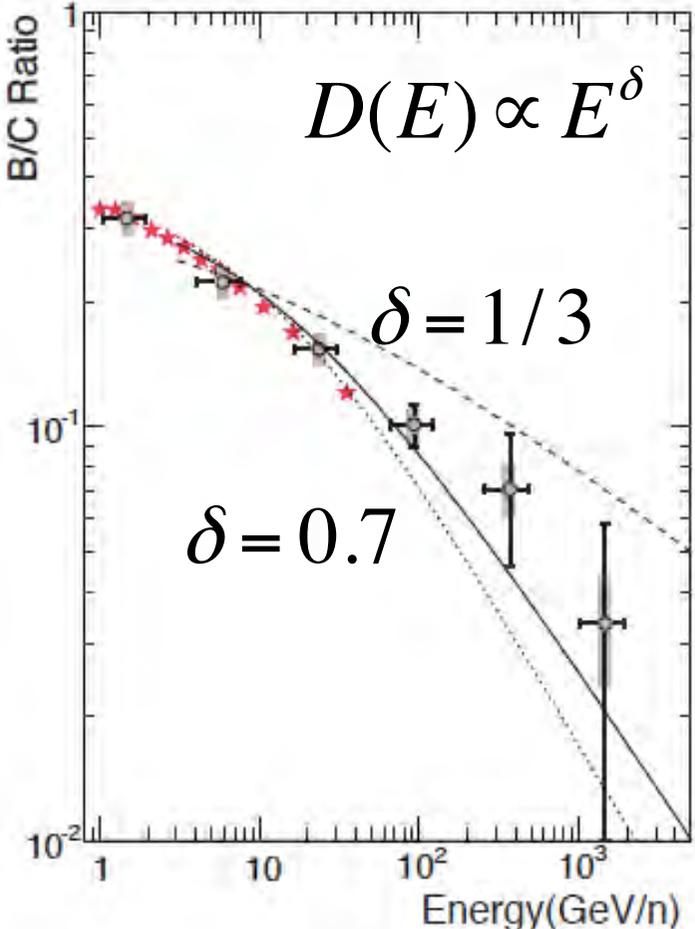
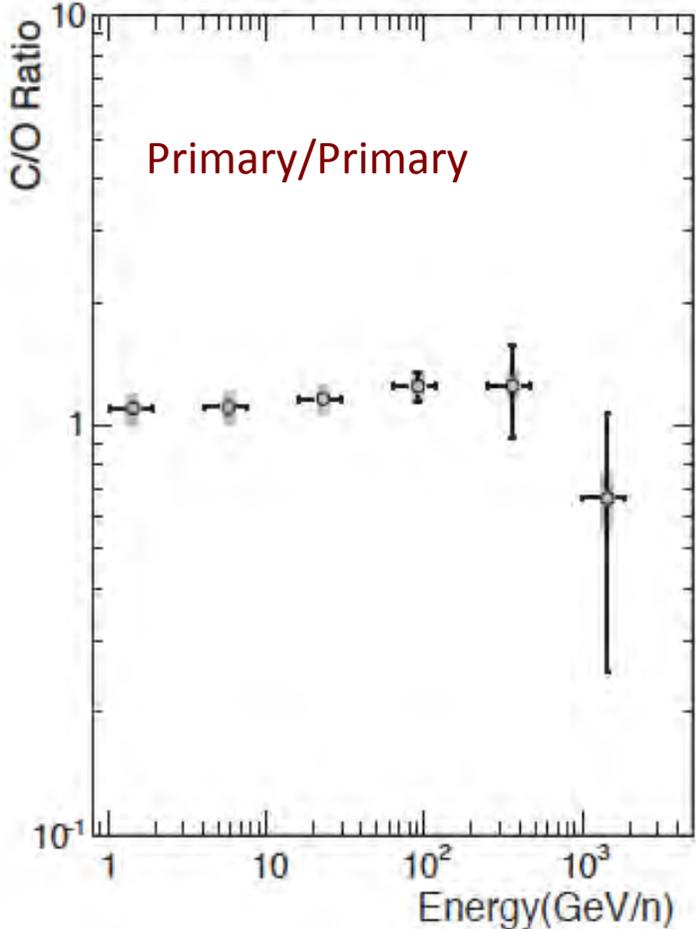
Box size, Diffusion coef.,
escape time, ...

Unstable/stable isotopos



Radioactive clocks

Energy dependence (τ_{sc})



Confinement and composition

Magnetic Field:

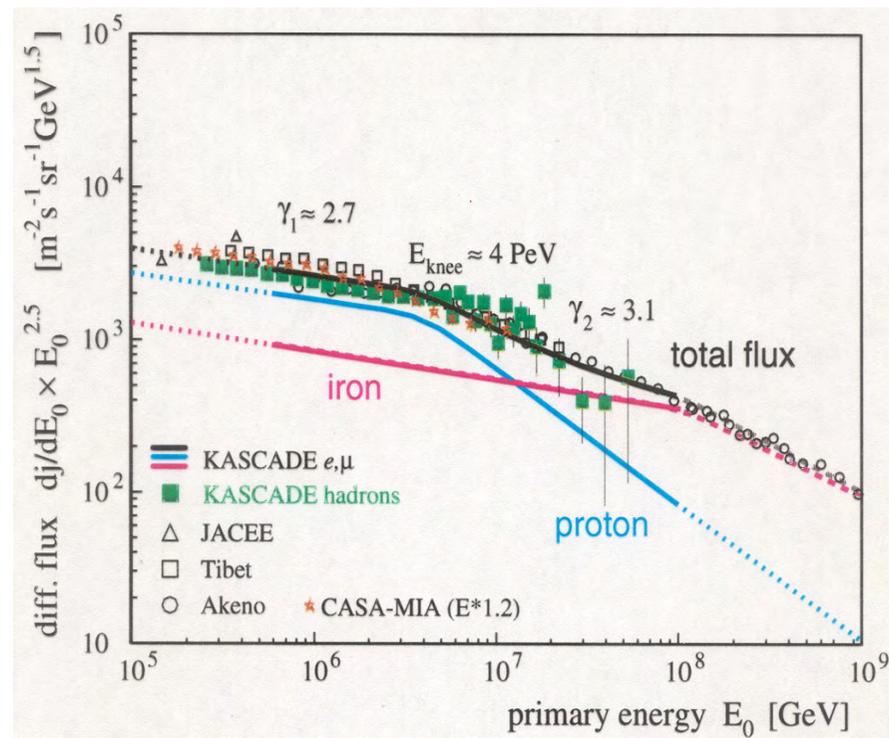
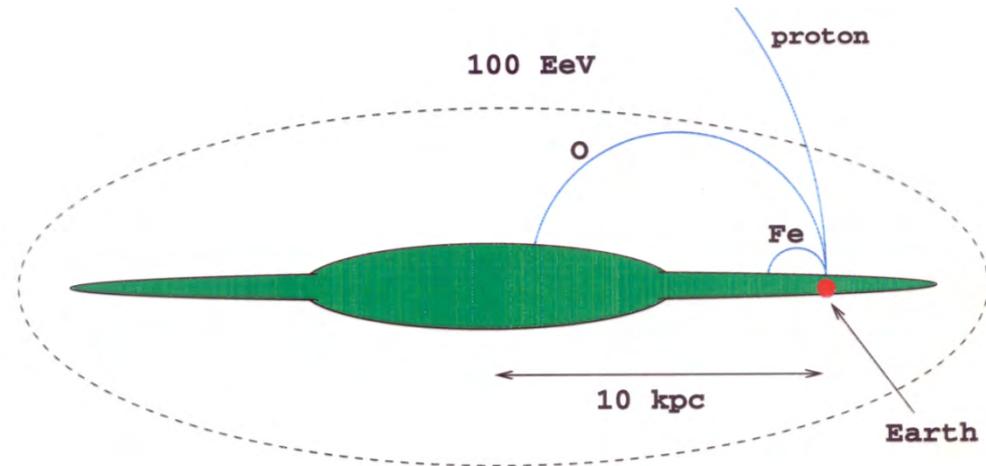
Galactic $\sim 1\text{-}3 \mu\text{G}$

Intergalactic $1 \text{ nG} > B > 1 \text{ fG}$

Larmor Radius:

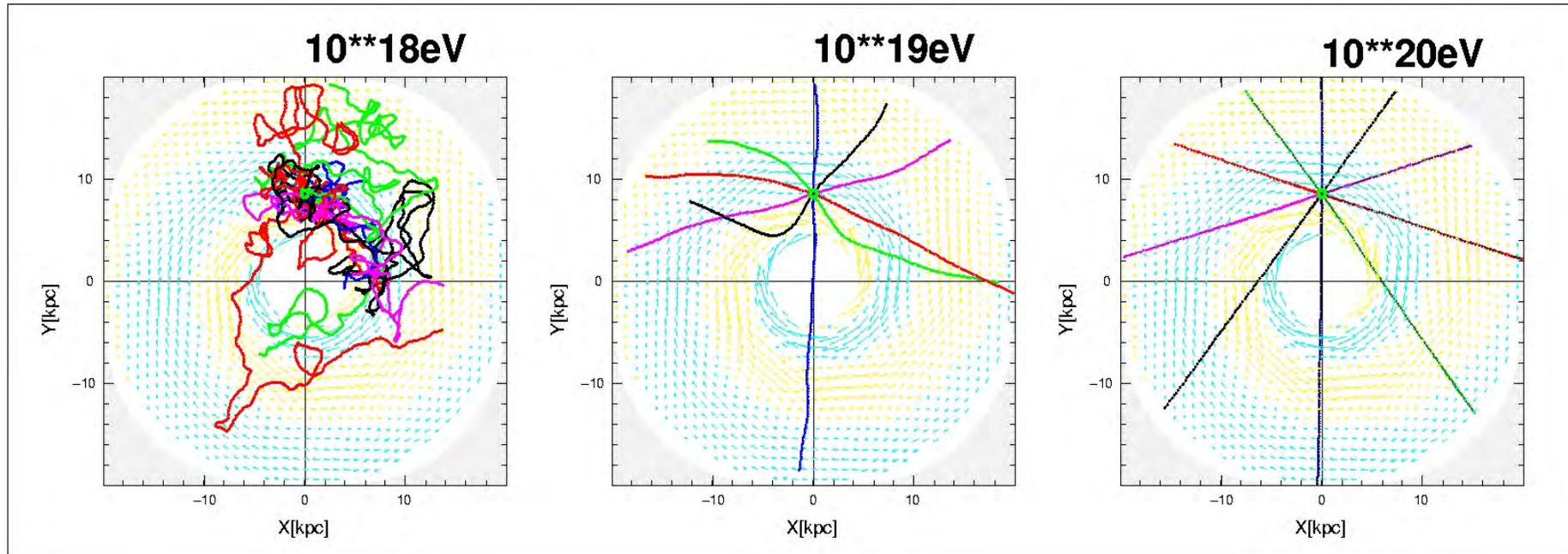
$$R = \frac{E}{ZeB}$$

Several knees?



