



## A computing exercise using ROOT

.. a taste of data analysis ..

- **What is ROOT ?**

- ROOT is an object-oriented C++ analysis package
- User-compiled code can be called to produce 1-d, 2-d, and 3-d graphics and histograms...



# Outline

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- **Variables used in the analysis of  $p - p$  collisions**
- **Useful relations**
- **Concept of invariant mass: inclusive Z boson production**
- **Kinematics of  $p - p$  collisions**
- **Analysis in  $p - p$  collisions :**
  - \* **Signal:** Production of a W and a Z
  - \* **Background:** Production of a pair of top-antitop
- **Example: Macro.C**

In all the following slides we assume the speed of the light

$$c=1$$

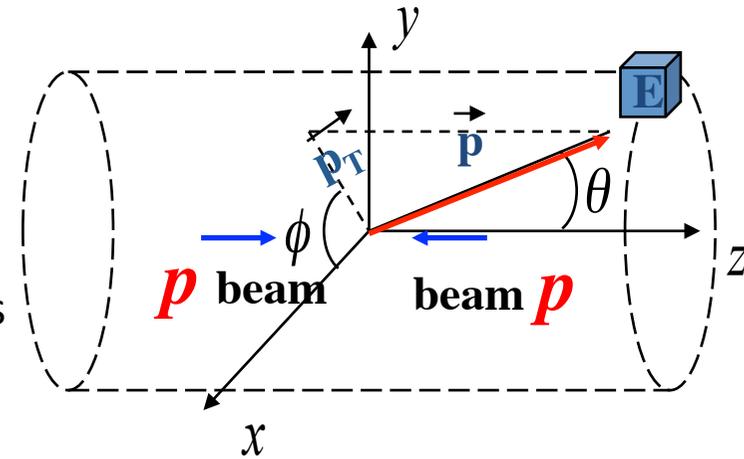
# Variables used in the analysis of $p - p$ collisions

A particle ( $Z, W, e+, e-, \text{etc ...}$ ) is described by its **four-momentum**:

$$\tilde{p} = ( E, p_x, p_y, p_z )$$

The particle mass is  $m = \sqrt{E^2 - p_x^2 - p_y^2 - p_z^2}$

When dealing with  $pp$  collision the following variables are used:



For **each** particle ( $Z, W, e+, e-, \text{etc ...}$ ):

- 1. Transverse momentum/energy :

$$p_T = p \sin \theta \quad E_T = E \sin \theta$$

- 2. Rapidity

$$Y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

or Pseudorapidity

$$\eta = - \ln \left( \tan \frac{\theta}{2} \right)$$

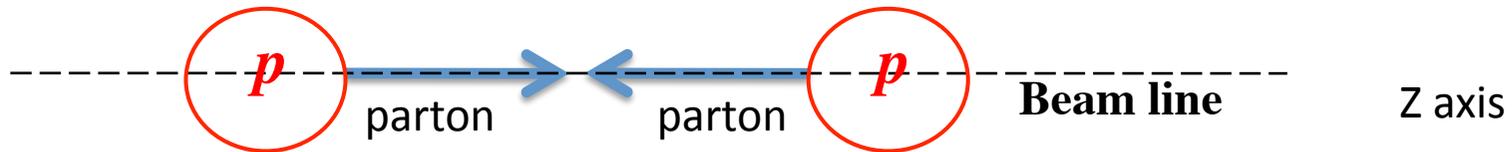
- 3. Azimuthal angle

$$\Phi$$

Why?

