The Virgo detector

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Reminder: effect of a GW on free masses

A gravitational wave (GW) modifies the distance between free-fall masses



$$\delta x(t) = -\delta y(t) = \frac{1}{2} h(t) L_0$$

h(t): amplitude of the GW

Typical amplitude of a GW crossing the Earth: $h \sim 10^{-23}$ (h has no dimension/unit)

A general overview of the Virgo detector



The interference pattern depends on ΔL : $\Delta L(t) = l_{x(t)} - l_y(t)$

Length of the arms: $L_0 = 3$ km

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Virgo: a more complicated interferometer

Suspended mirrors

 \rightarrow Mirrors can be considered as free for frequencies larger than ~10 Hz



Orders of magnitude



Typical amplitude of differential arm length variations when a GW crosses the Earth:

$$\delta \Delta L = \delta l_x(t) - \delta l_y(t)$$
$$= h(t) L_0$$

h ~
$$10^{-23}$$
 $L_0 = 3 \text{ km}$
 $\rightarrow \delta \Delta L \sim 3 \times 10^{-20} \text{ m}$
 $\sim \frac{\text{size of a proton}}{100000}$

How and for what did you use interferometers?



Wavelength of monochromatic source Sodium doublet wavelength separation





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Part 2: Virgo optical configuration

Reminder about electromagnetic waves and planes waves

How do we "observe" ΔL with a Michelson interferometer?
Measurement of a power variations
From power variations to ΔL (or to gravitational wave amplitude h)

Improving the interferometer

How do we increase the power on the beam-splitter mirror? How do we amplify the phase offset between the arms?

Electromagnetic waves





Propagation of a perturbation of electric and magnetic fields

- Direction of propagation: along k
- E and B are in phase, and with perpendicular directions
- E and B are perpendicular to the direction of propagation of the wave (transverse wave)
- Amplitude: amplitude of the E (or B) field,
- Two polarisations: defined by the direction of E (or B)

 $\vec{k} \times \vec{E}$

Description of plane waves



$$\begin{split} U(z,t) &= A_0 e^{j(kz - \omega t + \epsilon)} \\ &= \underline{\mathcal{A}}_0 e^{j(kz + \epsilon)} \quad \text{with} \quad \underline{\mathcal{A}}_0 = A_0 e^{-j\omega t} \\ \text{--> simpler algebraic calculations, for example} \quad \mathbf{P} \propto |U|^2 = UU^* \end{split}$$

--> real plane wave is the real part:

 $\Re(U(z,t)) = A(z,t)$

Plane waves do not exist but they are a good approximation of many waves in localised region of space

 \mathbf{Z}

- Input wave $U_i(x,t) = \underline{\mathcal{A}}_i e^{jkx}$ = $\overline{\mathcal{A}}_i$ on BS
- BS located at (0,0)
- Sensor located at (0,-y)
- Amplitude reflection and transmission coefficients: r and t
- → We are interested in the beam transmitted by the interferometer: it is the sum of the two beams (fields) that have propagated along each arm

Around the mirrors:

- Radius of curvature of the beam ~ 1400 m
- Size of the beam ~ few cm





Input wave $U_i(x,t) = \underline{\mathcal{A}}_i e^{jkx}$

 $=\overline{\underline{\mathcal{A}}_i}$ on BS

Beam propagating along x-arm:

 $U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{jkl_x} \dots$



Input wave $U_i(x,t) = \underline{\mathcal{A}}_i e^{jkx}$

 $=\overline{\underline{\mathcal{A}}_i}$ on BS

Beam propagating along x-arm:

$$U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{jkl_x} \quad (-r_x) e^{jkl_x} \dots$$



Input wave $U_i(x,t) = \underline{\mathcal{A}}_i e^{jkx}$

 $=\overline{\underline{\mathcal{A}}_i}$ on BS

Beam propagating along x-arm:

 $U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{jkl_x} \quad (-r_x)e^{jkl_x} \quad r_{BS} e^{jky_s}$



Input wave $U_i(x,t) = \underline{\mathcal{A}}_i e^{jkx}$ = $\overline{\mathcal{A}}_i$ on BS