Galactic Magnetic Field deflection (p)

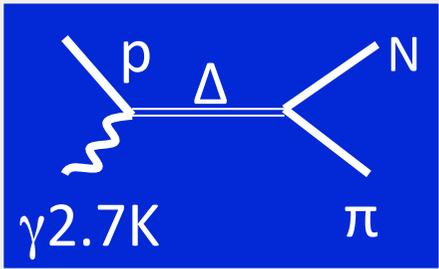
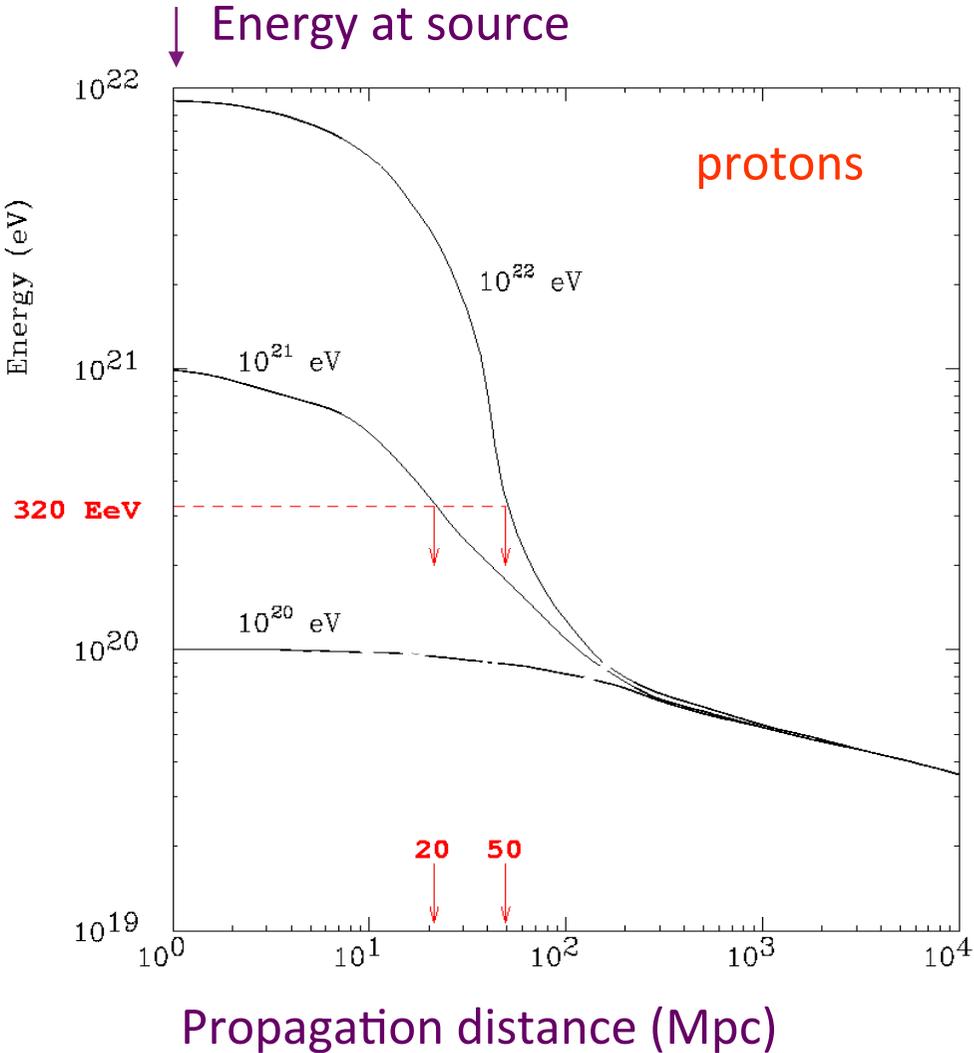
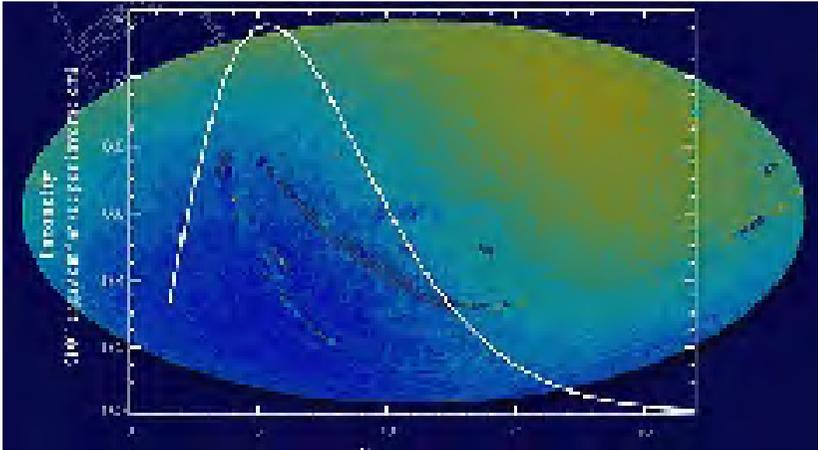
T.Stanev



Above 10^{19} : Astronomy !

An unique opportunity to measure the galactic magnetic field ?

The Greisen-Zatsepin-Kuzmin (GZK) cutoff



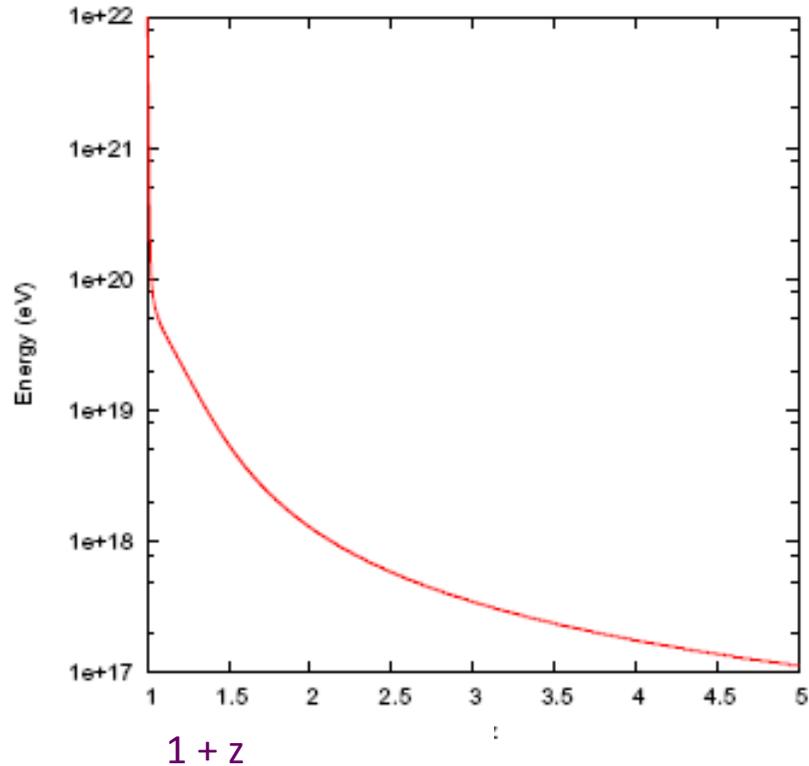
$$E_p \approx 10^{20} \text{ eV}$$

$$\lambda = \frac{1}{\sigma_{p\gamma} \rho_{CMB}}$$

$$\approx 6 \text{ Mpc}$$

GZK is model dependent

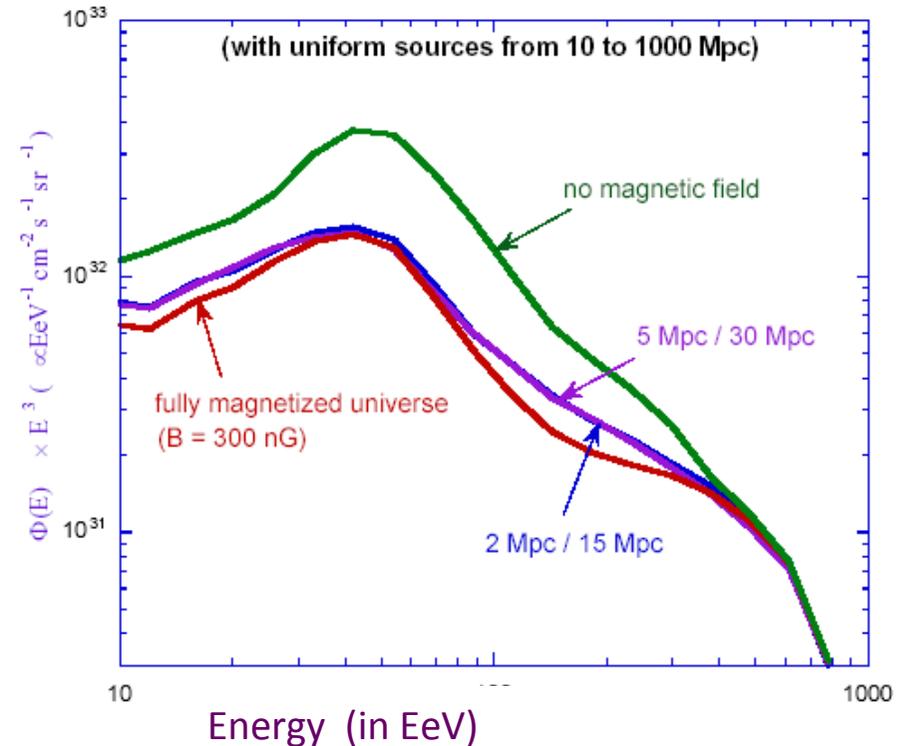
GZK cutoff Energy – Stecker and Scully



Sources type and
distribution
Primary composition

Magnetic fields

GZK and magnetic fields (protons)
Deligny, Parizot, Letessier-Selvon



Not a true cutoff !

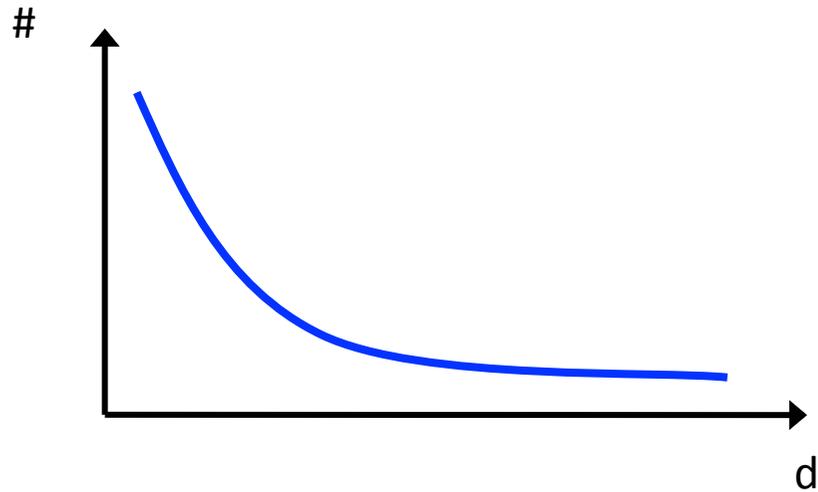
Pileup

Recovery of the spectrum
at higher energies ?

Particle showers

Pierre Auger, 1938

Coincidences

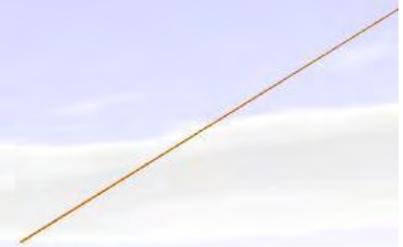


First shower energy estimates !