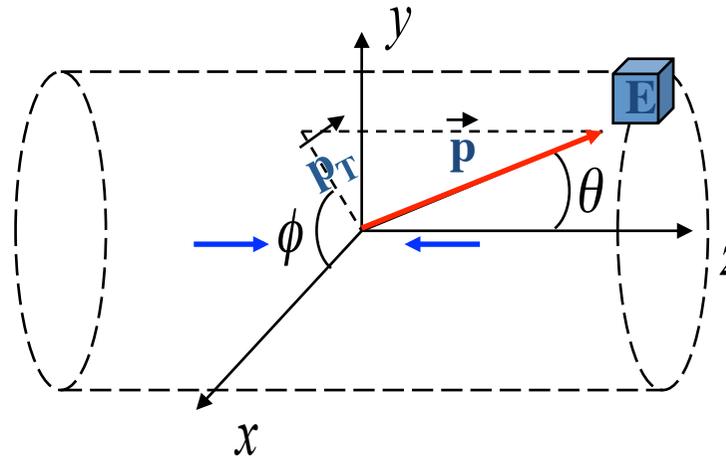
# Variables used in the analysis of $p - p$ collisions

Why? Many reasons.



1. The momentum of each initial parton along beam line is **unknown** while we know that  $\vec{p}_T^{\text{initial parton}} \sim 0$   
→ use transverse quantities (**in the plane  $\perp$  to the beam**) →  $p_T$
2.  $p_T$  and  $\Delta Y$  are invariants for Lorentz transformations along the z axis 
3.  $\sum^{\text{initial partons}} \vec{p}_T = \sum_{\text{vis}} \vec{p}_T + \sum_{\text{invis}} \vec{p}_T \approx 0$  → Allows to evaluate the  $p_T$  of particles not detected ( $\nu$ )
4. The “interesting” physics is due to hard scattering processes → high  $p_T$  particles (selection of high  $p_T$  particles assures “interesting” physics)