Beam propagating along x-arm:

$$U_{tx} = \underline{\mathcal{A}}_{i} t_{BS} e^{jkl_{x}} (-r_{x}) e^{jkl_{x}} r_{BS} e^{jky_{s}}$$

$$= \underline{\mathcal{A}}_{i} t_{BS} r_{BS} (-r_{x}) e^{2jkl_{x}} e^{jky_{s}}$$

$$= \frac{\underline{\mathcal{A}}_{i}}{2} \times (-r_{x} e^{2jkl_{x}}) e^{jky_{s}} \text{ with } t_{BS} = r_{x}$$

Complex reflection of the x-arm





Power transmitted by a simple Michelson

Transmitted field:
$$U_t = \frac{A_i}{2} e^{jky_s} \left(r_y e^{2jkl_y} - r_x e^{2jkl_x} \right)$$

Calculation of the transmitted power:

$$P_t \propto |U_t|^2 = \frac{P_{max}}{2} \left(1 - C \cos(\phi) \right) \quad \text{where } \phi = 2k(l_y - l_x) \\ C = 2 \frac{r_x r_y}{r_x^2 + r_y^2} \\ P_{max} = \frac{P_i}{2} (r_x^2 + r_y^2)$$



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What power does Virgo measure?

- In general, the beam is not a plane wave but a spherical wave
 - \rightarrow interference pattern
 - (and the complementary pattern in reflection)

- Virgo interference pattern much larger than the beam size:
- ~1 m between two consecutive fringes
 - \rightarrow we do not study the fringes in nice images !







Freely swinging mirrors

Setting a working point



From the power to the gravitational wave

$$P_t = \frac{P_i}{2} \left(1 - C \cos(\phi) \right) \quad \text{where } \phi = 2 \frac{2\pi}{\lambda} (l_y - l_x)$$

P_t/P_max

0.6

-2

-1

Around the working point:

$$\left. \frac{\mathrm{d}P_t}{\mathrm{d}\phi} \right|_{\phi_0} = \left. \frac{P_i}{2} C \sin(\phi_0) \right|_{\phi_0} \text{ where } \phi_0 = \left. \frac{4\pi}{\lambda} \Delta L_0 \right|_{\phi_0}$$

Power variations as function of small differential length variations:

$$\delta P_t = \frac{P_i}{2} C \sin(\phi_0) \delta \phi$$
$$\delta P_t = P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \delta \Delta L$$

 $\delta P_t \propto \delta \Delta L = h L_0$ around the working point !

2

 ϕ_0

 Φ (rad

From the power to the gravitational wave

Around the working point:

$$\delta P_{t} = P_{i} C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda}\Delta L_{0}\right) \delta\Delta L$$

$$\delta P_{t} = (\text{Interferometer response}) \times \delta\Delta L$$

(W/m)
Measurable
physical quantity
Measurable

Improving the interferometer sensitivity

 $\delta P_t = P_i C \sin\left(\frac{4\pi}{\lambda}\Delta L_0\right) \underbrace{\left(k\delta\Delta L\right)}_{\propto \delta\phi}$

Increase the input power on BS Increase the phase difference between the arms for a given differential arm length variation



In Virgo, the beam is resonant inside the cavities



Average number of light round-trips in the cavity:

$$N = \frac{2\mathcal{F}}{\pi}$$

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How do we amplify the phase offset?



(instead of $r_{armx} = -1 \times e^{j2k(L_x + \delta L_x)}$

in the arm of a simple Michelson)

How do we increase the power on BS?

Detector working point close to a dark fringe → most of power go back towards the laser



Resonant power recycling cavity



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The improved interferometer response

Response of simple Michelson:

$$\delta P_t = P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda}\Delta L_0\right) \delta \Delta L$$

 $\delta P_t = (\underbrace{\text{Michelson response}}_{\text{(W/m)}} \times \delta \Delta L$



Response of recycled Michelson with Fabry-Perot cavities:

$$\delta P_t = \frac{G_{PR}}{G_{PR}} P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda}\Delta L_0\right) \frac{2\mathcal{F}}{\pi} \delta \Delta L$$

$$\sim 38 \qquad \qquad \sim 300$$

For the same $\delta \Delta L$, δP_t has been increased by a factor ~ 12000.