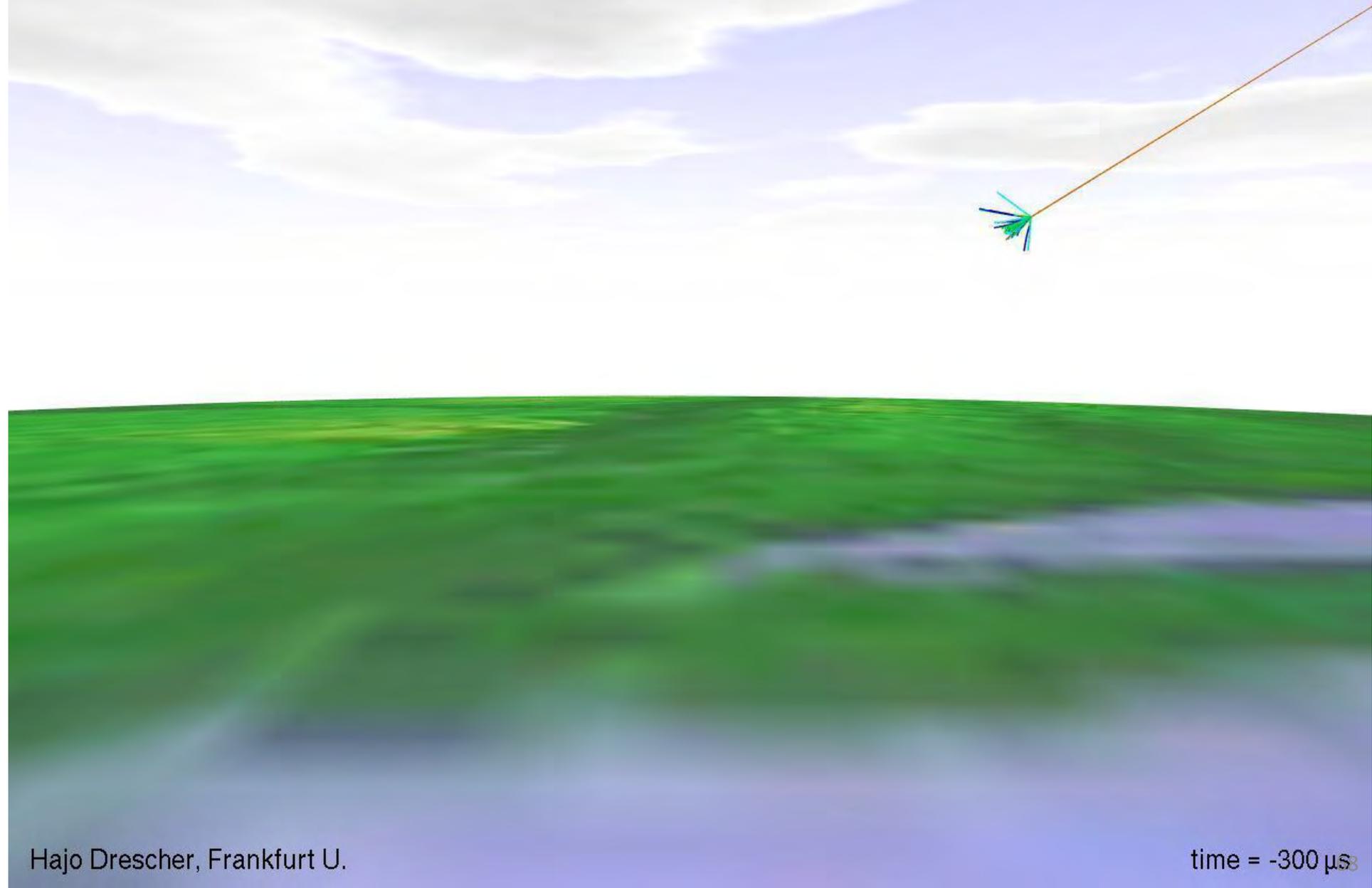
The events: Cosmic rays “rain”



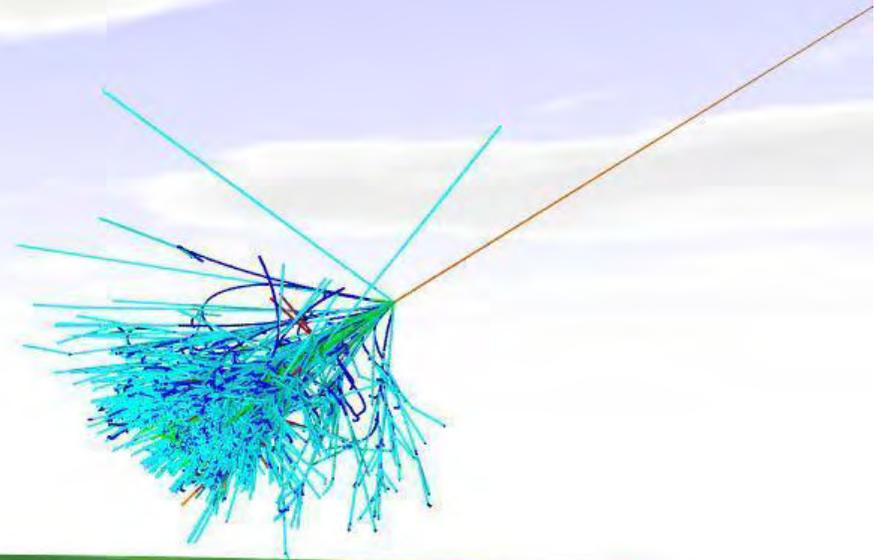
The events: Cosmic rays “rain”