## Useful relations



$$\begin{aligned} p_x &= \mathbf{p}_T * \cos(\Phi); \\ p_y &= \mathbf{p}_T * \sin(\Phi); \\ p_z &= \mathbf{E} * \tanh(\eta); \end{aligned}$$

$$\begin{aligned} \mathbf{p}_T &= \mathbf{p} \sin \theta \\ \eta &= - \ln \left( \tan \frac{\theta}{2} \right) \end{aligned}$$

- $m \ll E \quad \rightarrow Y \approx \eta$  (  $\eta$  doesn't require particle identification )
- $m \ll E \quad \rightarrow \mathbf{p}_T \approx \mathbf{E}_T \quad \mathbf{E}_T = E \sin \theta$

# Concept of invariant mass: inclusive Z boson production

$$p - p \rightarrow Z X$$

With  $Z \rightarrow e+e-$

$X = p_1, p_2, p_3, \dots$

Very 'clean' processes (low bkg)!!

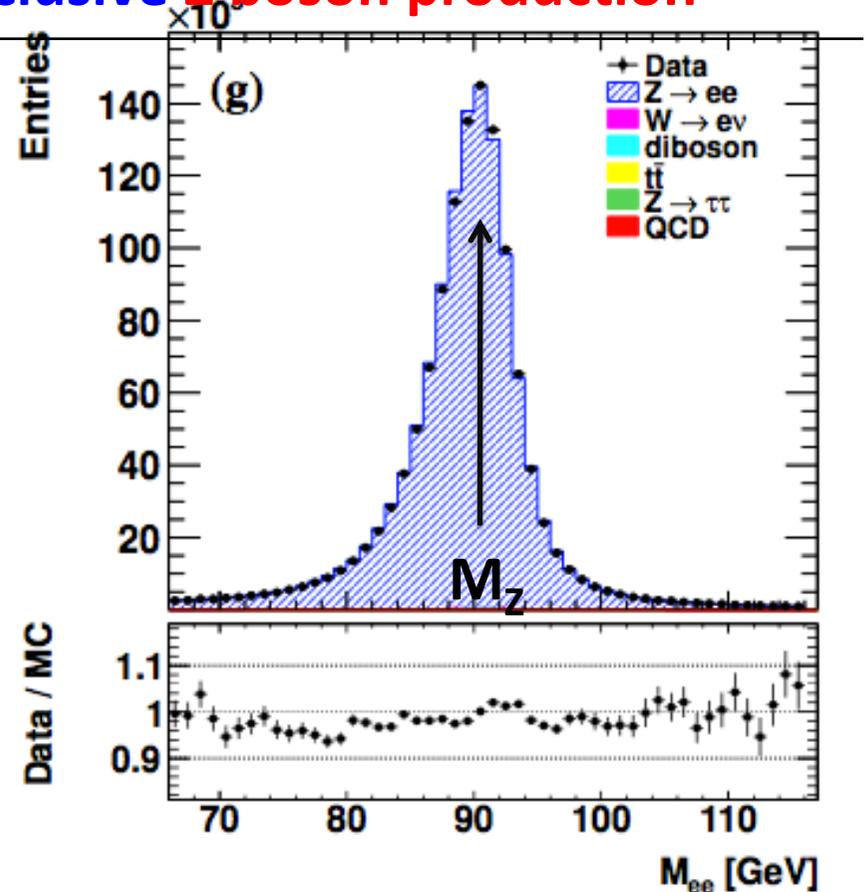
Invariant mass  $M_{ee}$  of  $ee$  system from the 4-momentum conservation  
( it allows to measure the Z mass,  $M_Z$  ):