A hint of AdvancedVirgo sensitivity



Response of recycled Michelson with Fabry-Perot cavities:

$$\delta P_t = \frac{G_{PR}}{G_{PR}} P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda}\Delta L_0\right) \frac{2\mathcal{F}}{\pi} \delta \Delta L$$

Laser wavelength	$\lambda = 1064 \text{ nm}$
Input power	$P_i \sim 100 \ \mathrm{W}$
Interferometer contrast	$C \sim 1$
Cavity finesse	$\mathcal{F} \sim 450$
Power recycling gain	$G_{PR} \sim 38$
Working point	$\Delta L_0 \sim 10^{-11} \text{ m}$

Shot noise due to output power of ~ 50 mW $\rightarrow \delta P_{t,min} \sim 0.1 \,\mathrm{nW}$ $\longrightarrow \delta \Delta L_{min} \sim 5 \times 10^{-20} \,\mathrm{m}$ $\rightarrow h_{min} = \frac{\delta \Delta L_{min}}{L} \sim 10^{-23} \,\mathrm{m}$

In reality, the detector response depends on frequency...

Optical layout of Virgo



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Part 3: How do we measure the GW strain, h(t), from this detector?

Notes about data processing

Controlling the interferometer working point A glimpse on the calibration and h(t) reconstruction

Data collection

Notes about data processing: digitisation



The Virgo detector – How do we measure the GW strain, h(t), from this detector ? Notes about data processing: spectral analysis







Frequency (Hz)34

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How do we control the working point?



We want $\Delta L_0 = n \frac{\lambda}{2} + 10^{-11} \,\mathrm{m}$ to be (almost) fixed! Control loop done for noises with f between ~10 Hz and ~100 Hz Precision of the control ~ 10⁻¹⁶ m



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From the detector data to the GW strain h(t)

- High frequency (>100 Hz): mirrors behave as free falling masses $A(t) = \frac{\delta \Delta L_{true}(t)}{L_0}$
- Lower frequency: the controls attenuate the noise... but also the GW signal!
 → the control signals contain information on *h(t)*



AdVirgo data acquisition summary



Continuous flow of ~2 TBytes/day (20 to 40 MBytes/s) Disk space on Virgo site: ~400 TB for 6 months of data

Longer storage: data sent via Ethernet to computing centers (Lyon, Bologna)

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Part 4: Virgo noises



What is a noise in Virgo?

Stochastic (random) signal that contributes to the signal h_{rec}(t) but does not contain information on the gravitational wave strain $h_{GW}(t)$

 $h_{rec}(t) = h_{noise}(t) + h_{GW}(t)$



39

2.5

2

2

2.5

How do we characterise a noise?



How do we characterise a noise ... in frequency-domain?



s(n) -Sampled signal → $S(k) = A(k)e^{j\Phi(k)}$ Fourier spectrum

→ Noise characterised by the fluctuations of its Fourier spectrum

 $ightarrow rac{D(k)}{D(k)}$ in units/ $\sqrt{
m Hz}$

Assumption: noise is random and ergodic

 \rightarrow noise characterised by its amplitude spectral density (ASD)

 $ASD = \sqrt{PSD} = \sqrt{\frac{|DFT|^2}{T}}$



What is the noise level of Virgo?



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Seismic noise and suspended mirrors



Ground vibrations up to ~1 $\mu m/\sqrt{Hz}$ at low frequency decreasing down to ~10 pm/ \sqrt{Hz} at 100 Hz

 $\gg 10^{-19}\,{\rm m}/\sqrt{{\rm Hz}}$ needed to detect GW !!