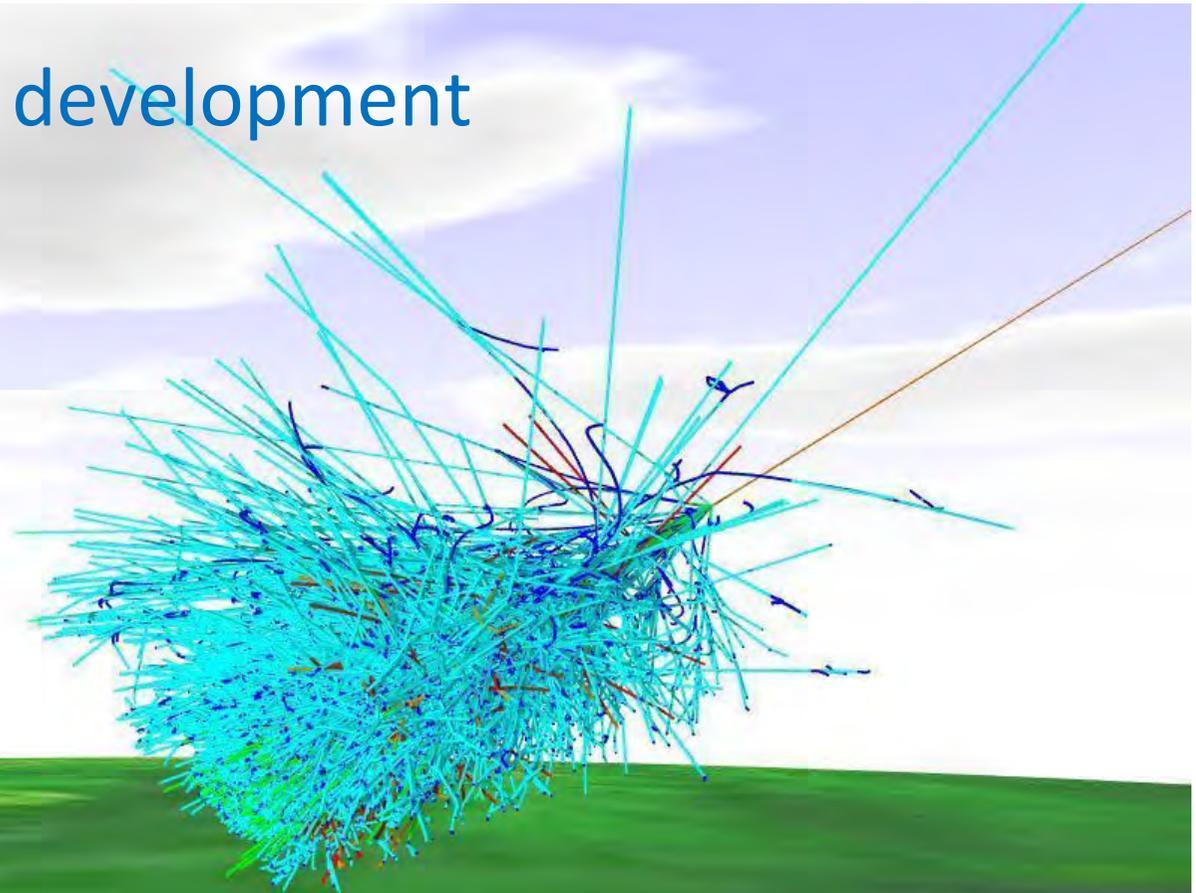
The events: first interaction



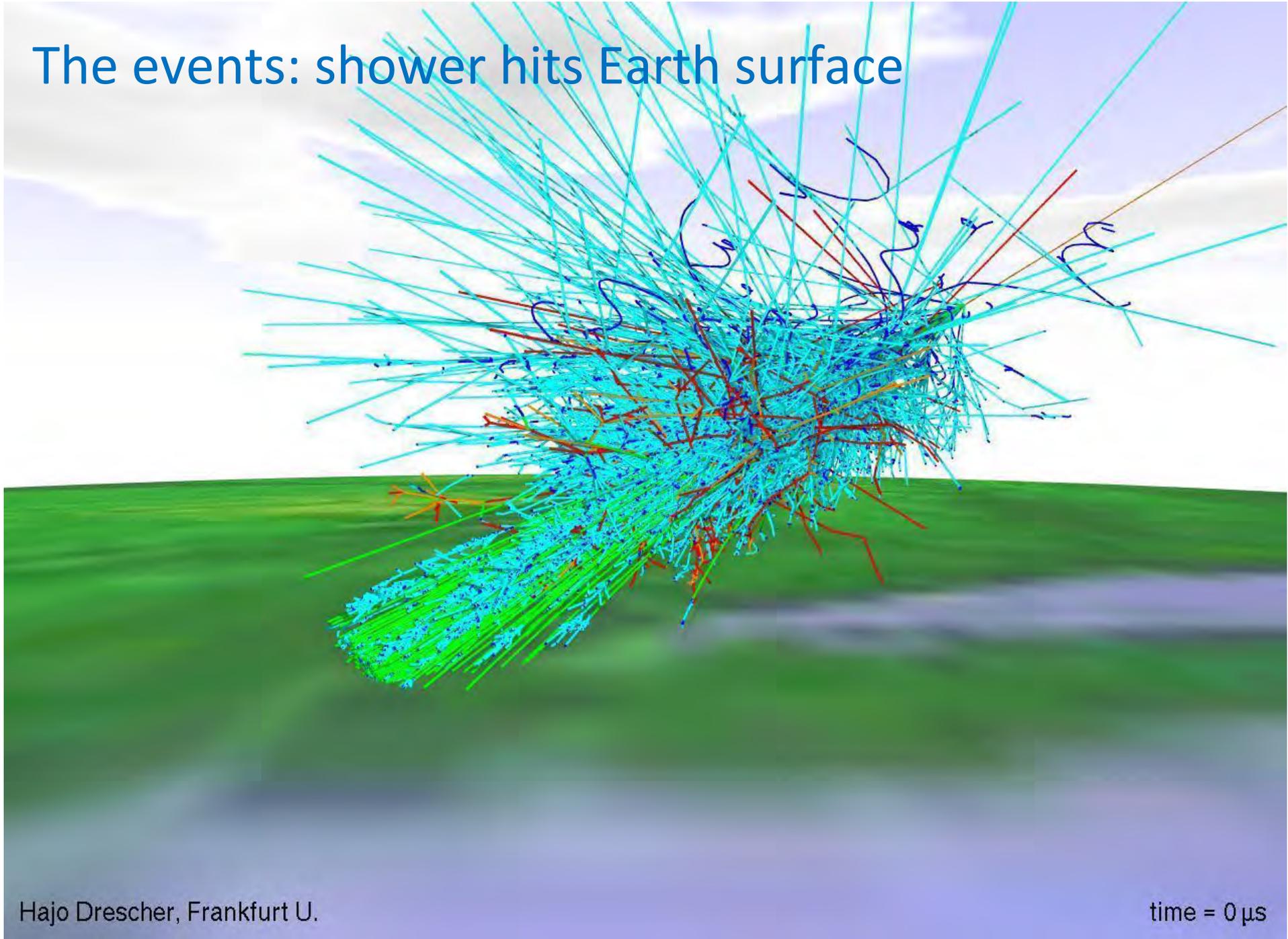
The events: shower development



The events: shower development



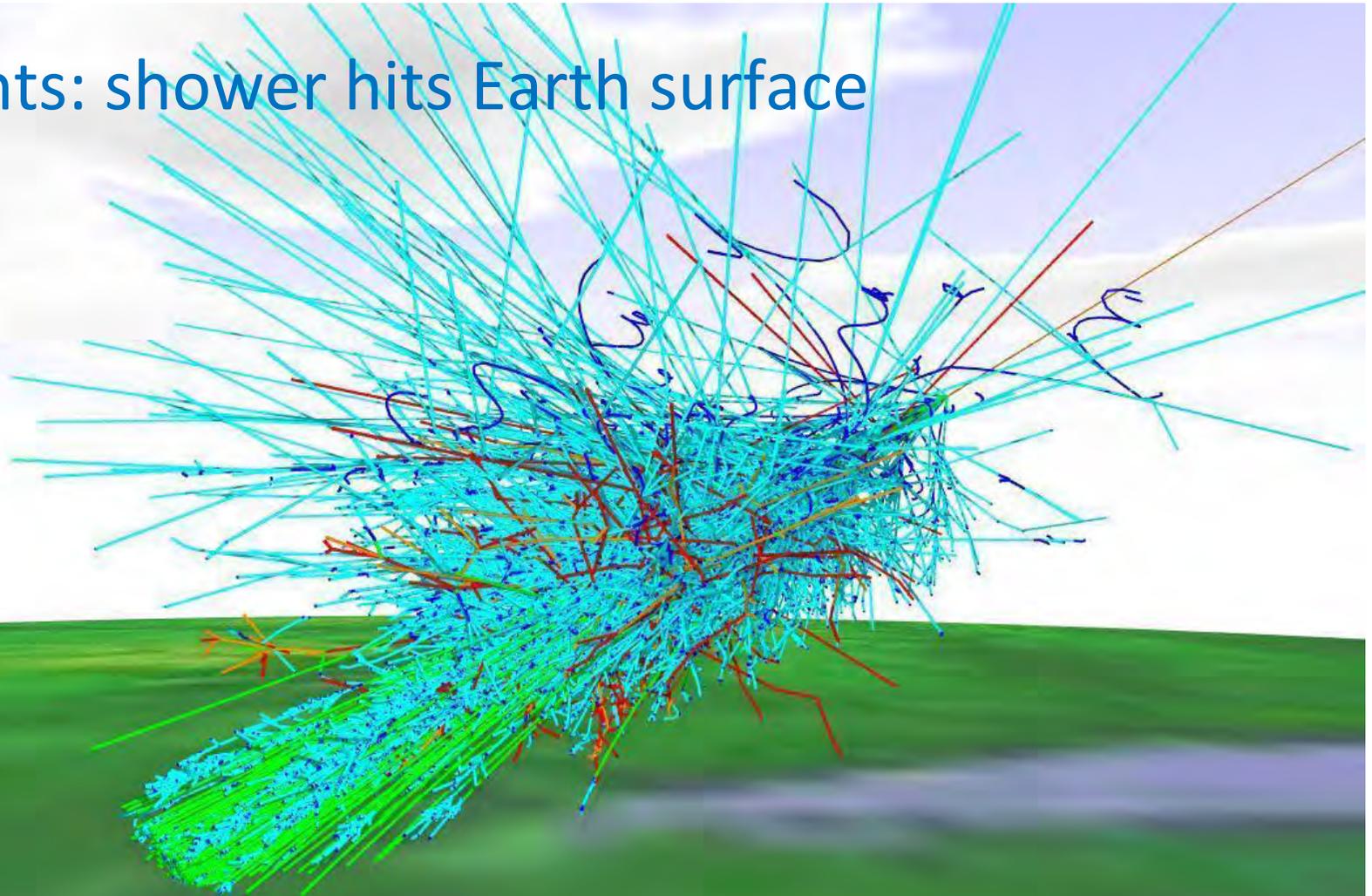
The events: shower hits Earth surface



Hajo Drescher, Frankfurt U.

time = 0 μ s

The events: shower hits Earth surface



P(Fe) Air \rightarrow Baryons (leading, net-baryon $\neq 0$)
 $\rightarrow \pi^0$ ($\pi^0 \rightarrow \gamma\gamma \rightarrow e^+e^- e^+e^- \rightarrow \dots$)
 $\rightarrow \pi^\pm$ ($\pi^\pm \rightarrow \mu^\pm$ if $L_{\text{decay}} < L_{\text{int}}$)
 $\rightarrow K^\pm, D, \dots$

Particle interactions

P(Fe) Air \rightarrow Baryons (leading, net-baryon $\neq 0$)
 $\rightarrow \pi^0$ ($\pi^0 \rightarrow \gamma\gamma \rightarrow e^+e^- e^+e^- \rightarrow \dots$)
 $\rightarrow \pi^\pm$ ($\pi^\pm \rightarrow \mu^\pm$ if $L_{\text{decay}} < L_{\text{int}}$)
 $\rightarrow K^\pm, D, \dots$

e.m. and weak interactions

- well known !

hadronic interactions

- large uncertainties !

- forward region, small p_t , very high \sqrt{s}

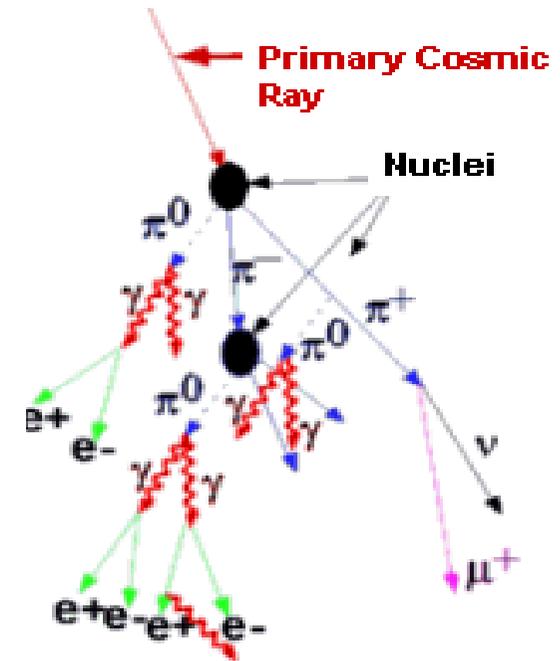
- main parameters: $\sigma_{\text{in}}, k_{\text{in}}, \langle n \rangle$, (fraction π^0 , Nb of Baryons, ...)

Nuclear fragmentation

- Nuclei are not just a superposition of nucleons !

Missing Energy

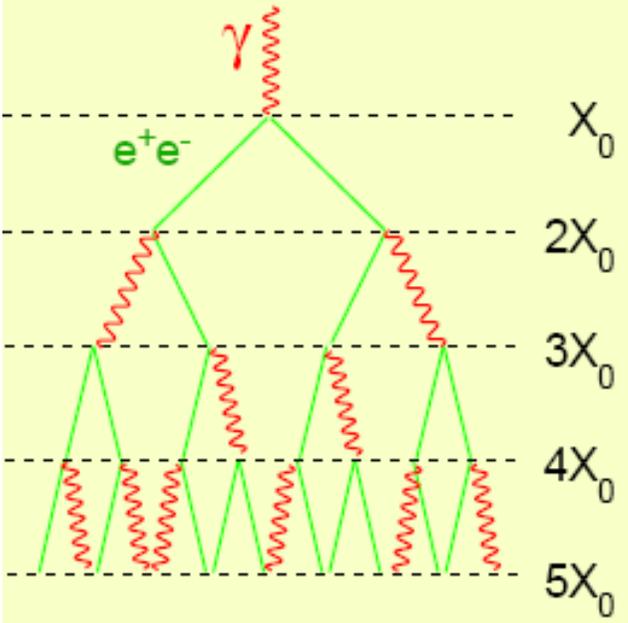
- 5% to 10% ...



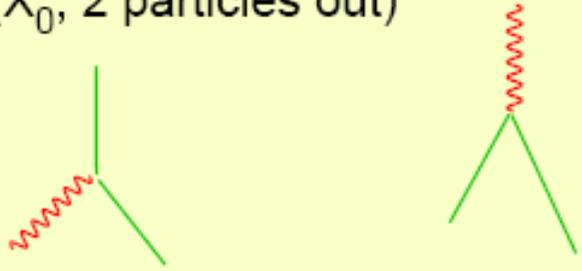
Electromagnetic interactions

J. Knapp

A simple (el.mag.) shower model:



Bremsstrahlung & Pair production
(X_0 , 2 particles out)



$N(t) = 2^t$ t is depth in X_0
 $E(t) = E_0/2^t$
 $N_{\max} = E_0/E_{\text{crit}} = 2^{t_{\max}}$
 $E_{\text{crit}} = E_0/N_{\max} = E_0/2^{t_{\max}}$
 $t_{\max} = \ln(E_0/E_{\text{crit}}) / \ln 2$

... reproduces shower behaviour rather well

but: X_0 for bremsstrahlung, $0.78 X_0$ for pair production,
both processes produce energy spectra,
 δ -electrons, ionization, scattering ...

Reality is more complicated, ... needs a MC simulation.