$$M_{ee}^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2 \approx 2 (E_{e1} E_{e2} - |\vec{p}_{e1}| |\vec{p}_{e2}| \cos \vartheta)$$

$$M_{ee} \approx \sqrt{2 E_{e1} E_{e2} (1 - \cos \vartheta_{e1 e2})}$$

(electron mass is neglected)

Why a distribution?



$$1. \Delta E * \Delta t > \hbar/2 \quad \Delta m * \Delta \tau > \hbar/2$$

$$\Gamma * \tau > \hbar/2$$

width

lifetime

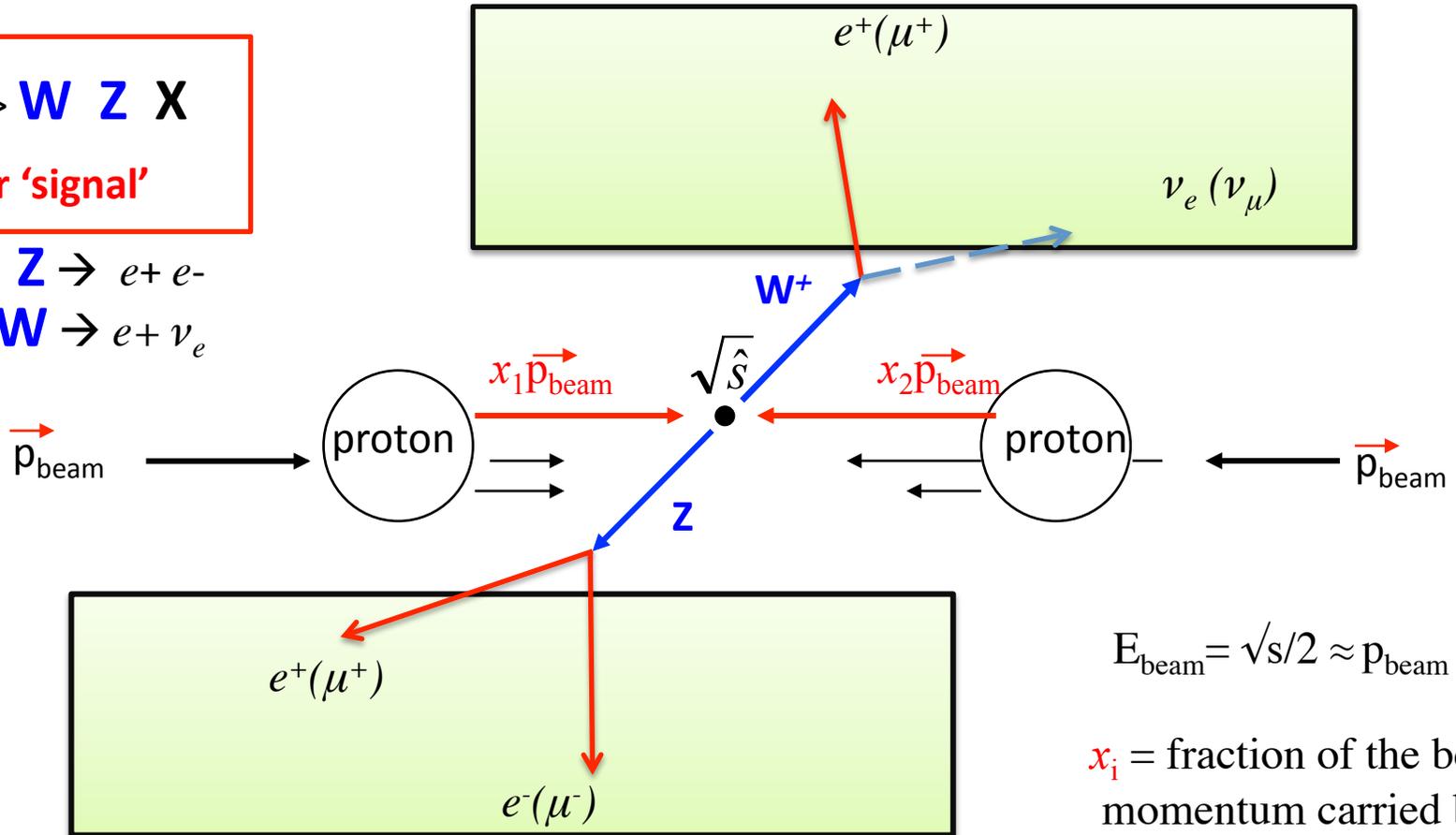
2. Experimental resolution

# Our signal : Production of a W and a Z

$p$ - $p$  'hard' collisions in the  $q_1 \bar{q}_2$  center of mass:

$p$ - $p \rightarrow$  **W** **Z** **X**  
Our 'signal'