Modulus

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Seismic noise and the Virgo suspension



Passive attenuation: 7 pendulum in cascade

At 10 Hz: $\frac{x_{mirror}}{x_{ground}} \sim (10^{-2})^7 = 10^{-14}$ $x_{ground} \sim 10^{-9} \,\mathrm{m}/\sqrt{\mathrm{Hz}}$ $\rightarrow x_{mirror} \sim 10^{-23} \,\mathrm{m}/\sqrt{\mathrm{Hz}}$

This noise directly modifies the positions of the mirror surfaces, and thus $\delta\Delta L$ and $h_{rec}(t)$!

Active controls at low frequency
Accelerometers or interferometer data
Electromagnetic actuators
Control loops

Some noises: thermal noise

Microscopic thermal fluctuations

--> dissipation of energy through excitation of the macroscopic modes of the mirror



This noise directly modifies the positions of the mirror surfaces, and thus $\delta \Delta L$ and $h_{rec}(t)$!

We want high quality factors Q to concentrate all the noise in a small frequency band

What is the shot noise?



^{*}PARTICLE**ZOO**

Fluctuations of arrival times of photons (quantum noise)

Power received by the photodiode: P_t $\rightarrow N = \frac{P_t}{h\nu}$ photons/s on average.



Arrival time of single photons

Standard deviation on this number: $\sigma_N = \sqrt{N}$ $\rightarrow \sigma_{P_t} = \sigma_N \times h\nu = \sqrt{\frac{P}{h\nu}}h\nu = \sqrt{P_th\nu}$

Virgo laser: $\lambda = 1.064 \,\mu\text{m} \rightarrow \nu = \frac{c}{\lambda} \sim 2.8 \times 10^{14} \,\text{Hz}$ Working point: $P_t \sim 80 \,\text{mW} \rightarrow \sigma_{P_t} = 0.1 \,\text{nW}/\sqrt{\text{Hz}}$

 \rightarrow a variation of power is interpreted as a variation of distance $\delta \Delta L$

 $\delta P_t = (\text{Virgo response}) \times L_0 \times h$ (in W/m) $h_{equivalent} = \frac{1}{L_0} \frac{\sigma_{P_t}}{\text{(Virgo response)}}$

Some other noises

- Acoustic vibrations and refraction index fluctuation
 - Main elements installed in vacuum
- Laser: amplitude, frequency, jitter noise
 - Lots of control loops to reduce these noises



Electronics noise



- Challenge for the electronicians to measure down to 0.1 nW/sqrt(Hz)
- Non-linear noise from diffuse light
 - Need dedicated optical elements with specific mechanical modes

Interpretation of the Virgo sensitivity curve

1/ Reconstruction of h(t) $h_{rec}(t) = h_{noise}(t) + h_{GW}(t)$

2/ Amplitude spectral density of *h(t)* (noise standard deviation over 1 s)

~ 10^{-19} m/ \sqrt{Hz} (Virgo, 201<u>1)</u> ~ 10^{-20} m/ \sqrt{Hz} (Advanced Virgo, ~2021)





Image: Danna Berry/SkyWorks/NASA





Image: B. Saxton (NRAO/AUI/NSF)

Rotating neutron stars Signal averaged over days (~10⁶ s)

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History of Virgo noise curve



Part 5: towards Advanced Virgo



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Horizon of Advanced detectors



Towards the Advanced Virgo sensitivity



Advanced Virgo is being built

New optical configuration

Better and heavier mirrors



Monolithic silica mirror suspension



More in vacuum suspended benches



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New electronics boards



A worldwide network of interferometers



- ► Confirm a detection
- Determine the position of a GW source
- Decompose the GW polarisation

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Multi-messenger astronomy

Astrophysical alerts



GCN (GRBs) Swift, Fermi, INTEGRAL, ... SNEWS (supernova) IceCube, Super-K, SNO, LVD

Alerts in LIGO-Virgo control rooms

Specific analysis (on-line and later)

Online GW candidates (LIGO-Virgo)

+ check by operators and scientists on site

Few minutes

Alerts for the observatories

Rotse, TAROT, SkyMapper, QUEST, Pi of the Sky, Zadko, Liverpool Telescope, LOFAR

X-ray satellites Swift/XRT

γ-ray telescomes HESS, CTA



Increase the significativity of the events
Better understand the physics of the sources

Towards the first GW detections!



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time /s