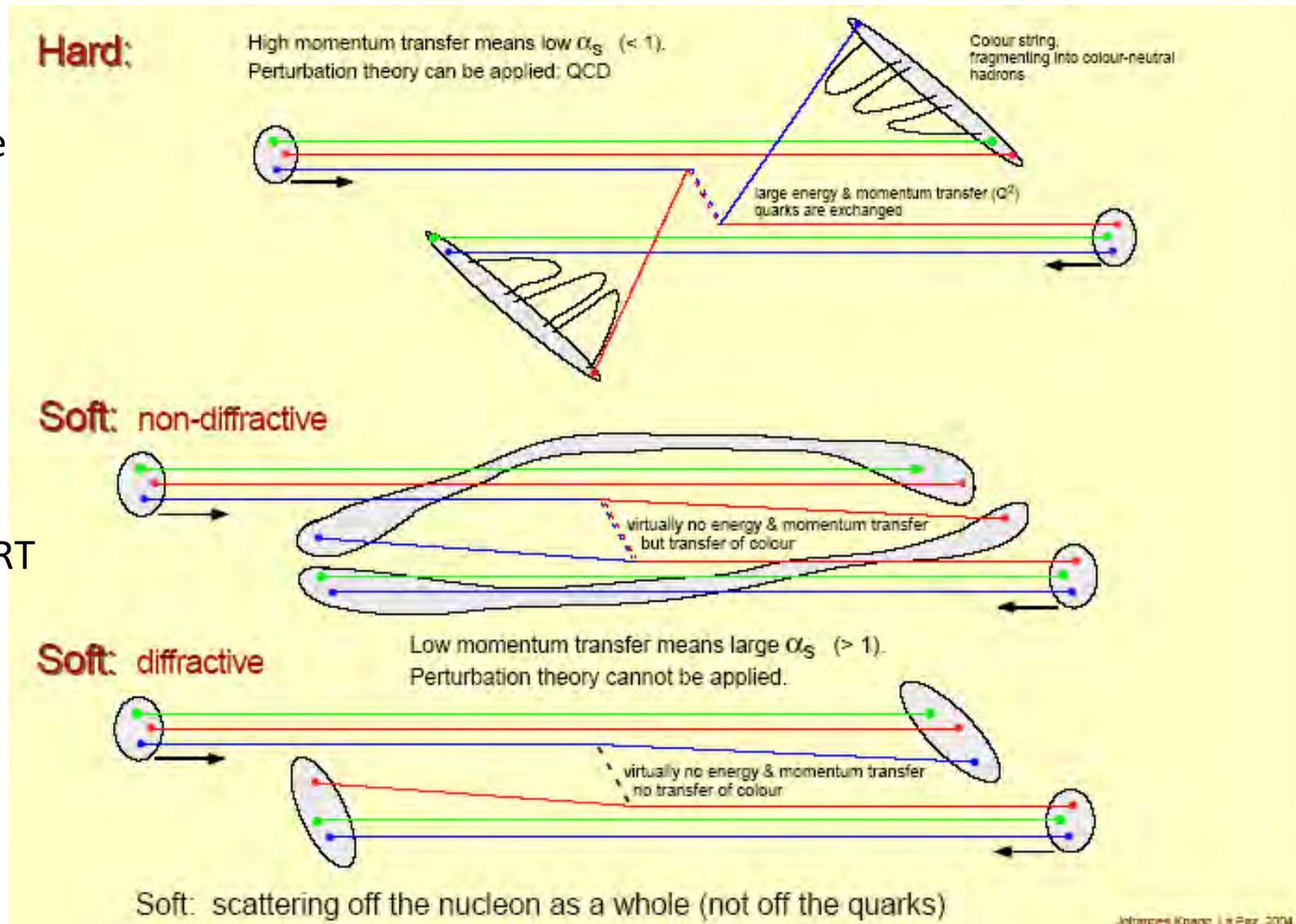
Hard and soft hadronic interactions

J. Knapp

Perturbative QCD



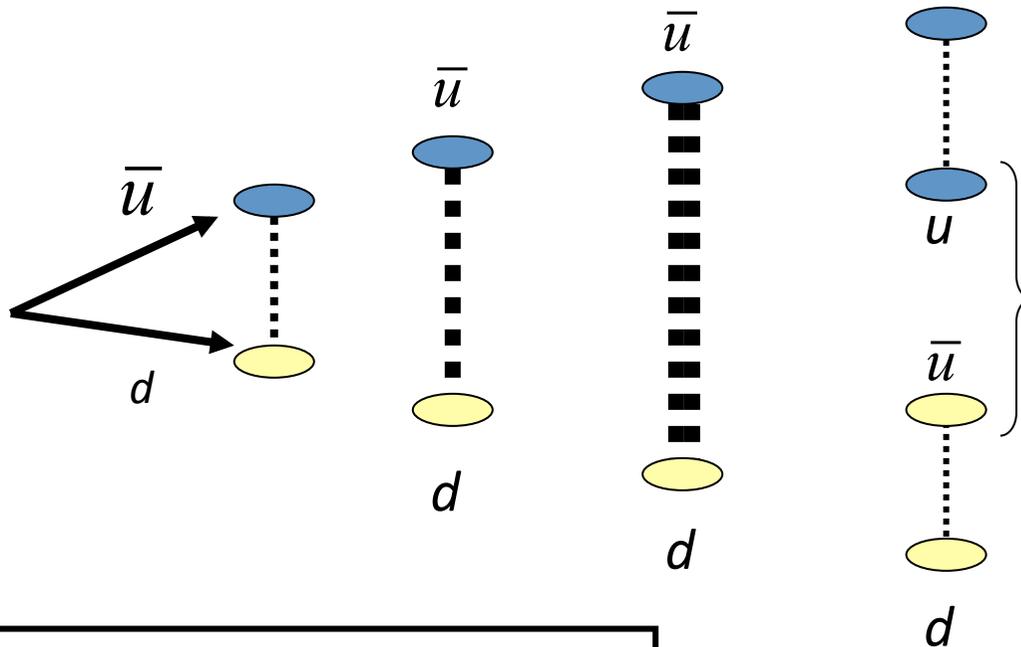
Pomeron exchange GRT



Johannes Knapp, La Paz, 2004

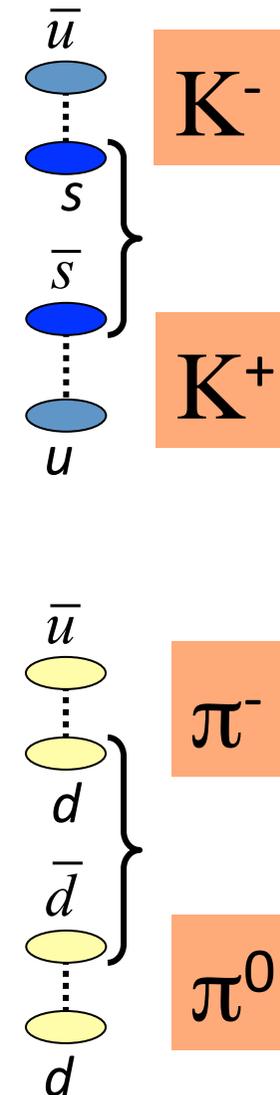
String fragmentation

Think of the gluons being exchanged as a spring... which if stretched too far, will snap!
 Stored energy in spring \rightarrow mass !



In this way, you can see that **quarks** are **always confined inside hadrons** (that's **CONFINEMENT**) !

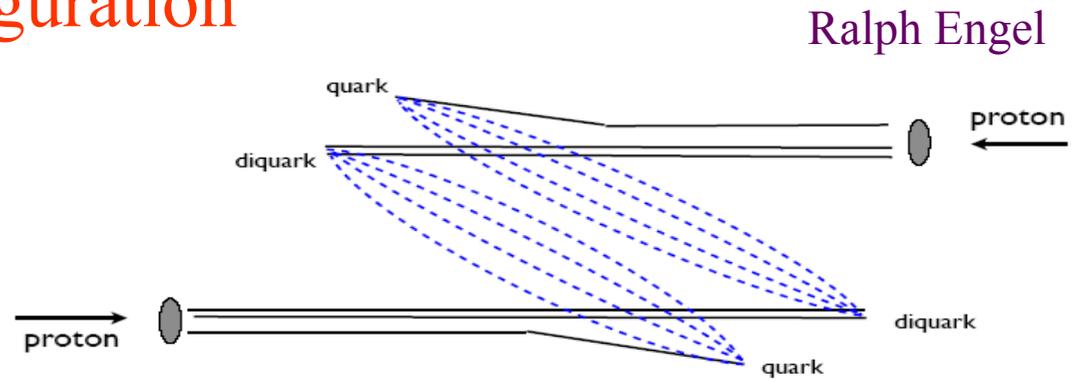
Hadrons!



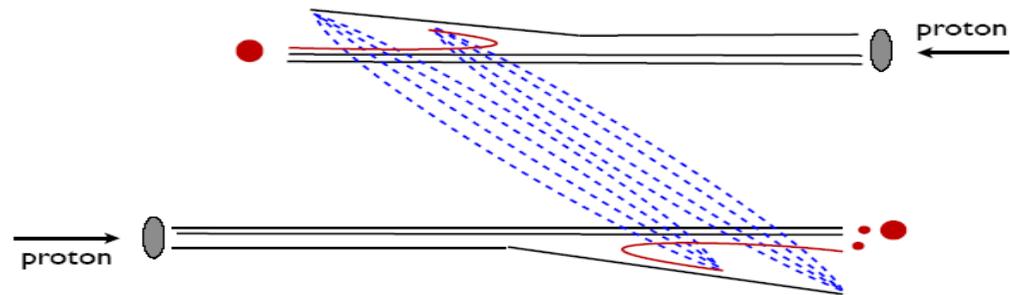
“Standard” Hadronic models (low pt)