With **Z**  $\rightarrow e^+ e^-$   
and **W**  $\rightarrow e^+ \nu_e$



$$E_{\text{beam}} = \sqrt{s}/2 \approx p_{\text{beam}}$$

$x_i$  = fraction of the beam momentum carried by the parton  $i$

$$0 < x_{1,2} < 1$$

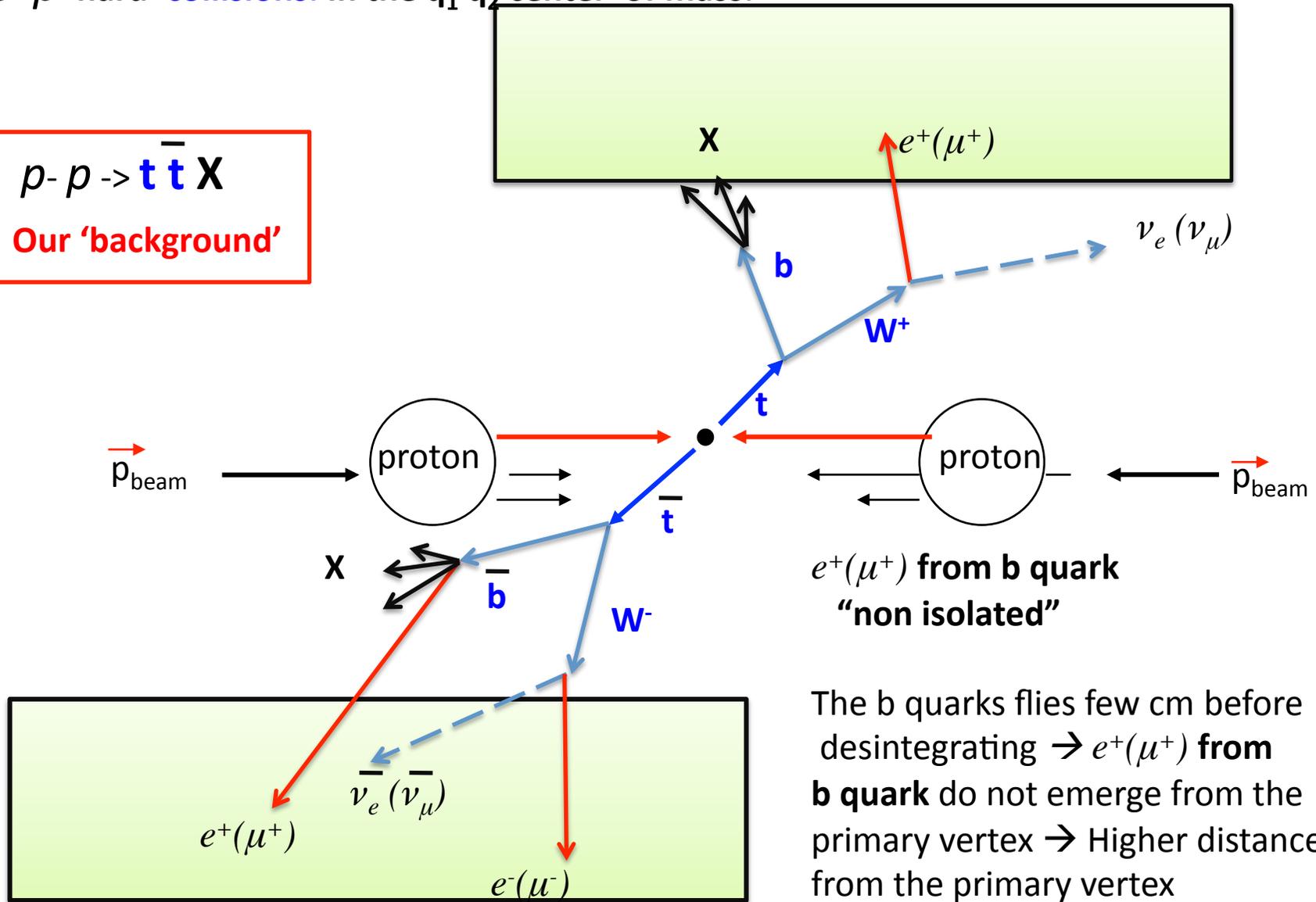
## Kinematics of $p$ - $p$ collisions

★ 4-mom of the initial partons :  $[(x_1+x_2)E_{\text{beam}}, 0, 0, (x_1-x_2) p_{\text{beam}}]$

# Our background: Production of a pair of top-antitop

$p$ - $p$  'hard' collisions. In the  $q_1 \bar{q}_2$  center of mass:

$p$ - $p \rightarrow t \bar{t} X$   
Our 'background'



$e^+(\mu^+)$  from **b quark**  
"non isolated"

The **b quark** flies few cm before desintegrating  $\rightarrow e^+(\mu^+)$  from **b quark** do not emerge from the primary vertex  $\rightarrow$  Higher distance from the primary vertex (higher "impact parameter")

Aim of the exercise:

- 1) look at some important variables,
- 2) build the Z invariant mass,
- 3) how one can discriminate between the 'signal' and the 'background'

On the GRASPA 2014 Web page you will be given :