Minimum string configuration

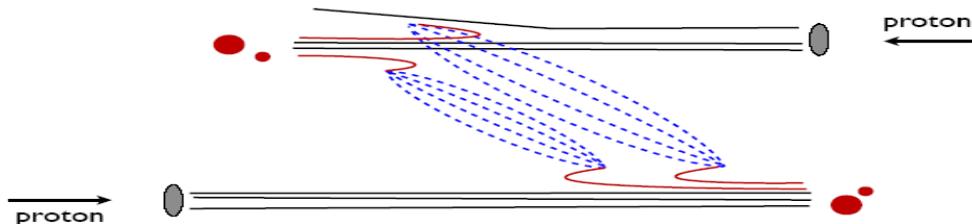
SIBYLL



QGSJET



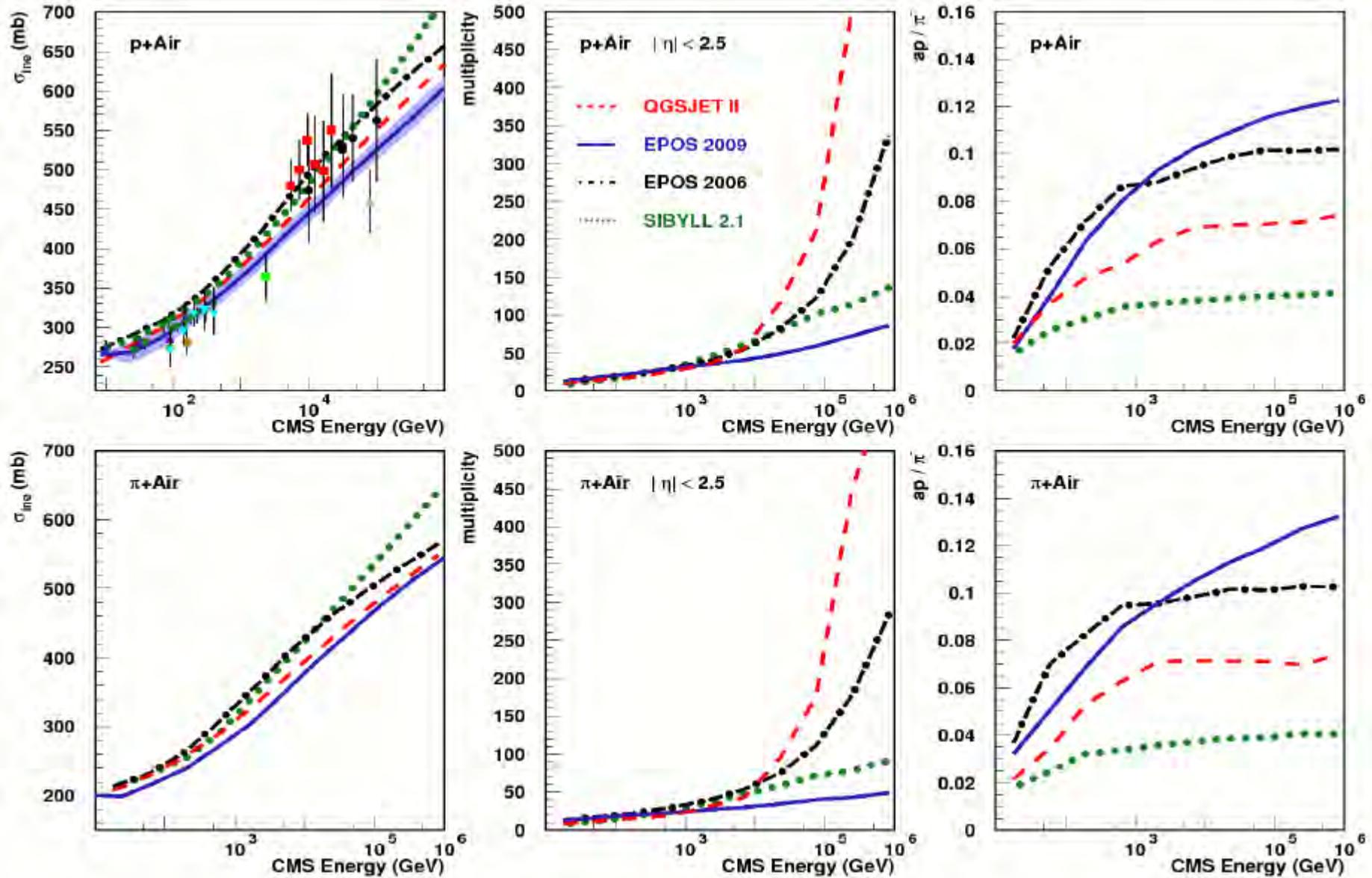
EPOS



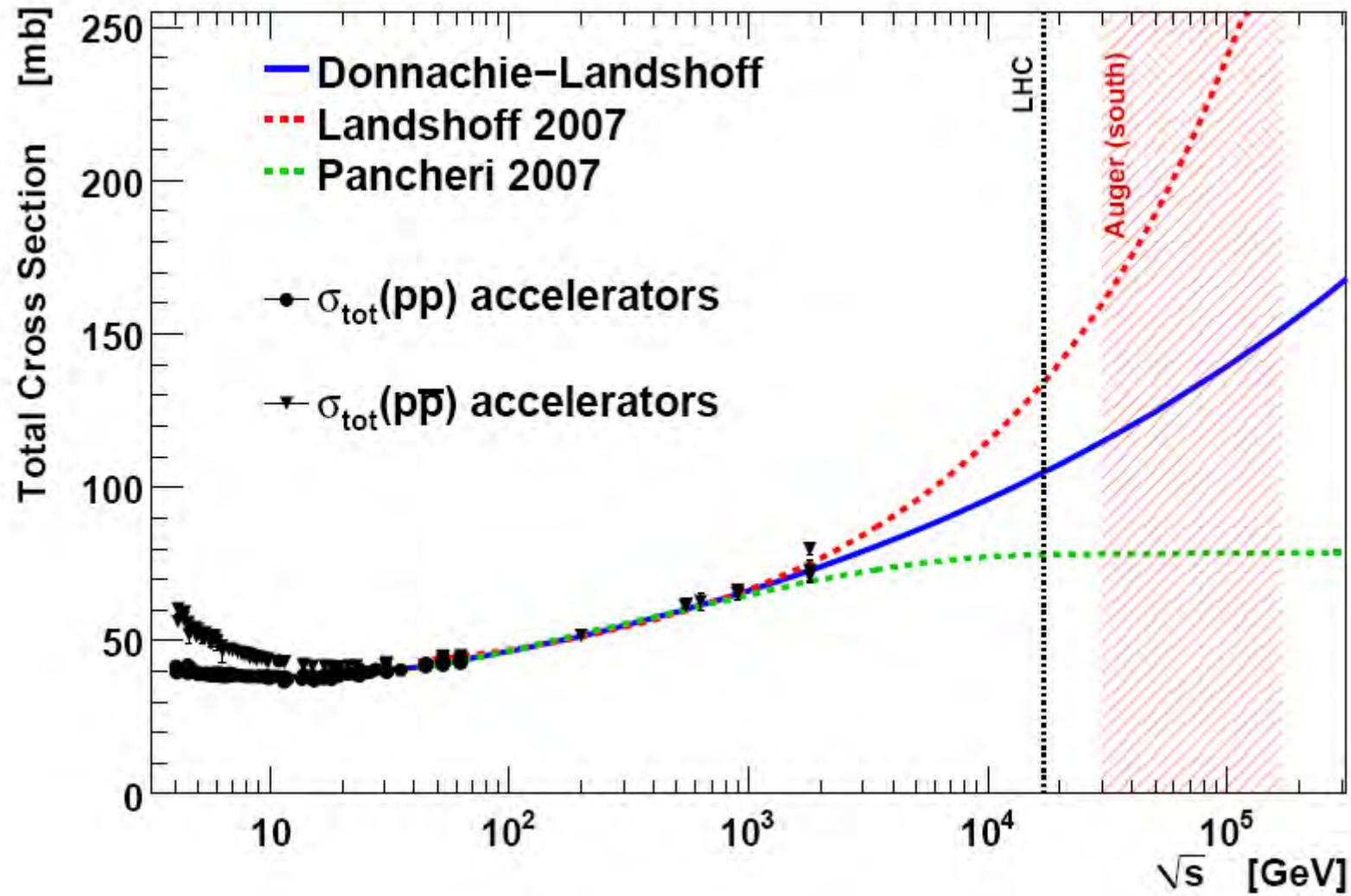
Hadronic models parameters

P.Tanguy

p air

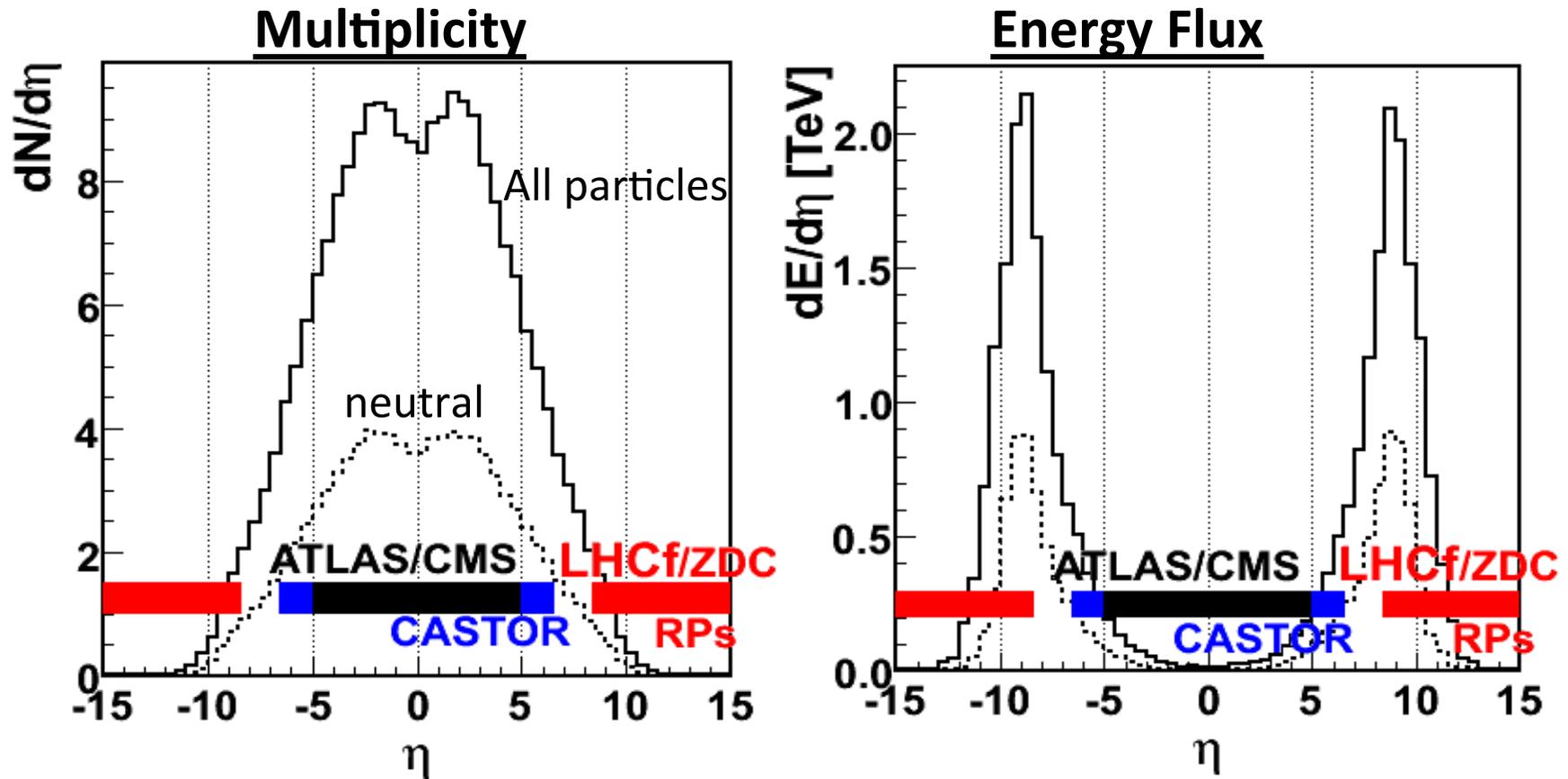


Cross sections extrapolations (before LHC)



LHC Kinematics (14 TeV)

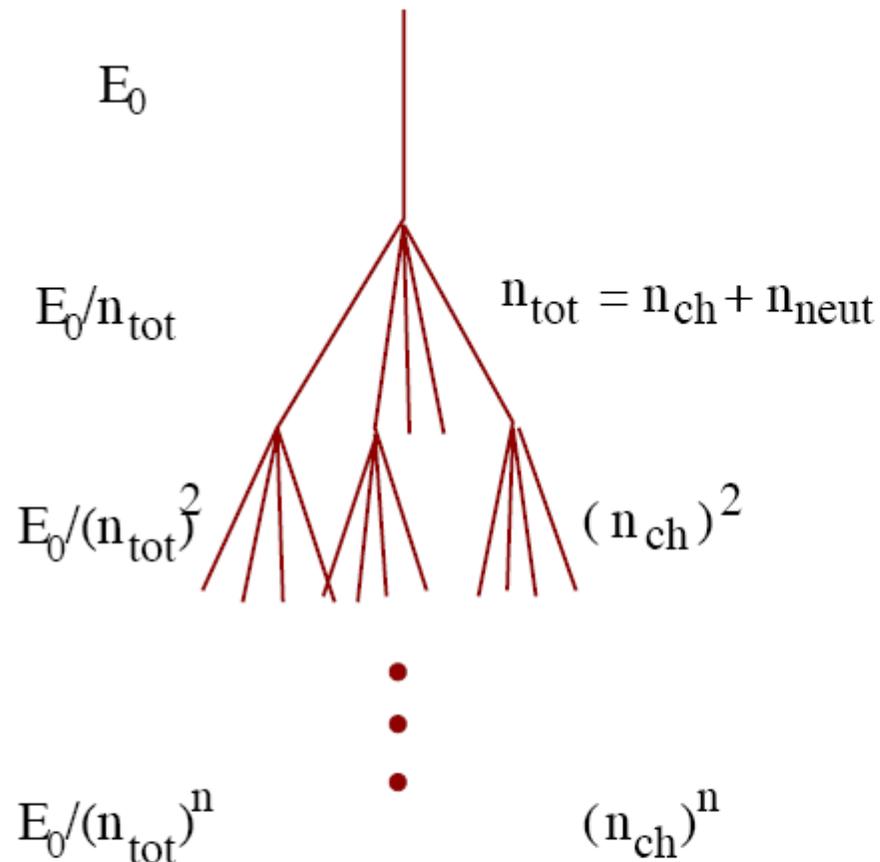
Takashi SAKO



pseudo-rapidity; $\eta = -\ln(\tan(\theta/2))$

Most of the energy flows into very forward region

Muon production



Primary particle proton

π^0 decay immediately

π^\pm initiate new cascades

Assumptions:

- cascade stops at $E_{\text{part}} = E_{\text{dec}}$
- each hadron produces one muon

$$N_\mu = \left(\frac{E_0}{E_{\text{dec}}} \right)^\alpha$$

$$\alpha = \frac{\ln n_{\text{ch}}}{\ln n_{\text{tot}}} \approx 0.82 \dots 0.95$$

(Matthews, *Astropart.Phys.* 22, 2005)

Muon spectrum at Earth Surface

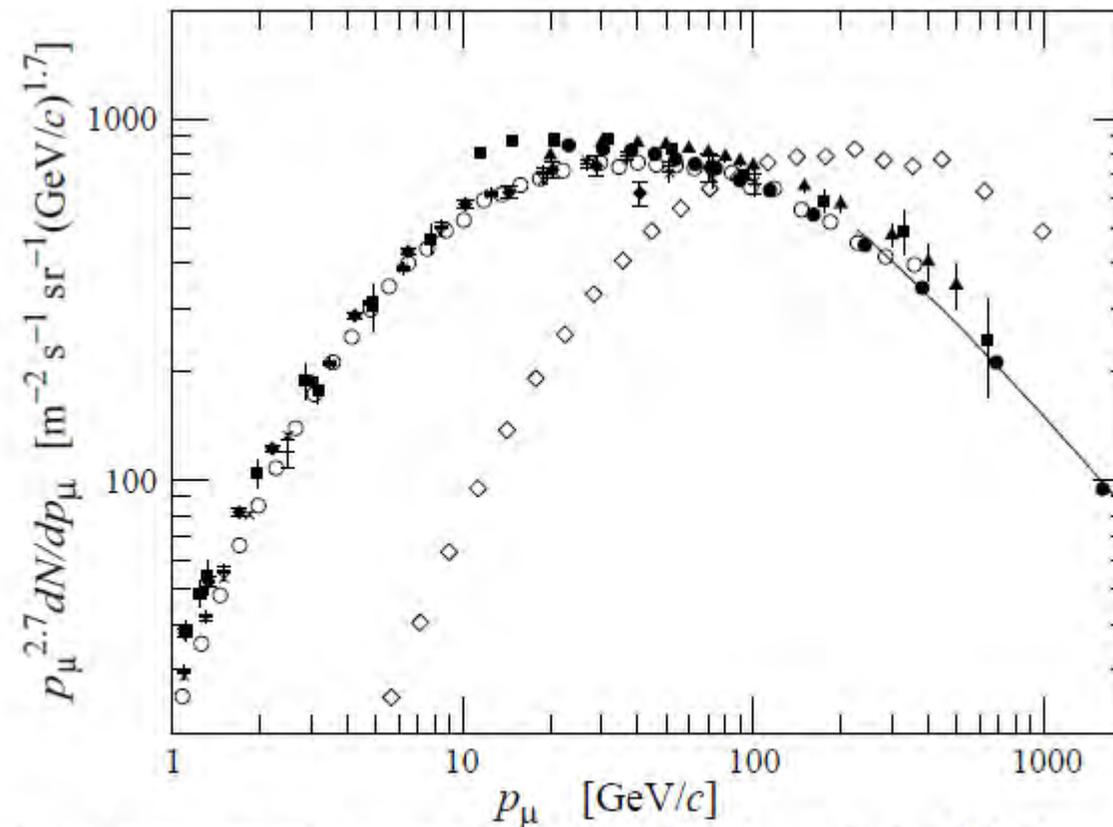


Figure 26.4: Spectrum of muons at $\theta = 0^\circ$ (\blacklozenge [41], \blacksquare [46], \blacktriangledown [47], \blacktriangle [48], \times , $+$ [43], \circ [44], and \bullet [45] and $\theta = 75^\circ$ \diamond [49]). The line plots the result from Eq. (26.4) for vertical showers. J. Beringer et al (PDG) PR D86 010001 (2012)

Fluxes in the atmosphere

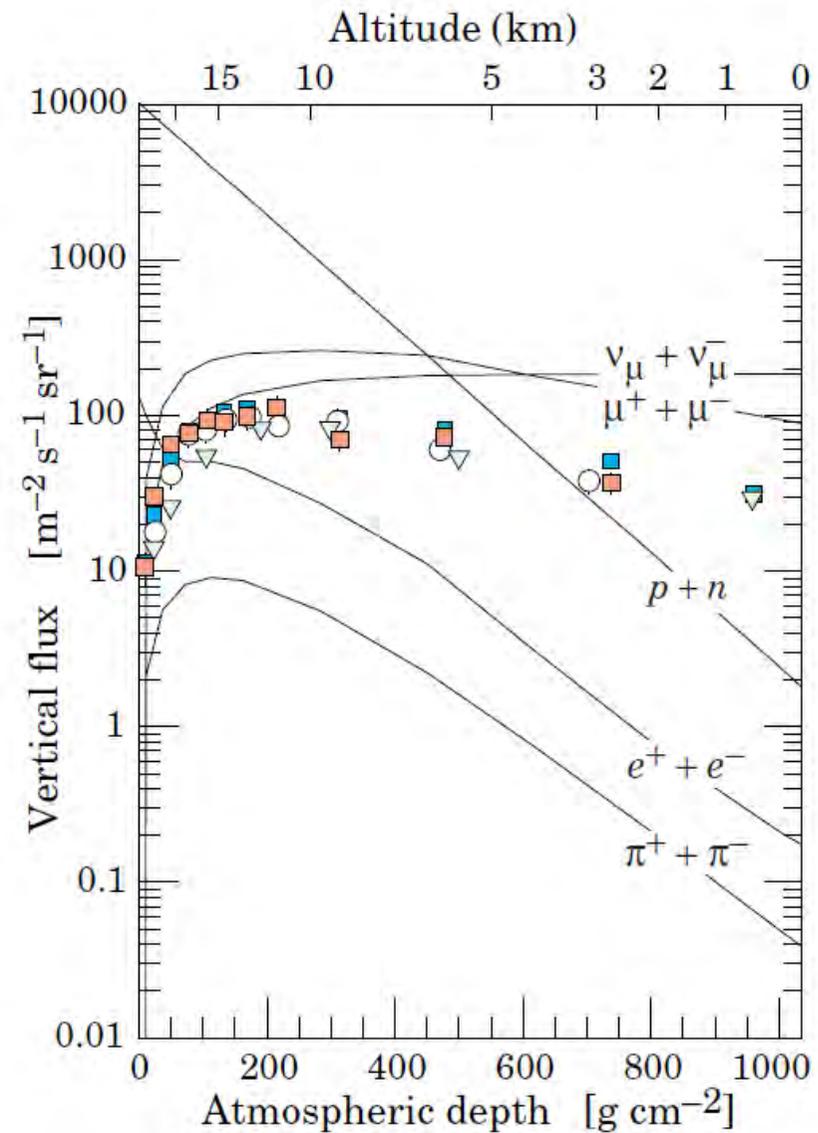


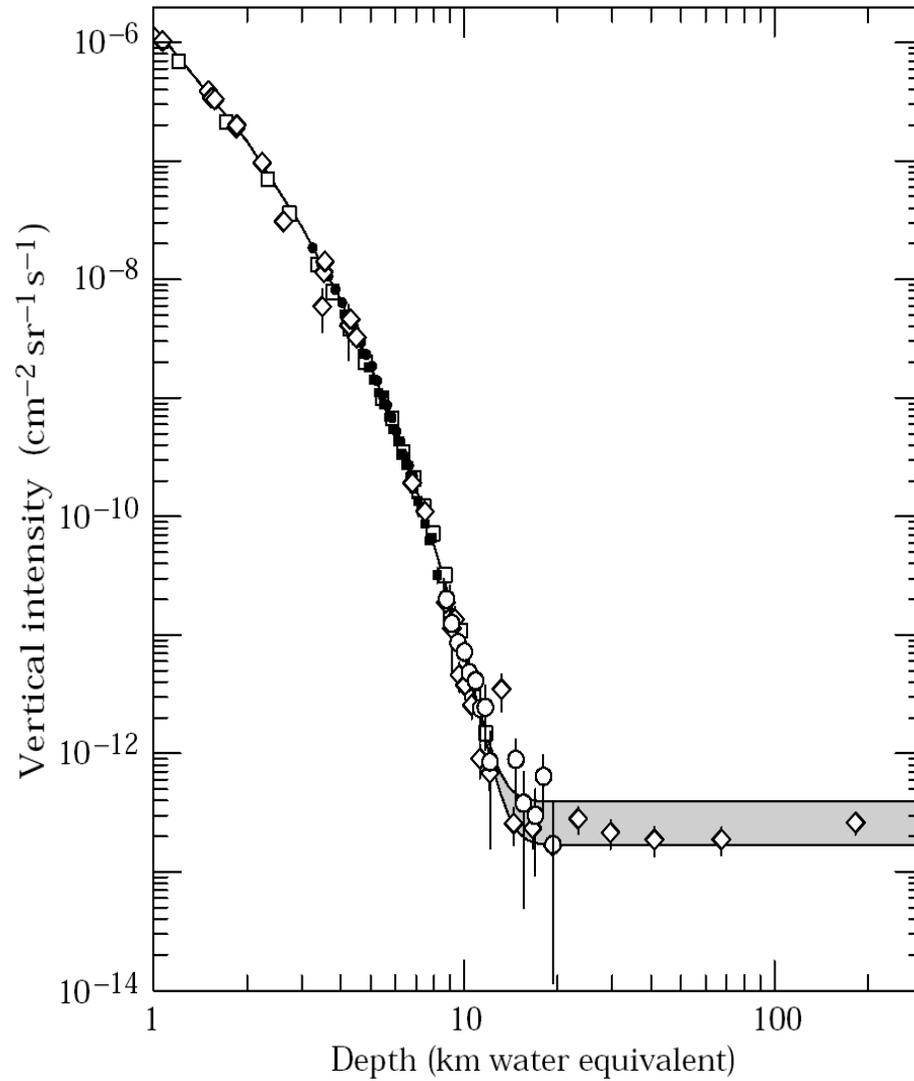
Figure 26.3: Vertical fluxes of cosmic rays in the atmosphere with $E > 1$ GeV estimated from the nucleon flux of Eq. (26.2). The points show measurements of negative muons with $E_\mu > 1$ GeV [32–36]. [J. Beringer et al \(PDG\) PR D86 010001 \(2012\)](#)

Under Earth

At the Earth surface :

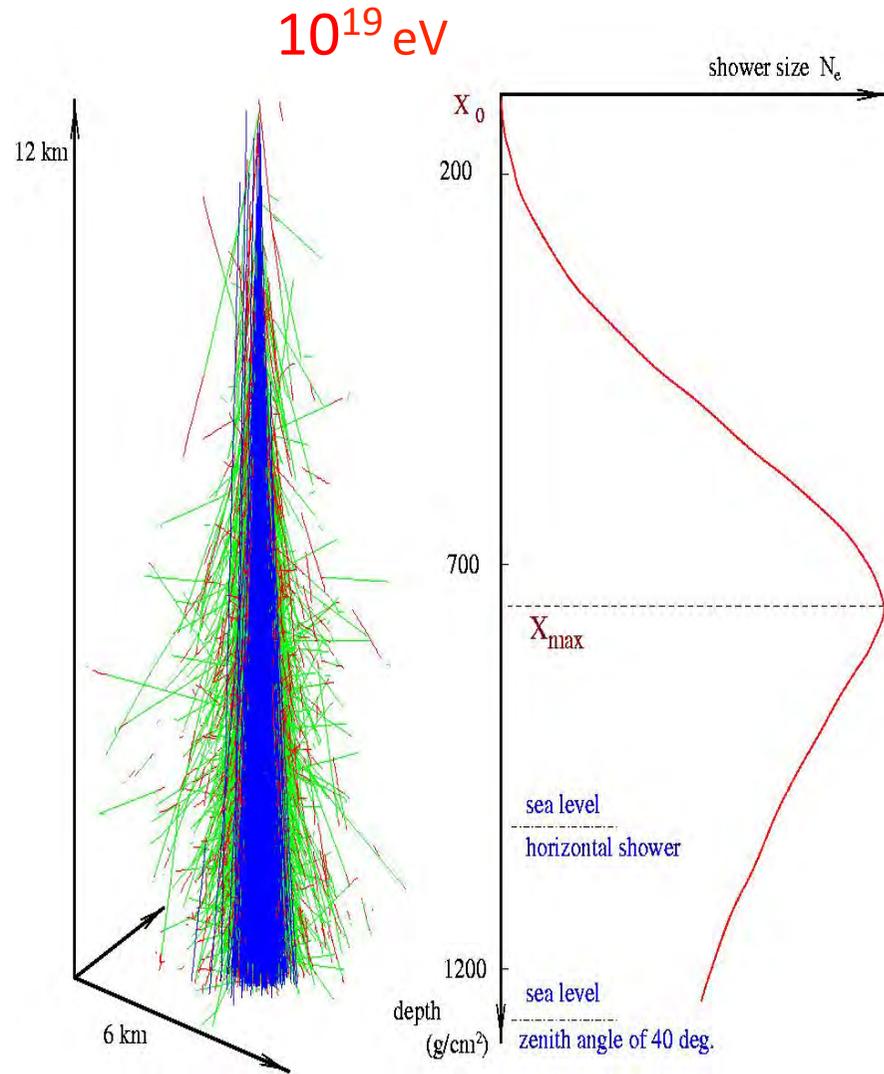
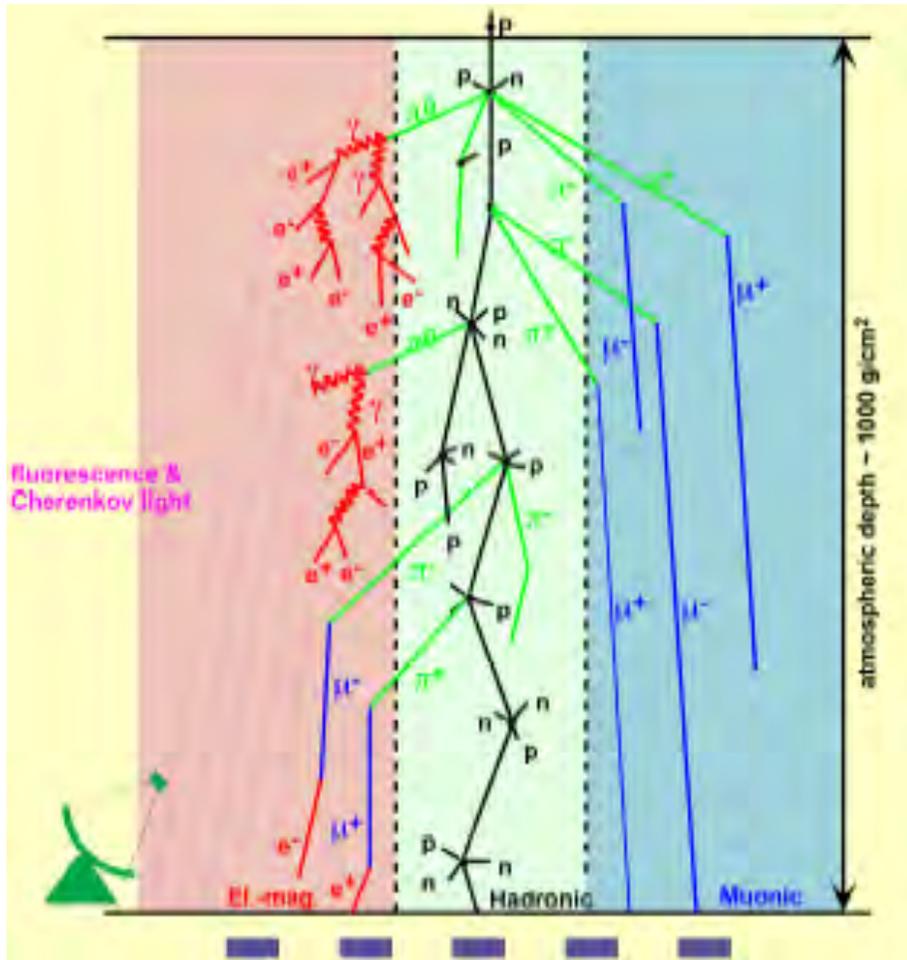
$\sim 70 \text{ m}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$