<https://indico.in2p3.fr/conferenceDisplay.py?confId=9841>

1) an **input file** containing the physics: **Selected\_All\_EEM.root**

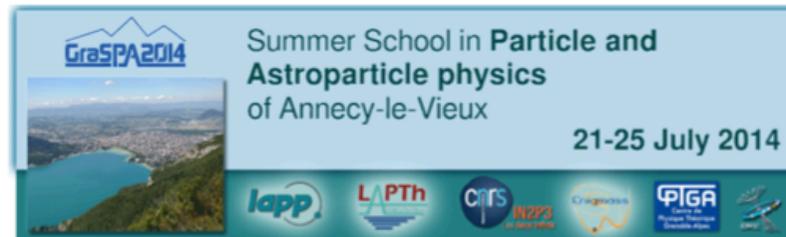
```
==== MOST ENERGETIC LEPTON FROM THE Z  
Br 4 :pt1 : pt1  
Br 5 :eta1 : eta1  
Br 6 :phi1 : phi1  
Br 7 :E1 : E1  
  
==== SECOND ENERGETIC LEPTON FROM THE Z  
Br 8 :pt2 : pt2  
Br 9 :eta2 : eta2  
Br 10 :phi2 : phi2  
Br 11 :E2 : E2  
  
==== LEPTON FROM W  
Br 12 :pt3 : pt3  
Br 13 :eta3 : eta3  
Br 14 :phi3 : phi3  
Br 15 :E3 : E3
```

List given  
per each collision event  
(kinematics of the final  
State leptons)

2) Instructions to make the computing exercise:

**GRASPA 2014**

**21-25 July 2013**



**COMPUTING EXERCISE**

**Study of the production of a pair of gauge bosons at the LHC**

The data to analyse are organised into a Root n-tuple (which we will provide to you). The Root n-tuple is a file containning information about "events", each resulting from a proton-proton interaction. These events have three leptons (electrons or muons) and are of two kind:

### 3) A skeleton of an analysis program using ROOT: **macro.C**

```
#include "TCanvas.h"
#include "TRoot.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
```

4) Useful links:

<http://root.cern.ch/drupal/content/root-primer-534>

<http://root.cern.ch/drupal/content/root-users-guide-534>

Look also to:

**ROOT Tutorial**

5) A 'manual' with ROOT instructions: [Tutorial\\_ROOT\\_Bose.root](#)

Tulika Bose  
Brown University  
NEPPSR 2007

## Example of analysis program

macro.C

23/07/2013 00:21

```
#include "TCanvas.h"
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void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
    sig->SetBranchAddress("eta1",&eta1);
    sig->SetBranchAddress("phi1",&phi1);
    sig->SetBranchAddress("E1",&E1);
    sig->SetBranchAddress("MZ",&MZ);
    sig->SetBranchAddress("Weight",&Weight);
    // add other variables ...
}
```

**Open the input file**

**Access the Signal info**

**Variables per each lepton**

## Access the background info

```
////get some variables for BACKGROUND EVENTS
TTree *ttbar = (TTree*)f->Get("ttbar");
Double_t pt1_bkg, eta1_bkg, phi1_bkg, E1_bkg;
Double_t MZ_bkg;
Double_t Weight_bkg;

//get some variables for ttbar
ttbar->SetBranchAddresses("pt1",&pt1_bkg);
ttbar->SetBranchAddresses("eta1",&eta1_bkg);
ttbar->SetBranchAddresses("phi1",&phi1_bkg);
ttbar->SetBranchAddresses("E1",&E1_bkg);
ttbar->SetBranchAddresses("MZ",&MZ_bkg);
ttbar->SetBranchAddresses("Weight",&Weight_bkg);
// add other variables ...

//create two histograms (for sig and ttbar)
TH1F *h_MZ = new TH1F("h_MZ","MZ distribution All events",40,65,115);
TH1F *h_MZ_bkg = new TH1F("h_MZ_bkg","MZ distribution BKG",40,65,115);
TH1F *h_MZ_sig = new TH1F("h_MZ_sig","MZ distribution SIG",40,65,115);

//read all SIGNAL entries and fill the histograms
Int_t nentries = (Int_t)sig->GetEntries();

for (Int_t i=0;i<nentries;i++) {
    sig->GetEntry(i);
    h_MZ->Fill(MZ,Weight);
    h_MZ_sig->Fill(MZ,Weight);
}
```

**Have fun !!**