$\sim 1 \text{ cm}^{-2} \text{ min}^{-1} (\Omega \sim \pi)$



Place	Depth(KmWater)	Threshold(TeV)
Mt.Blanc	~ 5	~ 3
GranSasso	~ 3.5	~ 2
Kamiokande	~ 2.7	~ 1

Extensive Air Showers (EAS)



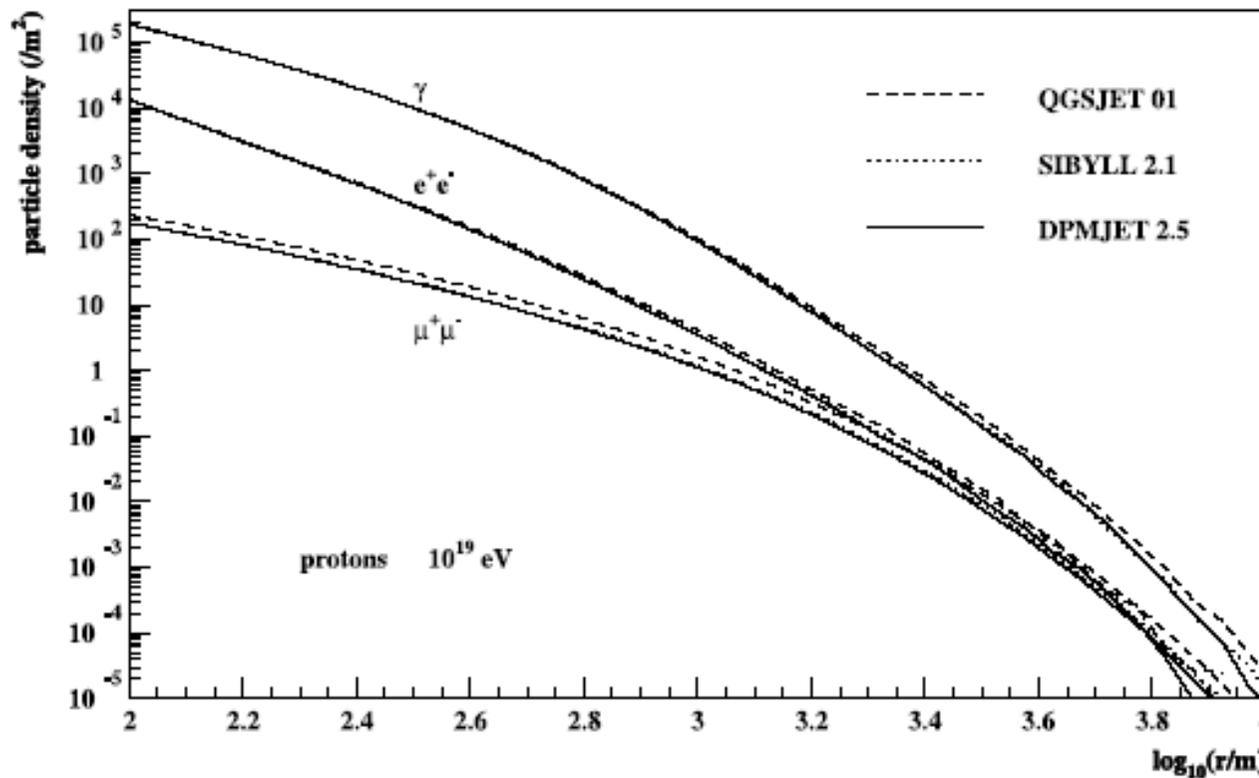
EAS transverse profiles

NKG (Nishimura, Kamata, Greisen)

$$\rho(r) = c(s)N_e / r_0^2 (r / r_0)^{s-2} (1 + r / r_0)^{s-4.5}$$

r_0 : Molière radius
 s : shower age

J. Knapp et al. / Astroparticle Physics 19 (2003) 77–99



P_t distributions
 Multiple Coulomb
 scattering

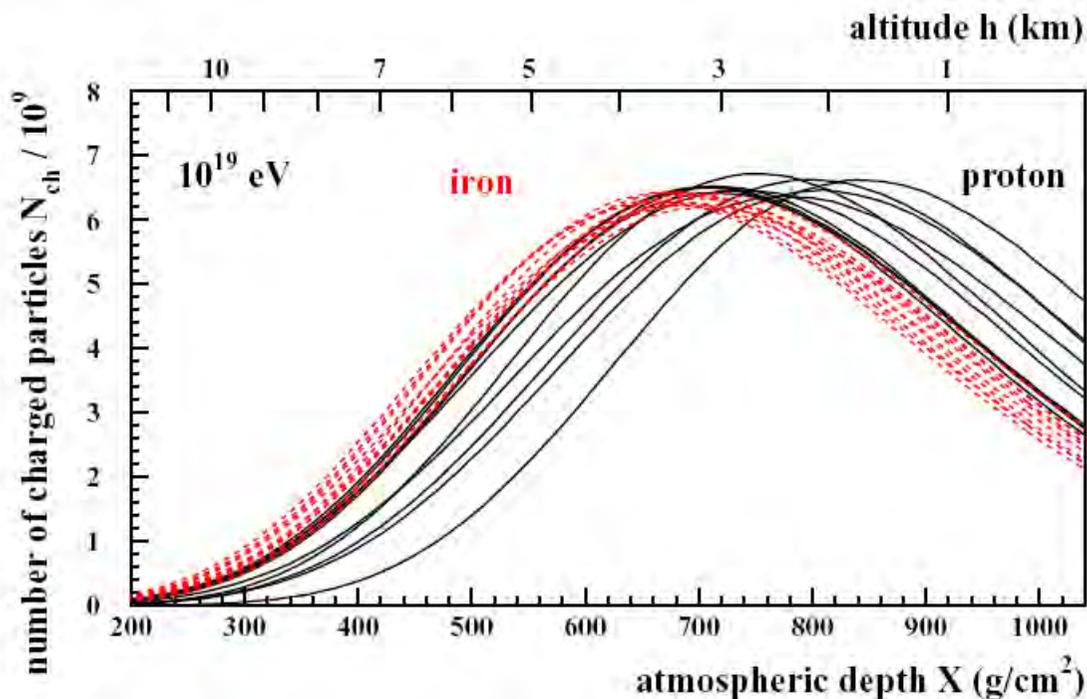
EAS longitudinal profiles

Gaisser

$$N_e = N_e^{\max} \left(\frac{X - X_1}{X_{\max} - \lambda} \right)^{\frac{X_{\max} - \lambda}{\lambda}} e^{-\left(\frac{X - X_1}{\lambda} \right)}$$

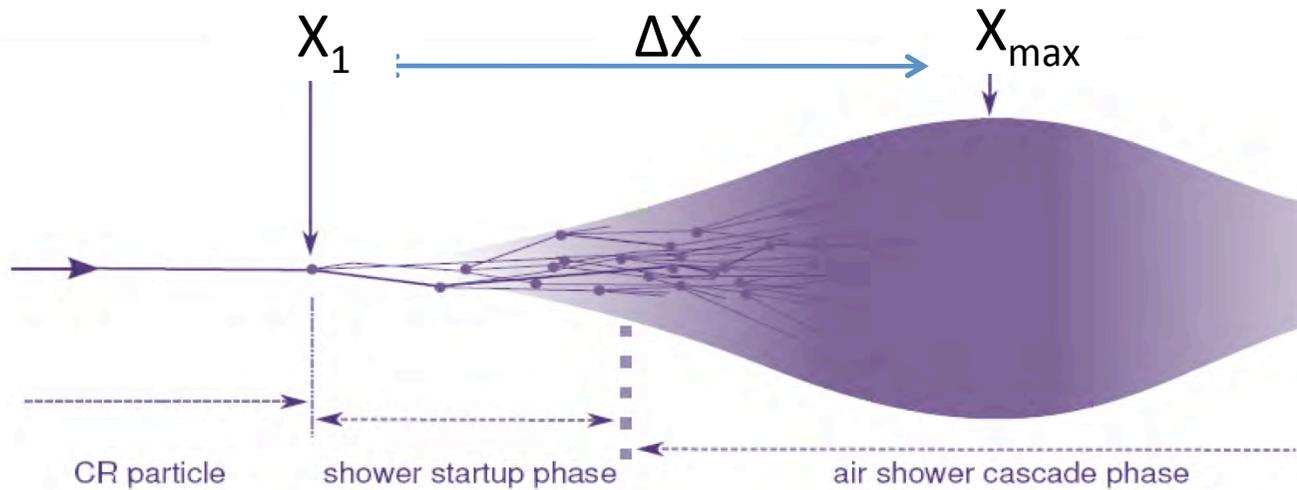
$$N_e^{\max} \propto E$$

$$X_{\max} \propto \ln E$$

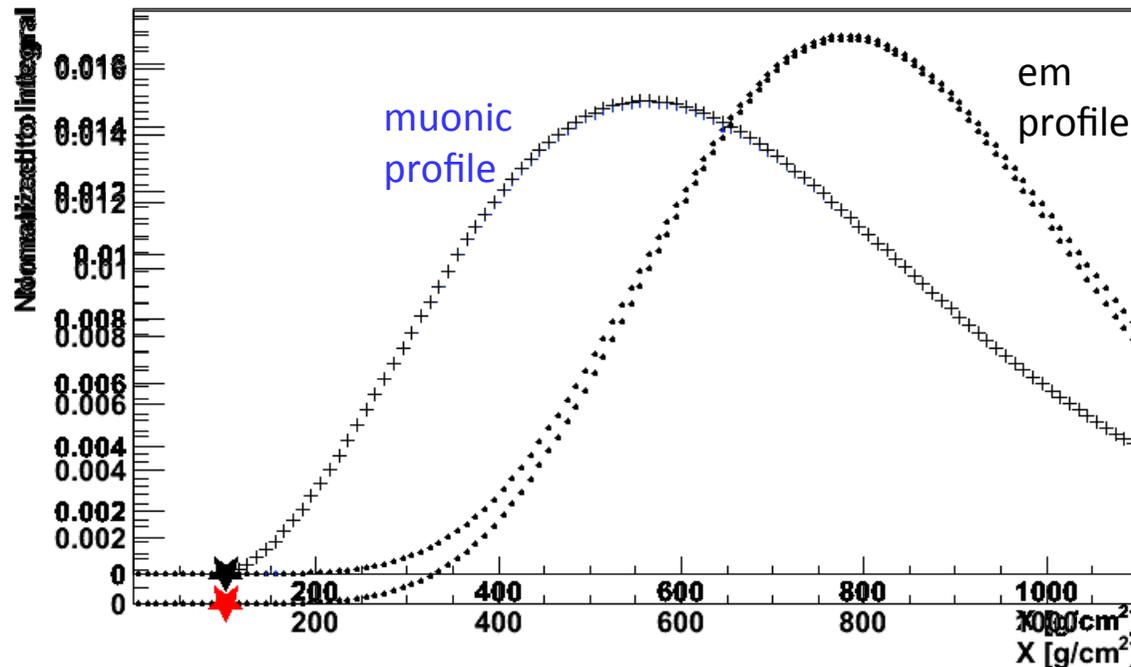


Iron $\sim 56 \text{ nucl}(E/56)$
 Smaller fluctuations
 Smaller X_{\max}

Shower development



$$X_{\max} = X_1 + \Delta X$$



$$E \propto N_e$$

$$\propto \int \frac{dN_e}{dX} dX$$

$$N_\mu \propto \int \frac{dN_\mu}{dX} dX$$